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FEASIBILITY STUDY FOR AN INFLATABLE BOW
RAMP

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Birdair Structures, Incorporated

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13. ABSTRACT A feasibility study for developing an inflatable bow ramp for the LST. The ramp must be 110 ft. long, 16 ft. wide, and carry the maximum loads imposed by an M103 tank. Ten possible conceptual configurations were investigated with a more detailed design analysis effort being concentrated on two of the concepts. The ramp will be constructed of a two ply neoprene fabric and inflated with an inflation system separate from ship air supply. A scale model of one concept was built and tested which verified design calculations.			

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**FEASIBILITY STUDY
FOR AN
INFLATABLE BOW RAMP**

**BIRDAIR JOB NO. 7258
NAVY CONTRACT NO. N62399-73-C-0003**

JUNE 21, 1973

TABLE OF CONTENTS

	PAGE
INTRODUCTION	1
DESIGN ASSUMPTIONS	5
DESIGN ANALYSIS	6
GENERAL COMMENTS ON FABRIC STRENGTH AND PRESSURIZATION SYSTEMS	3
CONCEPTUAL CONFIGURATIONS & PRELIMINARY FEASIBILITY EVALUATION	9
REFINED DESIGN ANALYSIS FOR CONCEPT NO. 2	21
REFINED DESIGN ANALYSIS FOR CONCEPT NO. 10	25
DISCUSSION & REMARKS	33
GENERAL CONCLUSION	41
REFERENCES	
APPENDIX A: LOAD AND MOMENT CALCULATIONS	
APPENDIX B: DERIVATION OF EQUATIONS	
APPENDIX C: PRELIMINARY DESIGN CALCULATIONS	
APPENDIX D: REFINED DESIGN CALCULATIONS	
APPENDIX E: MODEL ANALYSIS FOR CONCEPT NO. 10	
APPENDIX F: DEFLECTION THEORY	
APPENDIX G: PRESSURIZATION CALCULATIONS	

INTRODUCTION

The purpose of this study is to perform a preliminary conceptual design investigation, and make recommendations as to the feasibility of an inflatable bow ramp for the 1179 Class LST (Landing Ship Tank). The new 1179 Class LST has an over-the-bow ramp for roll-on, roll-off assault vehicles and MCB (Mobile Construction Battalion) construction equipment. The present ramp is approximately 16 ft. wide, 6 ft. deep, 100 ft. long, and weighs 36.6 short tons. It is a welded aluminum structure, and is stowed on the main deck level. See Photos, on Page 4.

The following performance requirements for the inflatable bow ramp were authorized by the Navy, and were treated as design parameters. The refined design analysis will attempt to satisfy as many of the parameters as possible.

Performance Requirements

- A. Concept. The inflatable ramp shall form a bridge for the transfer of military vehicles between the ship and a beach or pontoon causeway. The shipboard end of the ramp must be free to rotate horizontally through an arc of 15 degrees to port or starboard (30° excursion) of the ship's centerline. The causeway end of the ramp must be free to rotate through an arc of 12 degrees to port or starboard of the causeway centerline as well as move 20 feet longitudinally. The bearing surfaces of the ramp shall be designed to resist the forces generated by friction due to the ship's motion. The ramp shall be capable of accommodating ± 10 degrees of ship roll when the outboard end of the ramp is supported on a causeway.

B. Ramp Size. The ramp shall have a minimum length of 110 feet and minimum width of 16 feet such that unrestricted passage of military vehicles up to the M-103 tank and construction equipment used by the MCB's is possible. MCB equipment includes such vehicles as scrapers, truck cranes and low-boy trailer/tractors. The vertical inclination of the ramp will vary from 10 to 20 degrees for the 110 foot ramp.

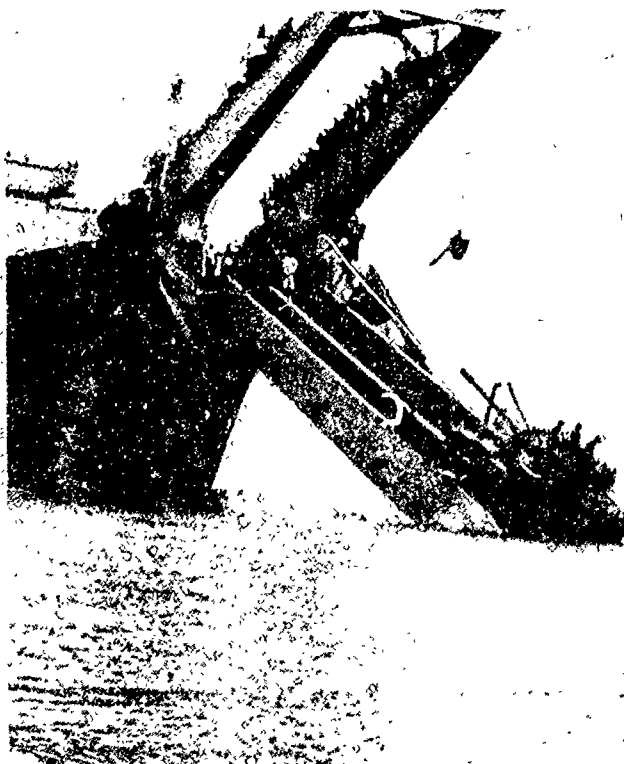
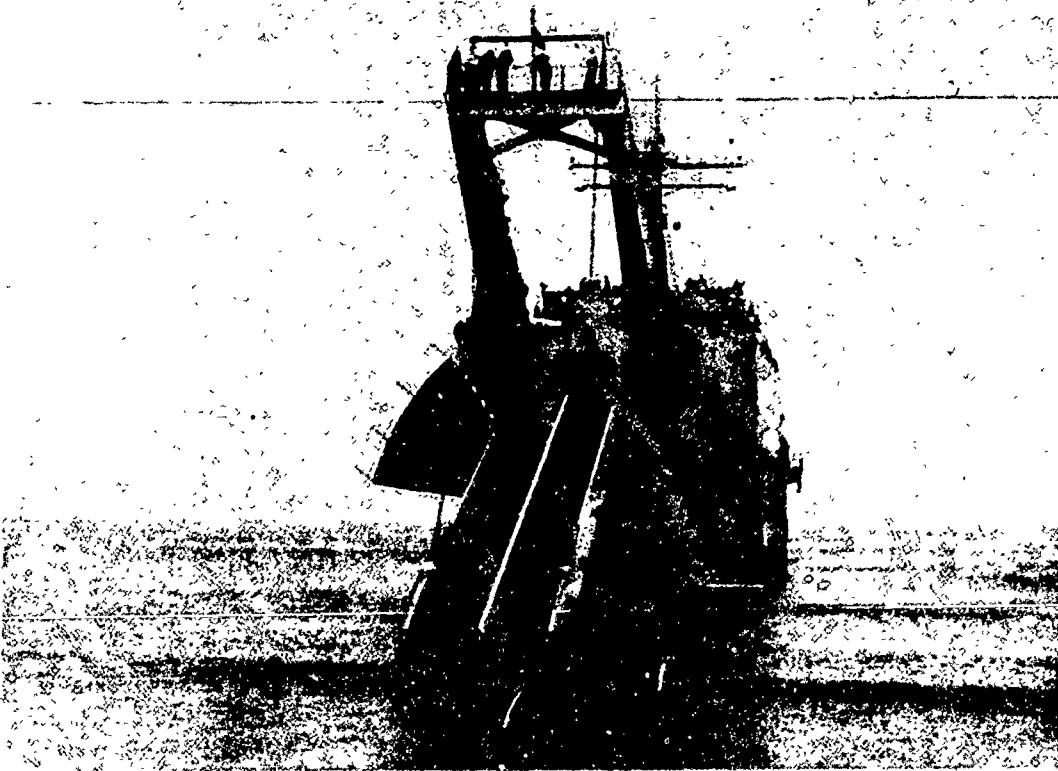
C. Design Loads. The ramp shall be capable of supporting the loads imposed by the M-103 tank (60 tons) and AASHO (American Association of State Highway Officials) H20 wheel loading in the fully extended position. Intermediate ramp supports may be incorporated into the inflatable ramp system. The ramp shall be capable of supporting the local loading of military vehicles with tracks and pneumatic tires.

D. Operational Requirements. Complete extension or retraction of the ramp shall be accomplished in no more than ten (10) minutes in winds up to 30 knots. In the beaching conditions, provisions shall be made to assure negative buoyancy when the outboard end is lowered into 4 feet of water with 5-foot breaking waves.

E. Special Requirements.

1. The ramp surface used for vehicle traffic shall be designed to assure positive traction for all vehicles at the maximum ramp inclination (20 degrees). Positive traction shall be maintained when vehicles move over the transition zones at both ends of the ramp.

2. The ramp shall be designed for Grade "A" shock loads according to ~~Military Specification S-901C (Navy) in its stowed position.~~
3. The ramp shall withstand the forces imposed by green seas and ship motions in storm conditions while stowed.
4. The ramp stowage configuration shall be as compact as practical to conserve deck space.
5. The ramp shall be designed to absorb damage by enemy action without compromising its structural integrity.
6. The ramp inflation system shall be self replenishing for multiple use.
7. Repair of the ramp shall be within the capability of shipboard personnel and equipment.
8. The life cycle cost of the inflatable ramp shall be comparable to the existing bow ramp.



DESIGN ASSUMPTIONS

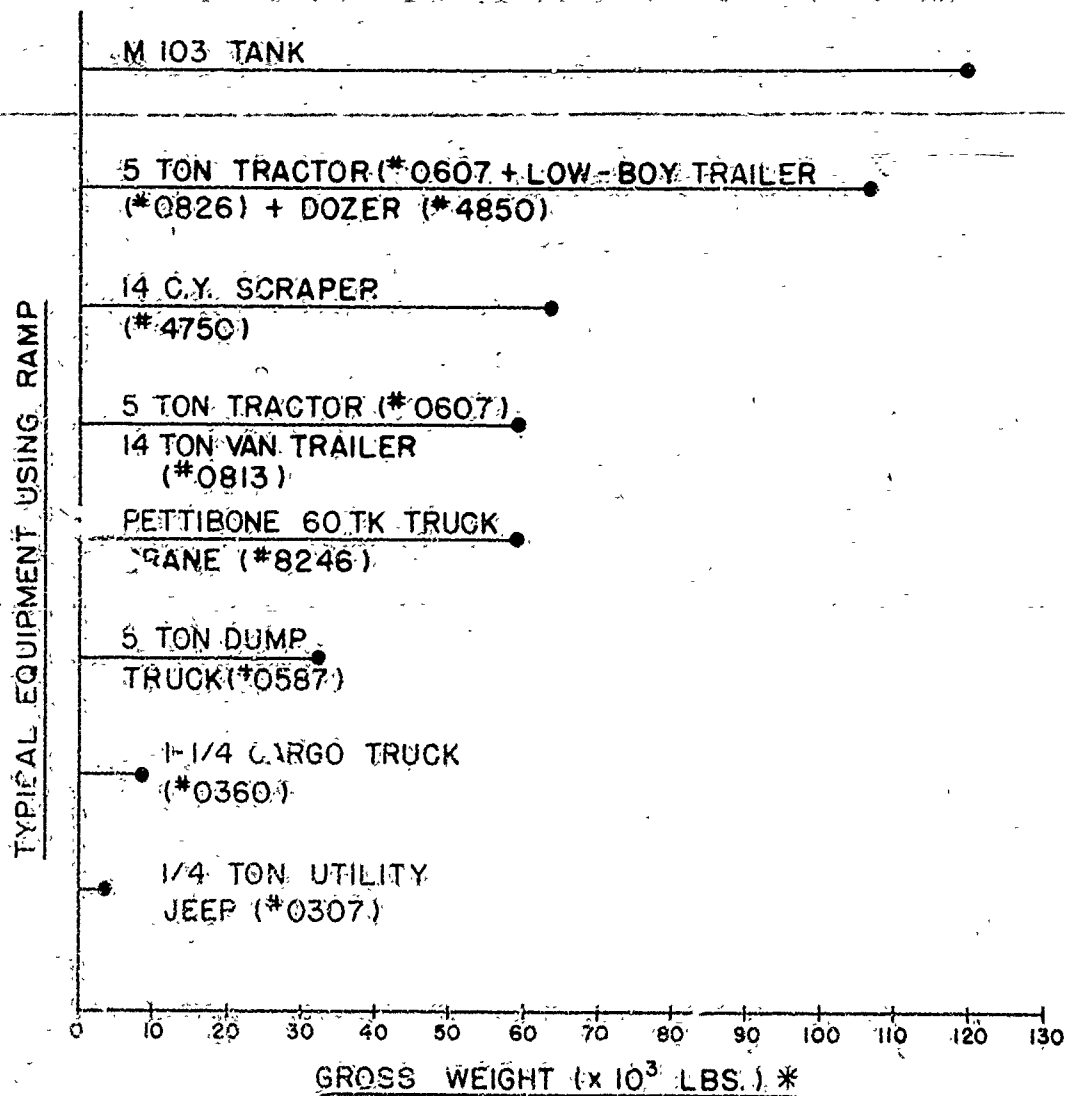
~~Since the inflatable bow ramp will be loaded with a variety of vehicles~~ ranging from a 60 ton tank to a 1/4 ton jeep, a bar graph showing typical vehicles and gross weights of each was prepared in order that a graphical relationship of loads could be visualized (refer to Figure No. 1). These vehicles, with the exception of the M103 tank, fall under the P-25 allowance of automotive equipment.

Conversely, the bending moments that are created for different load situations as vehicles move along the ramp were computed and are plotted in Figure No. 2. This is assuming that only one vehicle was on the ramp at a time. Refer to Appendix A for the calculations.

The inclination of the ramp is also important in determining the vertical load component of the force normal to the roadway surface. For a conservative design, however, the ramp was considered to be in a horizontal position, therefore creating the maximum vertical component of the force equal to the weight of the vehicle. The effects of the horizontal force created along the ramp at maximum inclination (20°) will be discussed in the refined design portion of the report.

Since the M103 tank is the heaviest of the vehicles normally using the bow ramp, the preliminary design for each of the conceptual configurations is based on a concentrated point load of 60 tons moving along the ramp, which has a clear span of 110 feet. This again is a slightly conservative design assumption, since the tank load is actually distributed over a length of tracks (174 in.). Also, the total length of the bow ramp is 110 feet, indicating that after supporting the ramp at each end, the actual clear span is something less than 110 feet.

WEIGHT COMPARISON OF TYPICAL VEHICLES USED ON BOW RAMP



* GROSS WEIGHTS LISTED ARE BASED ON PAYLOADS
FOR CROSS-COUNTRY TRAVEL

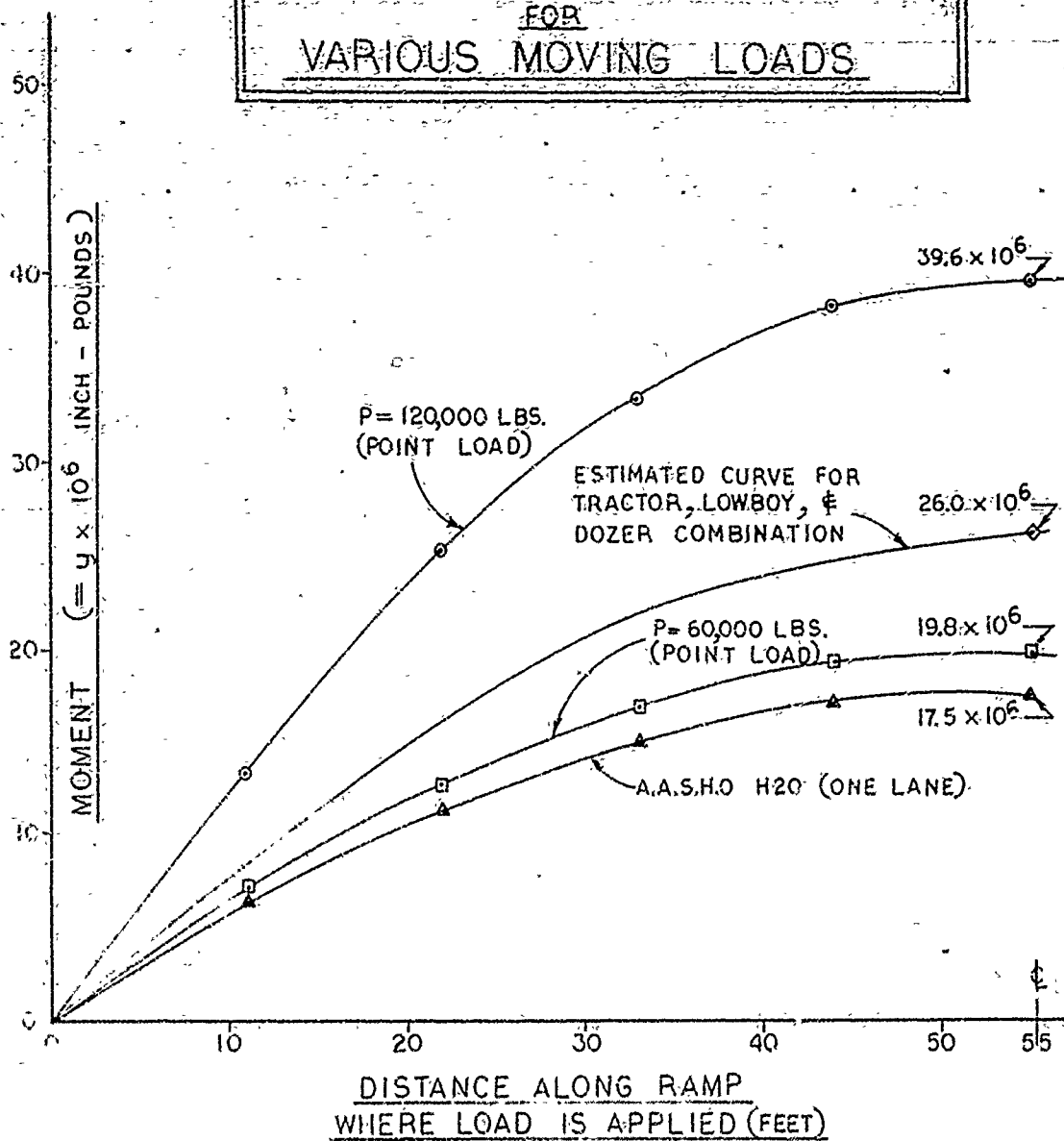
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VEHICLE LISTING

FIGURE 1

SHEET

RESULTANT BENDING MOMENTS FOR VARIOUS MOVING LOADS



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BENDING MOMENT GRAPH

FIGURE 2

SHEET

DESIGN ANALYSIS

Appendices B and F of this report explain the derivation of equations used to analyze the various fabric stresses, inflation pressures, and deflections that will be anticipated in the inflatable bow ramp. The derivations are rather self-explanatory if followed through in a systematic manner.

The basic theory applied to analyzing a structure of this type is commonly referred to as "initial wrinkle theory." That is, inflating a structure to a point where the tension in the fabric due to inflation pressure equals the compression force along the fabric due to bending moment. Theoretically, when these two forces are equal, the structure should just start to wrinkle. Tests have shown that the structure will not collapse at this point, however, but that only local wrinkling in the upper skin at the point of the load will be initiated. Actual collapse typically occurs when approximately twice this design load is applied to the structure.

The basic formulas used in analyzing an inflated beam with the initial wrinkle theory are:

INFLATION STRESSES

$$F = p A \quad (\text{EQ. 1})$$

where F = Force on Fabric

p = Inflation Pressure

A = Cross-Sectional Area

$$S_i = F/C \quad (\text{EQ. 2})$$

where S_i = Fabric Stress per Unit (1")

$$F = S_i C$$

Width due to Inflation Pressure

C = Circumference of Section

Therefore,

$$S_i C = pA \quad (\text{Eq. 3})$$

$$S_i = \frac{pA}{C}$$

BENDING STRESSES

$$\text{Resistive Moment} = (F_s) (A) \quad (\text{Eq. 4})$$

where f_s = Stress in Skin per Unit Width
of Fabric (tension or compression)

Since the skin must be pretensioned by inflation pressure to resist compression loads produced by bending moment (initial wrinkle theory), then

$$S_i = f_s$$

$$\frac{pA}{C} = \frac{M}{I}$$

M = Bending Moment

Required inflation pressure to carry bending moment

$$p = \frac{CH}{A^2} \quad (\text{Eq. 5})$$

The maximum longitudinal fabric stress is in the tension zone of the structure, and is equal to $S_i + f_s$. Since $S_i = f_s$, the maximum longitudinal fabric stress = $2 S_i$.

The maximum transverse fabric stress = pR where R = radius (simple hoop stress).

It should be noted that initial wrinkle theory was used on all of the preliminary conceptual configurations, except Nos. 3, 6, 9, and 10 (see Figure 3). In concepts 3 and 6 the basic formulas for hoop tension governed since the inflated fabric portion was not required to resist bending moment. In concepts 9 and 10, special hybrid structures were investigated, which made use of aluminum structural components, along with fabric bladders. The theory used to evaluate these hybrid structures is discussed later in the report.

GENERAL COMMENTS ON FABRIC STRENGTH AND PRESSURIZATION SYSTEMS

Fabric

A study of various materials available on the market, excluding the exotic state-of-the-art types still being researched, indicate that a range of fabric strengths could go as high as 3000 to 4000 pounds per inch tensile strength. Fabrics with these high strengths are usually several plies and become difficult to handle. From past experience, however, considering toughness and workability, fabric strengths up to 1000 pounds per inch would be considered in a normal range.

A more detailed report on fabric types and makeup, along with actual test reports, is included with the refined design study at the end of the report.

Pressurization

Upon reviewing various types of inflation systems that are available, many were dropped from further consideration on the basis that they could not deliver the large volume and relatively high pressures that are required to quickly inflate the ramp for the specified 10 minute deployment time. It was also found that in the systems available, for pressures over 10 psi, there was a substantial jump in the horsepower required to drive the unit. For these reasons then, a normal range of inflation pressures of 0 to 10 psi were considered in the preliminary investigation.

A more detailed report on inflation systems is included with the refined design analysis at the end of the report.

CONCEPTUAL CONFIGURATIONS AND PRELIMINARY FEASIBILITY EVALUATION

Much research was conducted in order to review and summarize current state of the art and structural forms that might be applicable to the specific requirements for the inflatable bow ramp. Various agencies or organizations that were in any way connected with research that might apply to this study were contacted; the information gathered is tabulated in the list of references at the end of the report. It might be noted that the English at the Military Engineering Experimental Establishment at Christchurch, Hampshire, England seem to be the foreleaders in developing and testing various inflatable, single span bridges. These bridges ranged in spans from 20 to 30 feet; and carried loads in the neighborhood of 1 to 1 1/2 tons. As information on this work was the only data available that was directly related to inflatable bridges of the type that we are concerned with, and since our design requirements were of a nature that far exceeded those used by the English, it was imperative that a new and completely unique type of structural form or forms must be developed to carry the high loads (60 tons) over the relatively long clear span of 110 feet.

With this in mind, we were able to arrive at ten different preliminary conceptual configurations. These preliminary designs spanned a wide range of conceivable means of using the inflated structure principle. Refer to Figure 3 which shows a general elevation and section view of each configuration, along with a chart showing a comparison of various properties of each concept. The preliminary design calculations for each concept are shown in Appendix C, and a brief discussion of each,

with specific reference to the calculations, will follow. The preliminary design information was tabulated and a review and evaluation of each concept was conducted at a meeting between Birdair and Navy personnel in order to arrive at one or more concepts to consider for refined design. The factors that were used in evaluating the feasibility of each concept are listed on Figure 3, along with additional comments that follow.

Refer to Figure 4 which lists possible operational methods for each concept; and Figure 5 which tabulates the required fabric strength that is required after the dead load of the structure is added to the fabric stress and then a factor of safety of three applied.

It should also be noted that in each concept, some type of roadway surface or decking is required to protect the fabric from abrasion under track vehicles, and also to maintain positive traction for vehicles using the ramp.

Some research was conducted in determining various materials which might be applicable for the roadway surface. Since the surface should probably be flexible and have the ability to be rolled or folded for storage, the following materials were under consideration:

- (a) Non-skid conveyor belt fabric (photo No. 1). This material is light weight and flexible, and could easily be bonded to the fabric ramp. Lab tests conducted by Birdair indicate that the coefficient of friction between this material and neoprene is approximately .6, and when in contact with steel, approximately .5.

CONCEPTUAL CONFIGURATIONS		SPAN - 110 FT. DESIGN LOAD - 60 TON	MAX. FABRIC STRESS (PSI)	INFLAT PRESS (PSI)	APPROX. VOL. (FT ³)	APPROX. FABRIC WGT. (TONS)	ATTACK VALUE OF ABILITY	EFFECT OF WAVES	EASE OF OPER.	WEAVING INCLINE ANGLE	COST
1-DUALWALL BEAM		ROADWAY	170.4	16	26,400	23.9	1-2	1	1	1	2
2-DUALWALL BEAM WITH SUPPORT		ROADWAY	692	6.4	29,500	11.0	1-2	2	1-2	2	1-2
3-DUALWALL WEDGE		FLEX. DECK	250	10	33,000	9.5	1	3	2	3	3
4-DUALWALL TUNNEL		ROADWAY	624	8.7	40,980	24.4	2-3	1	2-3	1	3
5-ARCH		CABLE SUSPEND. ROADWAY	776	7.4	21,856	15.2	3	1	1-2	1	2
6-REVERSE SUSPENSION		TENSION SLING INFLATABLE FILLER ROADWAY	674	14	28,658	12.8	3	2-3	1-2	1	2-3
7-TUBES WITH SUPPORT		DUALWALL ROADWAY VARY INFL. PRESS. TO CONTROL HT. STL. TRACK	1423	23.7	19,601	16.4	3	2	2-3	2	2
8-TUBE TUNNEL		ROADWAY	RANGE 456 2736	RANGE 10-57	22,117	25.5	3	1	2-3	1	2-3
9-HYBRID-TRUSS & INFLATED BLADDER		BLADDER RIGIDIZED ROADWAY ALUM. TRUSSES	161	5	10,960	1.3	2	1	1	1	1-2
10-HYBRID-COMPRESSION DECK & BLADDER		DUALWALL BLADDER CABLES COMPRESSION DK.	108	3.6	7,306	1.2	2	1	1	1	1-2

SCALE - 1" = 40'

NOTES -

① DESIGN IS BASED ON MAX. BENDING MOMENT CREATED BY A 60 TON CONCENTRATED LOAD. WGT. OF STRUCTURE WAS NEGLECTED FOR PRELIMINARY DESIGN.

② EXCLUDES WGT. OF SUPPORT TUBE

SCALE - 1" = 30'

③ WEIGHTS SHOWN DO NOT INCLUDE THE WGT. OF STL. TRUSSES, DECKING OR CABLES.

ON SCALE 1-3
1 EQUALS BEST CHOICE

FIGURE 3

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OPERATIONAL METHODS

1 DUALWALL BEAM



1. HOIST TO HORIZONTAL POSITION
2. DEFLATE SIDES & WINCH ONTO DECK
3. DEFLATE REMAINING SECTION
4. ROLL UP, FOLD FOR STORAGE
5. REVERSE ORDER FOR DEPLOYMENT

2 DUALWALL BLANK SUPPORT



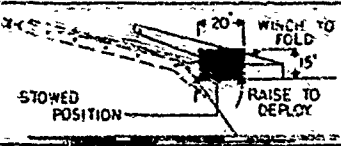
1. HOIST HINGE POINT TO HIGHEST POSITION
2. DEFLATE SUPPORT TUBE
3. WINCH IN EXTENDED POSITION
4. DEFLATE DUALWALL & DECKS TOGETHER
5. REVERSE ORDER FOR DEPLOYMENT

3 DUALWALL WEDGE



1. ROLL UP DECK
2. DEFLATE DUALWALL CELLS
3. WINCH EXTENDED BULKHEAD TOWARD SHIP
4. HOIST DEFLATED SYSTEM INTO POSITION
5. REVERSE ORDER FOR DEPLOYMENT

4 DUALWALL TUNNEL



1. DEFLATE SIDEWALLS & TOP
2. HOIST FOR FAST DEPARTURE
3. DEFLATE BOTTOM & FOLD ONTO MAIN DECK
4. TO DEPLOY—DUMP OVERBOARD, INFLATE, POSITION WITH CABLES

5 ARCH



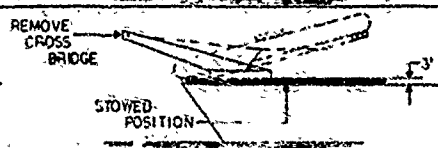
NOTE: BECAUSE OF THE LARGE WIDTH, NO PRACTICAL OR FEASIBLE ATTACHMENT METHOD HAS BEEN DEvised.

6 INVERSE SUSPENSION



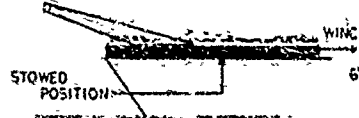
1. RELEASE PRESSURE, OPEN VALVES
2. WIND IN FORCING AIR OUT
3. SEQUENCE DEFLATION WITH WINDING RATE
4. REVERSE ORDER FOR DEPLOYMENT USING CABLES TO POSITION RAMP

7 TUBE SUPPORT



1. DEFLATE SUPPORT TUBE
2. WINCH TO VERTICAL POSITION USING OUTRIGGERS & ON LEVEL DECK
3. LOWER TO MAIN DECK & DEFLATE
4. REVERSE ORDER FOR DEPLOYMENT

8 TUBE TUNNEL



1. DEFLATE TOP TUBES—LOWER RIGID ENDS
2. HOIST TO HORIZONTAL POSITION
3. WINCH ONTO MAIN DECK
4. DEFLATE BOTTOM TUBES FOR STORAGE
5. REVERSE ORDER FOR DEPLOYMENT

9 H-BRID—TRUSS & BLADDER



1. HOIST TO HORIZONTAL POSITION
2. DEFLATE SIDES & WINCH ONTO MAIN DECK
3. DEFLATE BLADDER
4. SLIDE TRUSSES TOGETHER FOR STORAGE
5. REVERSE ORDER FOR DEPLOYMENT

10 H-BRID—CLAMP DECK & BLADDER



1. HOIST TO HORIZONTAL POSITION
2. DEFLATE SIDES & WINCH ONTO MAIN DECK
3. DEFLATE BLADDER
4. REVERSE ORDER FOR DEPLOYMENT

NOTES:

SCALE: 1" = 40'

DIMENSIONS SHOWN ARE APPROXIMATE


FIGURE 4



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CONCEPTUAL CONFIGURATIONS		SPAN - 110 FT. DESIGN LOAD - 60 TON		MAX. FABRIC STRESS (PSI)	INFLAT. PRESS. (PSI)	APPROX. VOL. (FT ³)	FABRIC TYPE	
				(PSI)	(PSI)	(FT ³)	45 BIAS	2 ST. PLY
1-DUALWALL BEAM				6132 2044 340 1704	16	26400	23.9	
2-DUALWALL BEAM WITH SUPPORT				2262 754 62 692	64	29150	11	2FB15.5N70 2FB15.5H70
3-DUALWALL WEDGE				750 250	10	33000	9.5	2NI2N56 2NI2H56 2DI2.5N56 2DI2.5H56
4-DUALWALL TUNNEL				2247 749 125 624	8.7	40980	24.4	2FB19N76 2FB19H76
5-ARCH				2619 873 97 776	74	21856	15.2	2FB19N76 2FB19H76
6-INVERSE SUSPENSION				2235 745 71 674	14	28658	12.8	2FB15.5N70 2FB15.5H70
7-TUBES WITH SUPPORT				5068 1686 263 1423	23.7	19601	16.4	2FB21N76 2FB21H76
8-TUBE TUNNEL				1668 10008 RANGE 456 2736	RANGE 10-57	22117	25.5	
9-HYBRID-TRUSS & INFLATED BLADDER				483 161	5	10960	1.3	2N8.5N49 2N8.5H49 2D7.6N49 2D7.6H49
10-HYBRID-COMPRESSION DECK & BLADDER				324 108	3.6	7306	1.2	2N5N42 2N5H42 2D6N42 2D6H42
NOTES		SCALE 1" = 40'	SCALE 1" = 30'					
O = DESIGN FABRIC STRESS (FACTOR OF SAFETY = 3)								

FIGURE 5



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FIGURE 5



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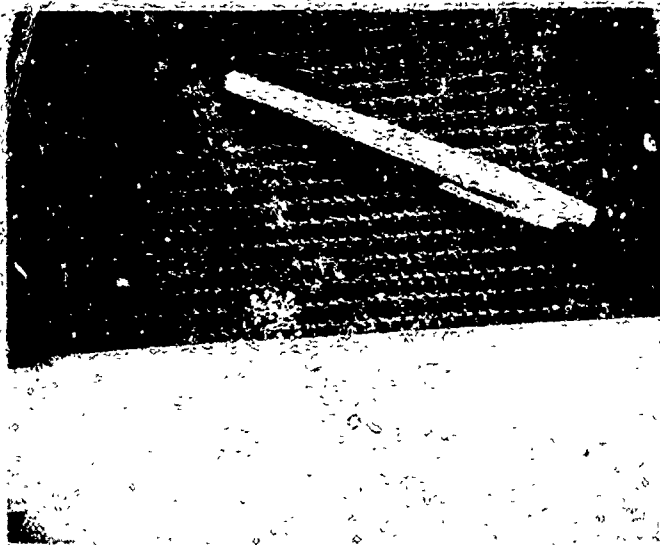


PHOTO #1

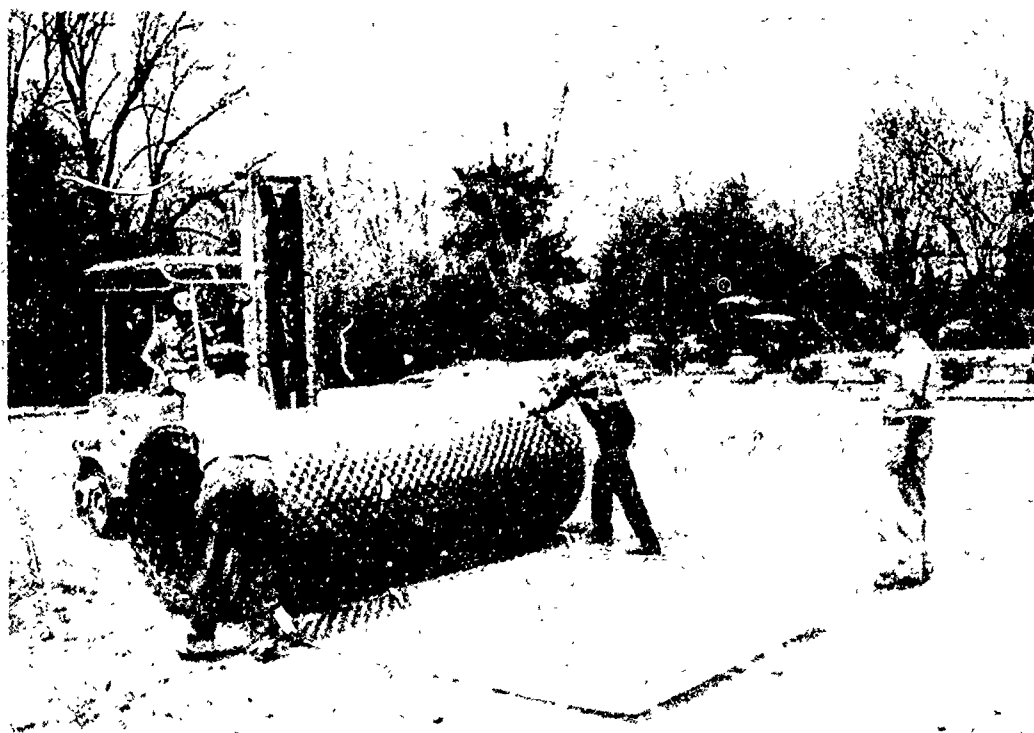


PHOTO #2

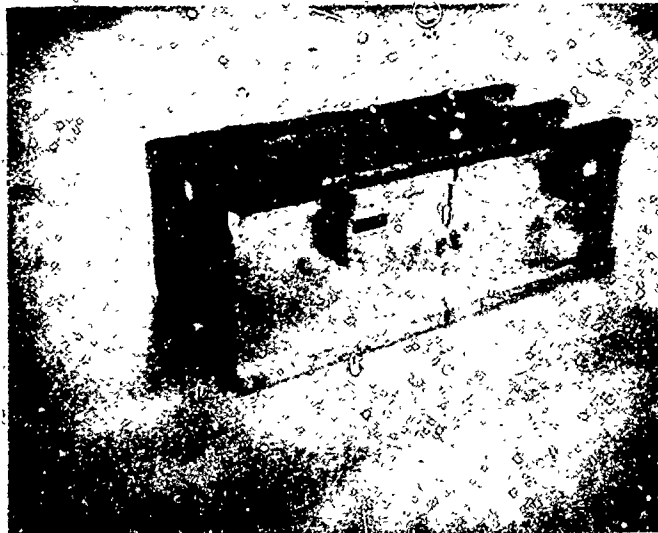


PHOTO # 3

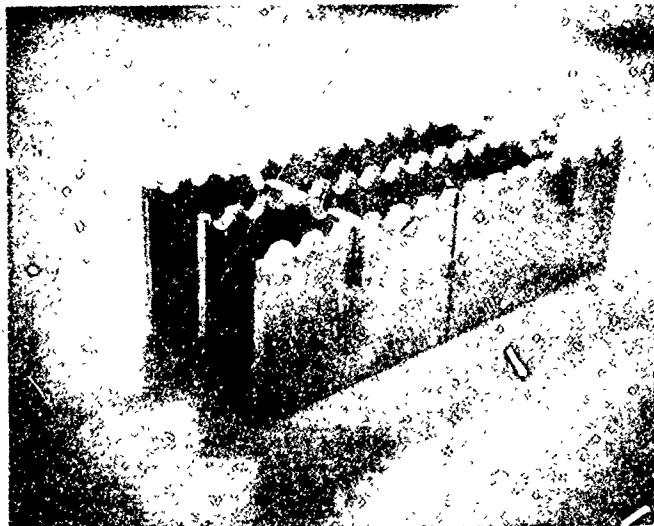


PHOTO # 4

- (b) A type of landing mat (MO-MAT) that is used in the military was also under consideration because of its flexibility (Photo No. 2). No information was readily available that stated coefficients of friction. This type of material would have to be stiffened up structurally in the transverse direction in order to distribute wheel loads.
- (c) A rigid type of aluminum grating that could possibly be folded is shown in Photos 3 and 4. Coefficients of friction vary according to the type of surface, and panels are available in various sizes.

Concept No. 1 - Dual-Wall Beam

The basic idea in this concept was to form a beam which would span the full 110 ft. It would consist of an upper and lower fabric skin, with a series of vertical fabric webs which would maintain the shape of the ramp and carry the shear loads along the ramp. Thus it is of the simplest air structure form: a dual-wall beam, or, if the webs are replaced with drop cords, airmat. In order for the top skin to carry the compressive force created by the bending moment, the structure must be inflated to a theoretical point at which the tension due to inflation pressure equals the compression due to bending moment (initial wrinkle theory). Likewise, the tension in the bottom skin is the summation of the tension due to inflation pressure, plus the tension due to bending moment.

On that basis then, the fabric stresses and inflation pressures required to resist the maximum bending moment for varying depth sections were computed. A graph of the results is shown on Page C 4 and, assuming a

maximum depth of 150 inches at midspan is the optimum, an inflation pressure of 15.7 psi is required with the maximum fabric stress of 1704 lbs. per inch. After adjusting the fabric stress for dead load of the ramp, and then applying a factor of safety of three, the required fabric strength is 6132 lbs. per inch (refer to Figure 5).

After review, this concept was dropped from continuing study for the following reasons:

- (a) In keeping with fabric types that are readily available on the market, there is no fabric that will meet the required strength of 6132 lbs. per inch, and still maintain the flexibility that is required for ease in constructing and handling a structure of this size.
- (b) Also, the high inflation pressure of 15.7 psi presents some problems in selecting an inflator that will inflate the ramp in 10 minutes. It should be noted, however, that if lighter loads and shorter spans were considered, this concept might prove to be very feasible.

Concept No. 2 - Dual-Wall Beam with Support

The idea here was the same as Concept No. 1, except that by using a support at midspan, the bending moment would decrease, therefore allowing the inflation pressure and fabric stress to decrease. Assuming again an optimum depth of 150 inches (refer to Page C 5), the inflation pressure required is 6.4 psi, and the fabric stress is 692 lbs. per inch. After adjusting the fabric stress for dead load, and then applying a factor of safety of three, the required fabric strength is 2262 lbs. per inch (refer to Figure 5).

After review, this concept was considered to have some possibilities for a more refined design. The fabric strength required is rather high, but not out of reach of some of the newer fabrics on the market. With the inflation pressure of 6.4 psi, there is no problem in finding an inflator that can deliver the volume of air required to get the structure up to pressure in 10 minutes.

The effects of more than one intermediate support should be considered in the refined design analysis.

Concept No. 3 - Dual-Wall Wedge

The principle here was to form an inflatable wedge that simply carries the load by floating on the water. The ramp would consist of a series of vertical dual-wall sections (see Page C 20) that, when inflated, would be bound together by a cable or web system. The inflation pressure required would be directly related to the local wheel or track loading, and in this case would be 10 psi. Fabric stress then is a function of cell diameter, and, for a 50-inch cell diameter, the resulting fabric stress is 250 lbs. per inch (see Page C 19). Applying a factor of safety of three, the required fabric strength is 750 lbs. per inch.

Although the fabric strength required is well within the limits of fabric types available, the inflation pressure is a little high for the inflation systems being considered.

Other, and probably more important, reasons for not pursuing this concept are the fact that this rigid type of wedge cannot accommodate varying degrees of inclination that are required for use on a causeway, or when landing on a beach. Also, since the wedge has a large surface

area, the contact of 5 ft. breaking waves, along with the effects of 30-knot winds, make it possible to develop a moment of 39 million foot pounds at the shipboard end of the ramp. Therefore, guying or anchoring of this wedge concept is required when high winds and waves exist. A final point to be considered is the buoyancy effects of the ramp as a 60-ton tank moves across. As the tank first leaves the ship and debarks down the ramp, high shear stresses are developed at the shipboard end of the ramp. Provision must be made to handle these shear stresses until an appropriate volume of water is displaced to offset the weight of the tank. Also, as the tank approaches the extended end, approximately the last 20 feet will sink and rest on the bottom in 4 feet of water. Reference graph on Page C 28. This situation alone creates difficulty with transition areas between the extended end of the ramp and a floating causeway. For these reasons then, this concept was dropped from further investigation.

Concept No. 4 -- Dual-Wall Tunnel

The idea here was to create the required depth of section to carry the bending moment, and in so doing make use of a box section in which the vehicles actually debark along the inside of the section. The design method is similar to Concept No. 1, that is, the fabric must be pre-tensioned with enough inflation pressure to resist the compressive force due to bending moment. Inflation pressure versus cell depth is plotted on Page C 31; for an optimum depth of 6 feet, an inflation pressure of 0.7 psi is required and the maximum fabric stress is 624 lbs. per inch. Adjusting this figure for dead load and applying a safety factor of three, the required fabric strength is 2247 lbs. per inch (reference Figure 5).

The fabric strength and the inflation pressure fall within the limits of materials available to handle the requirements; however, the size and vulnerability from enemy attack, along with an appropriate method for operating this concept, presented some questionable areas. For these reasons then, this concept was dropped from further consideration.

Concept No. 5 - Arch

The theory in this concept was to form two parabolic-shaped tubes which would in turn support a roadway system by a series of suspension cables. A computer program was written that analyzes the moment on the arch as the load moves along the roadway. It should be noted that the tank loading was distributed over three cables per side. The results are shown on Page C 54. Then, applying the initial wrinkle theory (as used in the preceding dual-wall concepts), it was found that for a 10 foot diameter tube, an inflation pressure of 7.4 psi and a fabric stress of 776 pounds per inch were required. (See graph on Page C 58.) After adjusting the fabric stress for dead load and applying a factor of safety of three, the required fabric strength is 2619 pounds per inch. Again, the fabric strength and inflation pressure fall within the limits of materials available to meet these requirements. However, the size of this concept left us with no feasible or practical method of attaching the arches to the ship. Also, the great vulnerability from enemy attack associated with quick collapse led us to the conclusion that this concept did not justify further investigation.

Concept No. 6 - Inverse Suspension Concept

The idea in this concept was to form an inflatable system in which tubes acting much like rails would carry the compression loads independent of the rest of the structure. The tension loads would be carried by a cable sling which would be attached at each end to a bulkhead. An inflatable filler resting on the cables would support the roadway. Any deflection of this cable sling would not deflect the compression tubes since they are only in contact at the ends. On this basis then, it was found that for a 10 foot diameter tube, the inflation pressure of 14 psi and the fabric stress of 674 pounds per inch are required (Reference graph on Page C 64).

Again adjusting the fabric stress for dead load and adding a factor of safety of three, the fabric strength of 2235 pounds per inch is required. Although the fabric strength falls within the limits of fabrics that are available, the inflation pressure is rather high and problems were encountered in selecting an inflator device that would deliver the volume in the required time to get the system up to pressure. Also, since the compression tubes are not laterally supported and might possibly buckle, some question was raised concerning the structural integrity of the system. Realizing that the compression tubes are very vulnerable under enemy attack, it was then decided to scratch this concept from further investigation.

Concept No. 7 - Tubes with Support at Midspan

The idea in this concept was to form an inflatable beam by using two tubes to carry the bending moment with a flat inflatable mat on top to form a surface for the roadway. In order to keep the fabric stresses down into a reasonable range, a support tube at midspan is required to reduce the bending moment.

For a design comparison, the shipboard end of the ramp was designed as being simply supported in one instance and fixed in the other. The reduction in bending moment, however, is not very significant, as shown on Page C 67. By applying initial wrinkle theory, it was determined that for an optimum tube diameter of 10 feet, the inflation pressure of 23.7 psi and a fabric stress of 1423 pounds per inch are required (refer to graph on Page C 69). After adjusting the fabric stress for dead load and applying a factor of safety of three, the required fabric strength is 5058 pounds per inch. With reference to Figure 5, it should be noted that two straight plies of the Fiber B fabric would carry the load. However, the inflation pressure is very high, and selecting a system to deliver this pressure and volume in the required time proved infeasible. Some questions were also raised concerning the torsional stability of this concept if the load should get off center, along with the catastrophic results if one of the tubes is punctured. The operational method of deploying the support tube, along with the effect of waves on the support tube, was also of some concern. Therefore, because of the above mentioned considerations, this concept was also dropped from further investigation.

Concept No. 6 - Tube Tunnel

The idea in this concept is similar to the approach taken in Concept No. 4, except the dual-wall beams are replaced with tubes, and the sides are constructed of two ply bias fabric. The exact method of analysis for this concept is difficult to arrive at, since it is not known if the bias sides will transmit the full or a portion of the shear load. Therefore, two design approaches were taken. A conservative

approach would be to consider that each of the tubes will carry one fourth of the bending moment. On this basis, the inflation pressure of 57 psi is required and the fabric stress of 2736 pounds per inch is developed. A less conservative approach would be to assume that the side webs carry the full shear load and the four tubes act as one beam. On this basis, the inflation pressure of 9.5 psi is required with the fabric stress of 456 pounds per inch being developed. Refining each of the fabric stresses for dead load and then adding a factor of safety of three, the required fabric strength would fall somewhere in the range of 1668 to 10,008 pounds per inch, while the inflation pressure would be between 9.5 to 57 psi. Because of the uncertainty of the exact design approach, the mean value of the fabric strength and inflation pressure fall well above the normal ranges under consideration. Therefore, this concept was discontinued from further study.

Concept No. 9 - Truss and Inflated Bladder

The idea in this concept was to develop a hybrid structure which would use an air-supported bladder in conjunction with some type of aluminum truss work. The aluminum trusses would actually carry the bending moment, while the inflated bladder would simply stiffen and hold the trusses in the correct position. To do this, an inflation pressure of 5 psi is required which creates a fabric stress of 161 pounds per inch. Applying a factor of safety of three, the required fabric strength is 483 pounds per inch. These factors are well within the limits of fabric types and pressurization systems available. Typical truss systems and details that might be incorporated in this concept are shown on Pages C 79 to C 82. After reviewing this concept with Navy personnel, however, it was decided that this concept was basically the

same type of system that is presently being used, and that the inflatable portion did very little to actually carry the load. For this reason then, this concept was dropped from further investigation.

Concept No. 10 - Compression Deck and Inflated Bladder

Since high fabric stresses and inflation pressures are required to resist the compressive force due to bending moment, a system which could use a rigid aluminium-type deck to carry the compression load, and a cable system underneath to carry the tensile loads, will allow the main components of force to be carried by the structural members, rather than the fabric. The fabric bladder would serve as a means of tensioning out the cables and maintaining their shape.

A preliminary investigation of this concept revealed that an inflation pressure of 3.6 psi would be required and a fabric stress in the outer skin of 103 pounds per inch would be developed. Applying a factor of safety of three, the required fabric strength would be 324 pounds per inch.

Both the inflation pressure and fabric stress required fall within the normal range of materials available to meet these requirements. Upon evaluation, it was decided to continue with a more refined design analysis of this concept.

In summary then, after evaluating each of the ten preliminary conceptual configurations, it was decided to continue with a refined design analysis of the dual-wall beam with intermediate supports (Concept No. 2) and the compression deck with inflated bladder (Concept No. 10). It was also decided at this time in the study that the types of deck materials that were under consideration as being suitable for the roadway surface

would not meet the toughness and durability that are required for conditions imposed by the M103 Tank.

Navy personnel then directed us to evaluate each of the two remaining concepts to undergo refined design analysis on the basis that the roadway surface would consist of a material similar to that presently being used on the existing bow ramp. That is, the deck will consist of an aluminum grating approximately 3 1/2 inches deep, with rectangular openings approximately 3" x 6" on centers, with the individual bars 1/2" thick. Details of this grating are shown on Page D.23 in the refined design analysis.

It should also be noted that when evaluating each of the 10 concepts against the performance requirements outlined earlier, no mention was made concerning Grade "A" shock loads in the stowed condition and repairability by shipboard personnel. In each of the concepts the ramp was stowed in a manner which we felt would pose no problem in withstanding Grade "A" shock loads. Also, since all of the concepts were constructed of fabric, the repairability of the structure is well within the capabilities of shipboard personnel. The method of repair simply involves cleaning and patching of the affected area.

The effects of winds and waves had great importance only in Concept No. 3, since this concept had the most contact with the seawater. The remaining concepts, however, had little contact with the sea and therefore posed no serious problem concerning the effects of wind and waves. When speaking of vulnerability, it should be noted that any air-inflated fabric structure is vulnerable to some degree. The concepts which we felt are the most vulnerable and would lead to quick collapse were pointed out.

REFINED DESIGN ANALYSIS FOR CONCEPT NO. 2

Dual-Wall Beam with Intermediate Supports

The refined design calculations for this concept are shown in Appendix D, and a drawing conveying the final shape is shown in Figure 6.

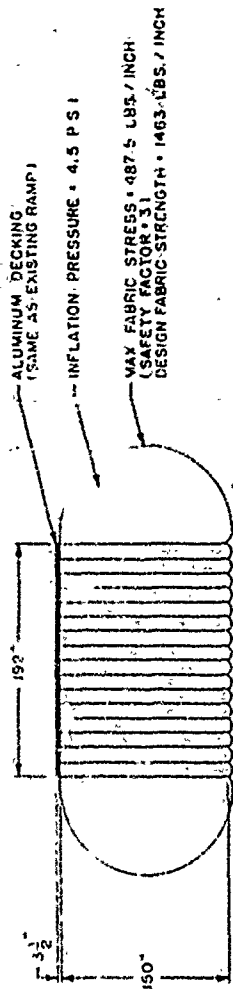
Reference will be made to these items.

With the refined design analysis, two new parameters entered into the design. First, since the roadway surface to be used must be similar to the existing bow ramp, this adds an additional dead load of approximately 11 tons to the structure. Secondly, with this increased load, consideration should be given to the effects of more than one intermediate support mechanism.

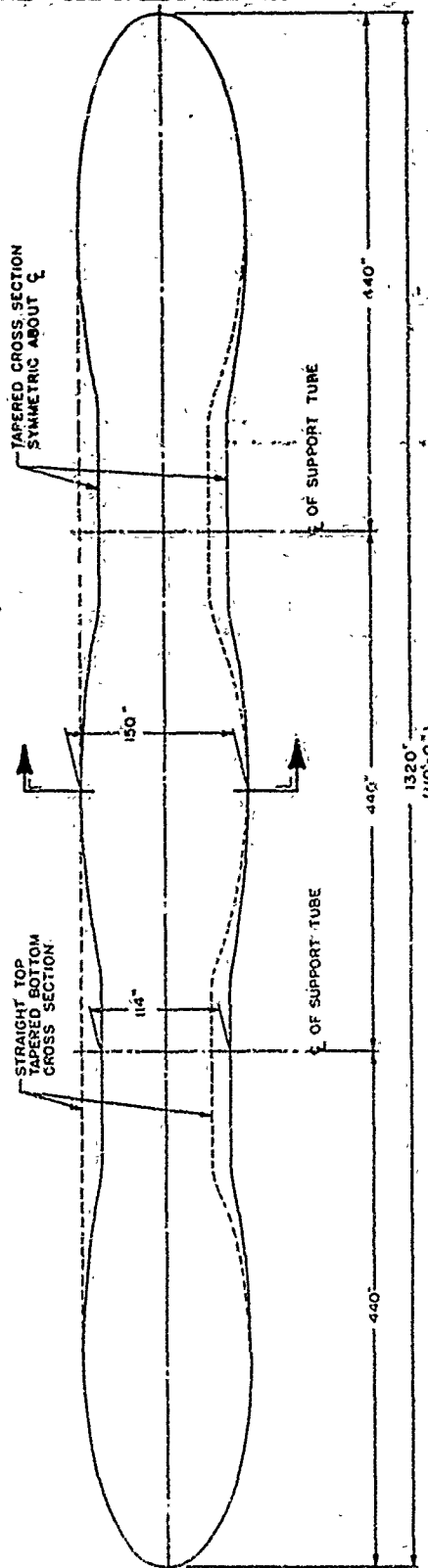
Therefore, applying a concentrated live load of 120,000 pounds and a dead load of 33.8 pounds per inch (Reference Page D-2), the maximum bending moments were computed for a two and three span continuous inflatable dual-wall beam. Computer printouts of the bending moment are shown on Pages D-6 thru D-9.

Applying the initial wrinkle theory as used in the preliminary design, the resulting fabric stresses and inflation pressures for varying depth sections are plotted on Page D-12. Again, an optimum depth of 150 in. seems to occur at the knee of the curve, and a three span continuous inflatable dual-wall beam requires the least inflation pressure and fabric stress to carry the load.

A graph on Page D-17 shows the relationship between bending moment, fabric stress, and inflation pressure for 0, 1, or 2 intermediate support tubes. By extrapolating the curves, it can be seen that the use of three support tubes will probably have little effect in reducing the bending moment,



CROSS-SECTION



SIDE ELEVATION VIEW

CONCEPT No 2
DUAL WALL BEAM WITH
TWO INTERMEDIATE SUPPORTS

FIGURE 6

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since the curve is flattening out. Therefore, for a three span continuous inflated dual-wall beam, the inflation pressure of 4.5 psi is required which creates a maximum longitudinal fabric stress of 487.5 pounds per inch in the outer skin. Applying a factor of safety of three, the required fabric strength in the outer skin is 1463 pounds per inch.

Up to this time, little has been said concerning how the inflatable dual-wall will transmit the shear loads as the load moves along the ramp. On Figure 6, the cross section view shows a series of 17 vertical webs. These webs, in addition to defining the shape of the structure, will carry the shear loads from the upper to lower skin along a 45° line. On Page D 20 and D 21, the calculations are shown for determining the shear load in the webs. After applying a factor of safety of three, the required fabric strength is 150 pounds per inch in the bias ply and 162 pounds per inch in the straight ply. One other important design consideration is the deflection of the dual-wall beam. With reference to Appendix 7 under deflection, it was concluded that an exact method for determining the deflection of an inflated dual-wall beam is very complex, if not impossible. The English, however, in their studies have arrived at an equation which in all cases seems to give very conservative results. Simply, the equation expresses deflection as a function of inflation pressure, cross sectional area, and the shear load at the point in question.

Upon applying this equation, reference Pages D 18 to D 19, it was found that a maximum 61 inch deflection would occur under a

120,000 pound point load. (It should be noted that if this equation were applied to the dual-wall beam with any number of interior supports, the deflection equation yields the same results. This is due to the fact that the inflation pressure, bending moment, and shear are a function of each other.) Since this 61 inch deflection is very conservative, in actual practice the deflection would probably be something less. However, an exact answer in this regard would involve actual field testing of a prototype.

The exact method of developing support tubes is of some concern also. Preliminary ideas were to actually float a cylindrical bag on the water's surface and, by varying the inflation pressure, regulate the height for accommodating the ramp to varying inclination angles. However, when investigating the idea further, it was found that such a large volume of water must be displaced to hold the load and that the diameter of the support bag became so large it was totally infeasible. Other methods of rigid vertical support mechanisms were considered, but with little success.

In conclusion then for Concept No. 2, the best way to evaluate its overall feasibility is to actually list the advantages and disadvantages:

Advantages

1. The inflation pressure is well within the limits of inflation devices available that will deliver the volume and maintain the pressure in the time requirement specified (10 minutes).
2. The fabric strengths required for the webs are well within the limits of easily workable fabrics available, while the fabric

strength required for the outer skin is within the limits of some of the newer fabrics.

3. The fact that each of the individual cells between the webs can be sealed off separately, and inflated with a manifold system, allows the ramp to withstand a puncture of a few cells and still remain intact.

Disadvantages

1. Size is the main problem. With reference to Figure 6, it can be seen that the structure is basically 150 inches deep for its entire length. This makes transition areas from the ship to ramp, and ramp to causeway difficult. A secondary type of inflatable would be required in these areas.
2. Operational methods also present problems (see Figure 4). Because of its width, clearance in winching the ramp back onto the deck between the derricks require that the side closures be deflated. Conversely, for deployment, the sides must be inflated after the ramp is extended.
3. Method of attachment to the ship is a problem because of its size. It does not fit into the existing area.
4. The negative buoyancy requirement when the extended end is lowered into 4 feet of water is a problem. The large volume of water that must be displaced makes it difficult to sink the extended end when not loaded.
5. The difficulty in finding a suitable support mechanism that is easy to deploy or retract, and still be versatile enough to accommodate the various heights required for varying ramp inclination, also exists.

6. Since the roadway must be similar to the present aluminum grating used on the existing bow ramp, it is difficult to handle or fold this structure into a compact unit.
7. Although not known for certain, it appears that the deflection under the tank loading will be significant and severely affect the maximum gradient the vehicles can encounter.

It is our opinion then, when weighing the advantages against the disadvantages, that this concept is infeasible with respect to its present application. Other similar applications might exist, however, where the span and load conditions are reduced, and the rigid deck requirement is removed. This would then allow the structure to be much more flexible and easier to handle, along with being able to store the unit in a more compact area.

REFINED DESIGN ANALYSIS FOR CONCEPT NO. 10

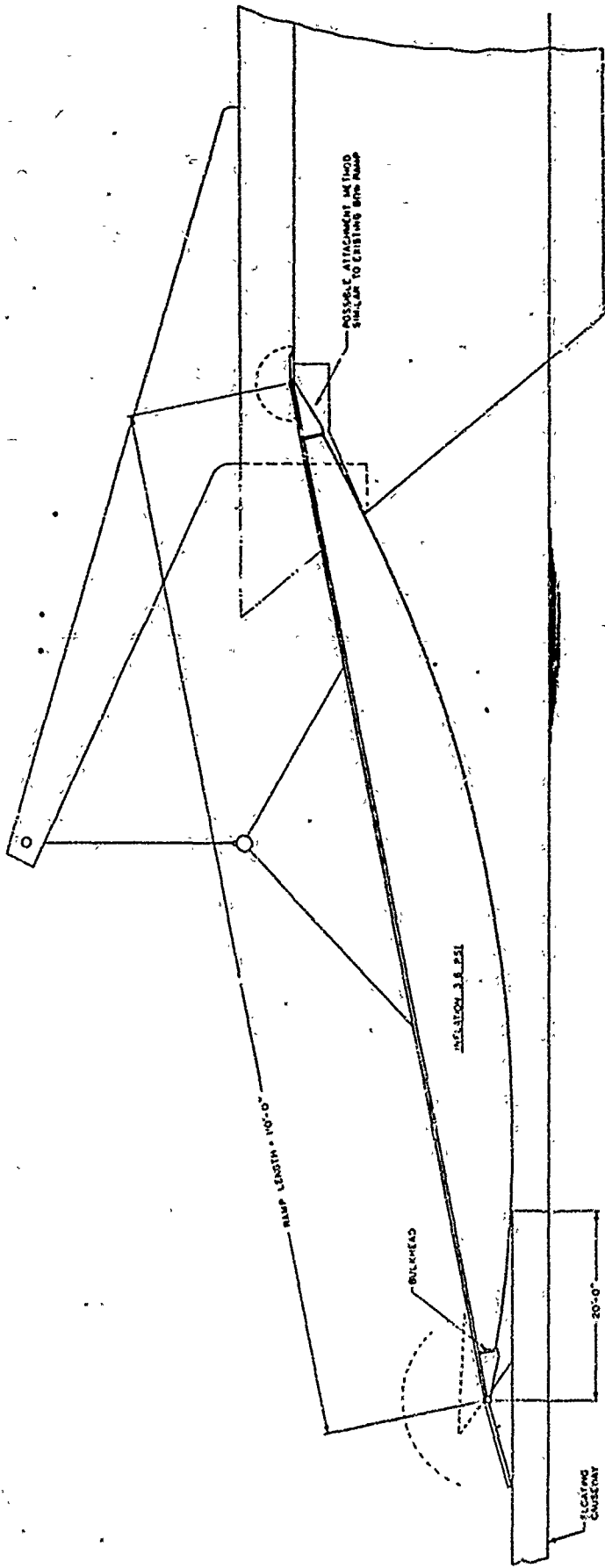
Compression Deck with Inflated Bladder

Since it is mandatory to use the type of deck that exists on the present bow ramp, we investigated the possibility of using this aluminum grating as the structural member to carry the compression force due to bending moment. In turn, as noted in the preliminary design, a series of cables forming a sling will carry the tension loads created by the bending moment and inflation pressure. The inflated bladder will tension out and hold the cables in position, while the fabric webs will transmit the shear loads along the ramp.

Figures 7, 8, 9, and 10 show general conceptual views and details, and will be referred to in later text. The method of operation proposed for this concept is similar to that being used for the existing ramp. The ramp will be attached to the ship with a kingpin connection which will allow for the rotational requirements, while the derrick and winch system will be used to deploy and retract the inflatable ramp. The ramp itself will be inflated and deflated on the main deck level. The design calculations start on Page D 23, and a brief summary of the design procedure and theory follows.

Investigating the structural properties of the existing deck, and assuming that the deck is fully supported in the longitudinal direction to the fabric bladder, and that the compressive force is distributed over the width (16 feet) of the grating, it was discovered that the deck is capable of supporting an allowable compressive load of 1,592,500 pounds. Further evaluation also indicated that under the tank loading, the deck is capable of distributing the track pressure equally across the width of the ramp. The effects of wheel loadings on the deck were also investigated, and the deck again was found satisfactory to distribute the wheel loads over an area equally equivalent to or better than the area of contact created by track loading. Upon this basis, it was concluded that an inflation pressure of 3.6 psi

26a

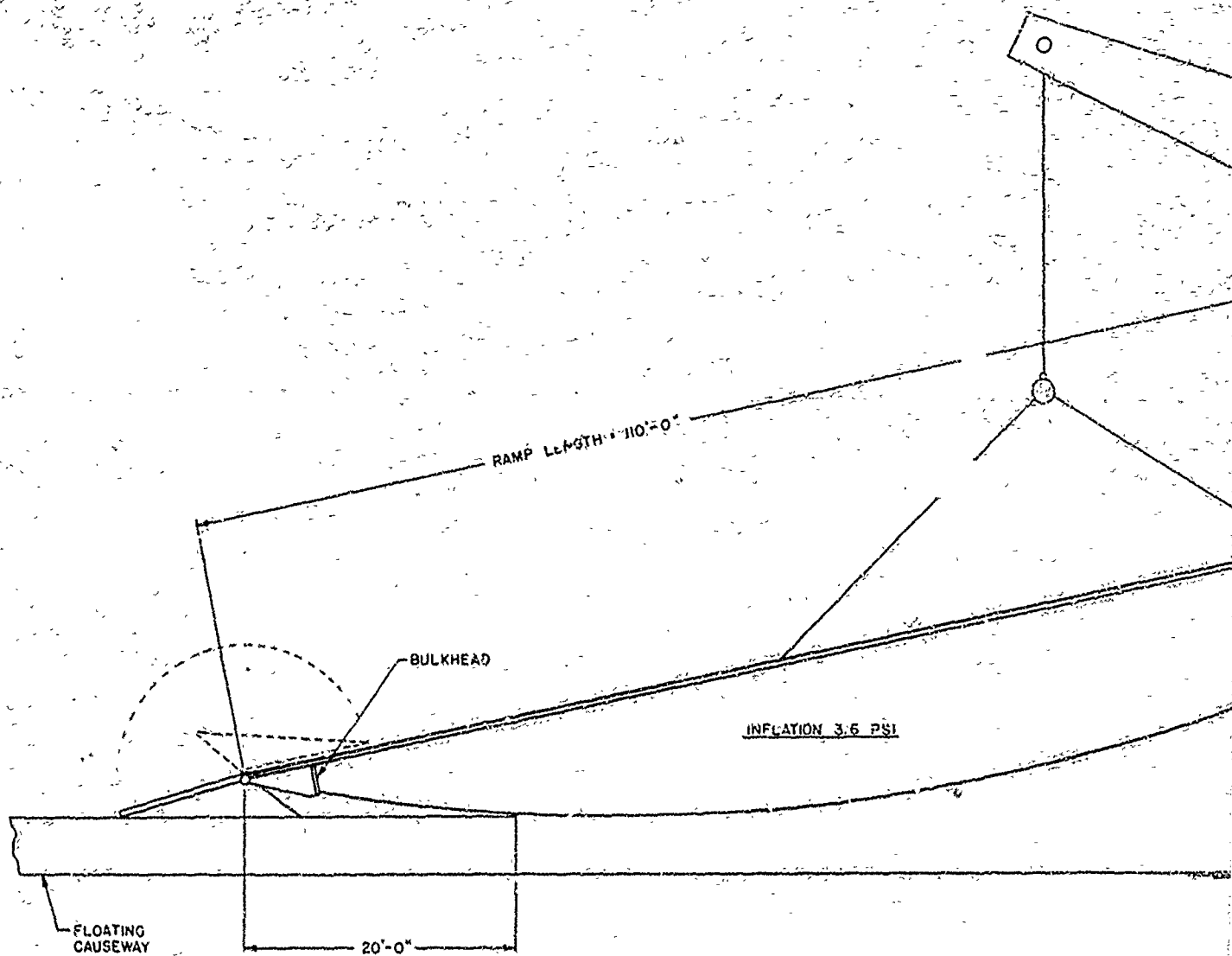


ELEVATION

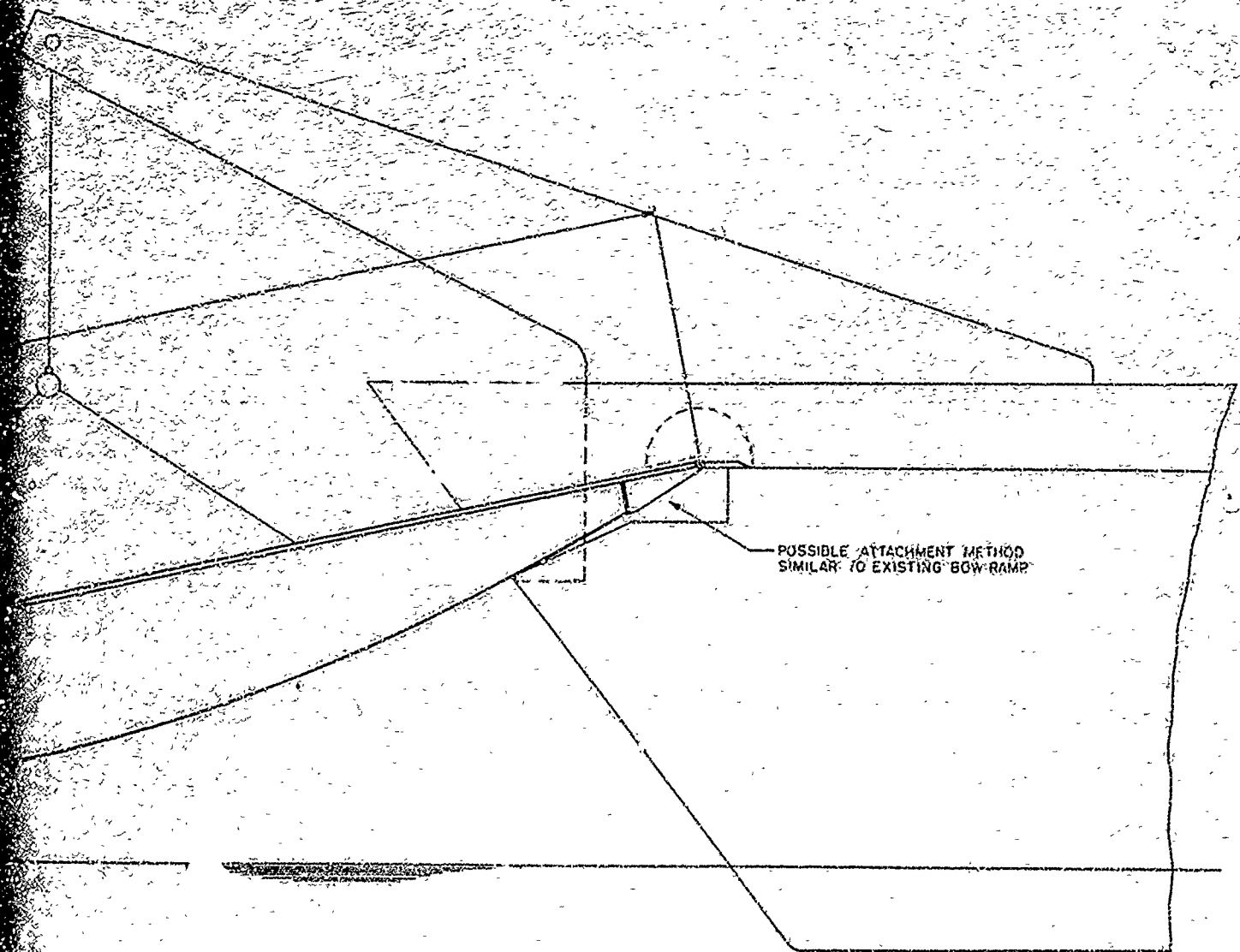
See the full set of drawings for details of this structure.

FIGURE 7





ELEVATION

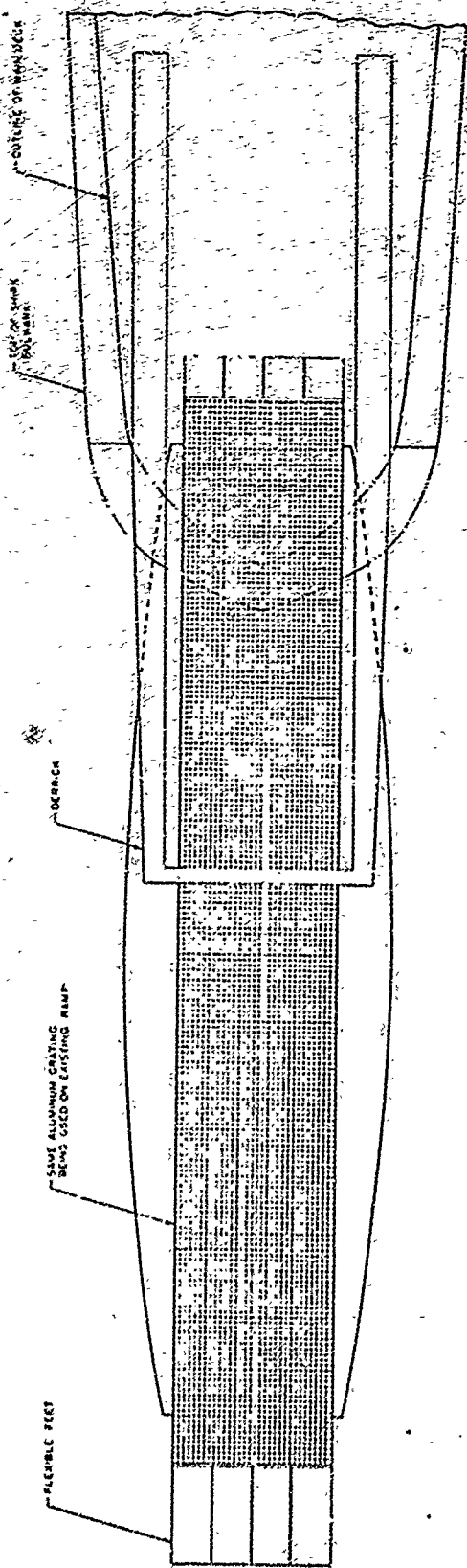


ELEVATION

FIGURE 7



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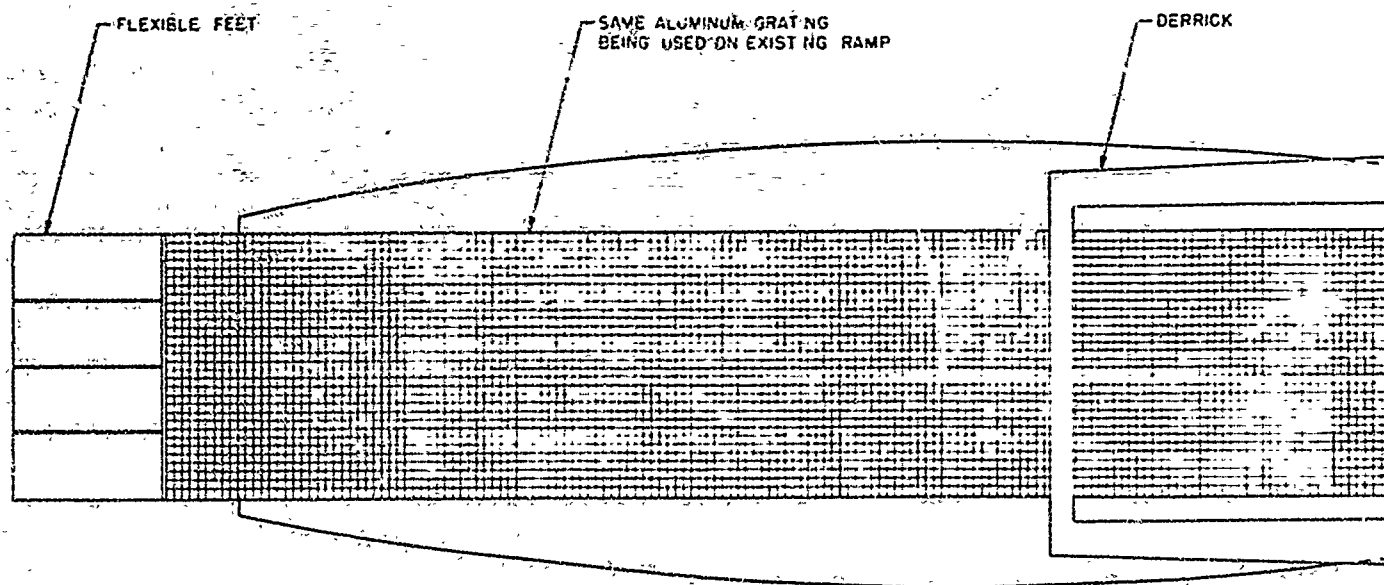


PLAN

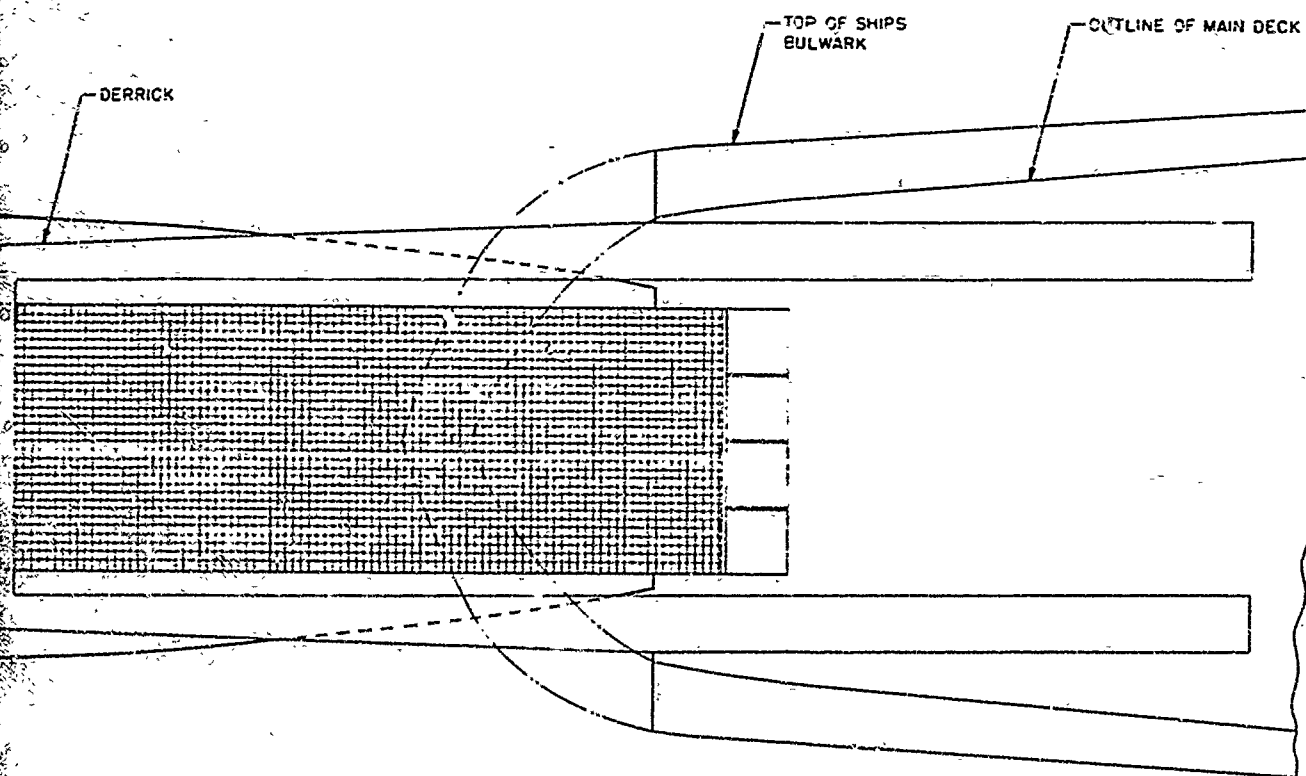
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NAVY DRAWING NO. 100-100
DATE 1-1-60

FIGURE 9





PLAN



PLAN

FIGURE 8



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126-0647-322.6 INCHES MAX AT MIDSPAN
118-151-277.5 INCHES MIN AT BULKHEAD

22
47.5

25.5 IN

110-107-130 INCHES MAX AT MIDSPAN
118-037-22.9 INCHES MIN AT BULKHEAD

FIBREX STRENGTH
TOTAL LB / INCH

WEB STRENGTH - 2 PLY BIAS
516 PLY 150 LB / INCH 253442
BIAS PLY 332 LB / INCH

17" LIP SINKING
14 CABLES REQUIRED

DETAIL B

INSULATION 1/8 IN

XXXXXXXXXXXXXXXXXXXX
See the following page
for the following detail
XXXXXXXXXXXXXXXXXXXX

FIGURE 9

TYPICAL CROSS SECTION AT MIDSPAN

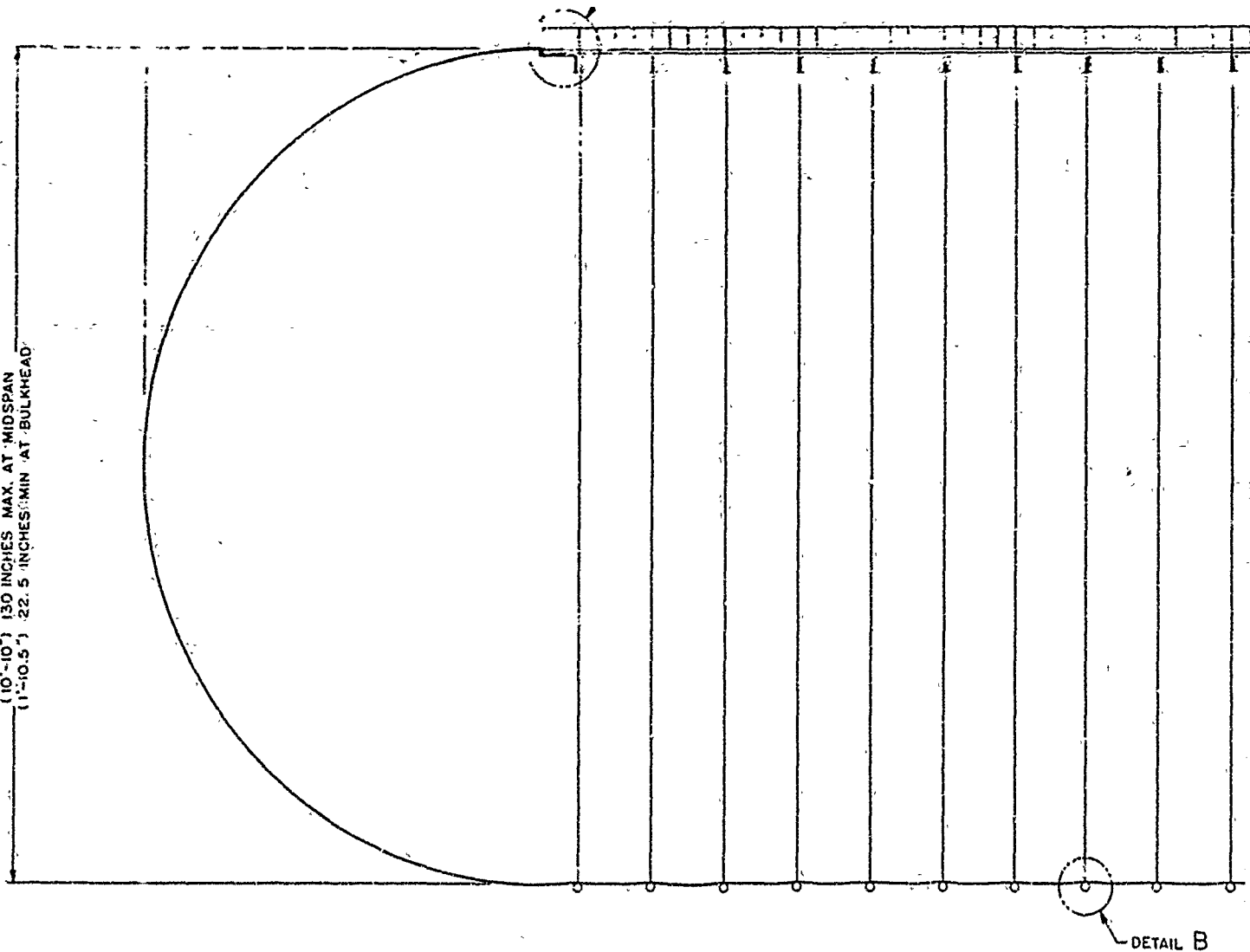


(10'-10") 130 INCHES MAX. AT MIDSPAN
(11'-10.5") 22.5 INCHES MIN AT BULKHEAD

(26'-10.6") 322.6 INCHES MAX. AT MIDSPAN
(18'-1.5") 217.5 INCHES MIN AT BULKHEAD

32
5-0

DETAIL A

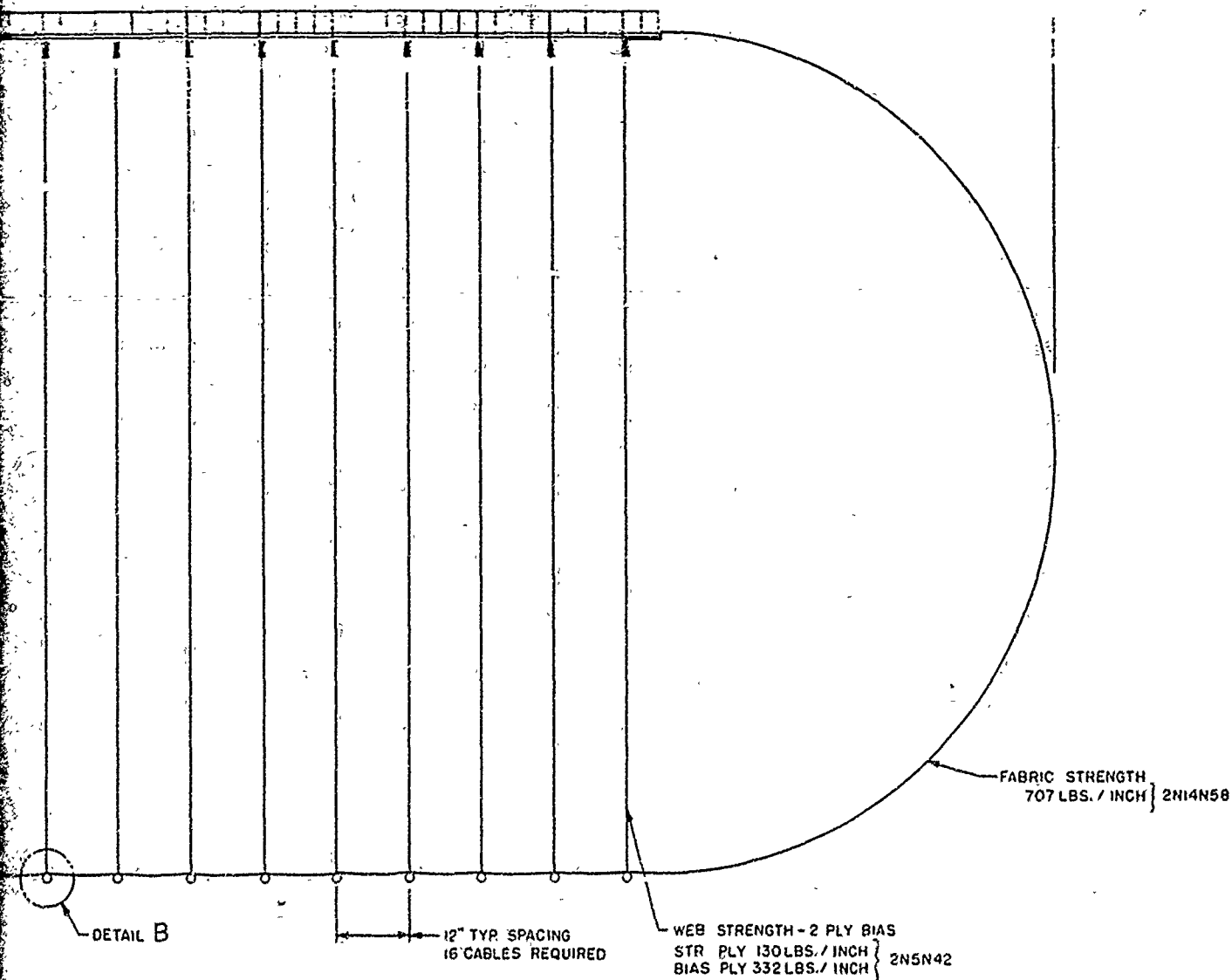


INFLATION 3.6 PSI

TYPICAL CROSS SECTION

26c

MAX. AT MIDSPAN
MIN. AT BULKHEAD



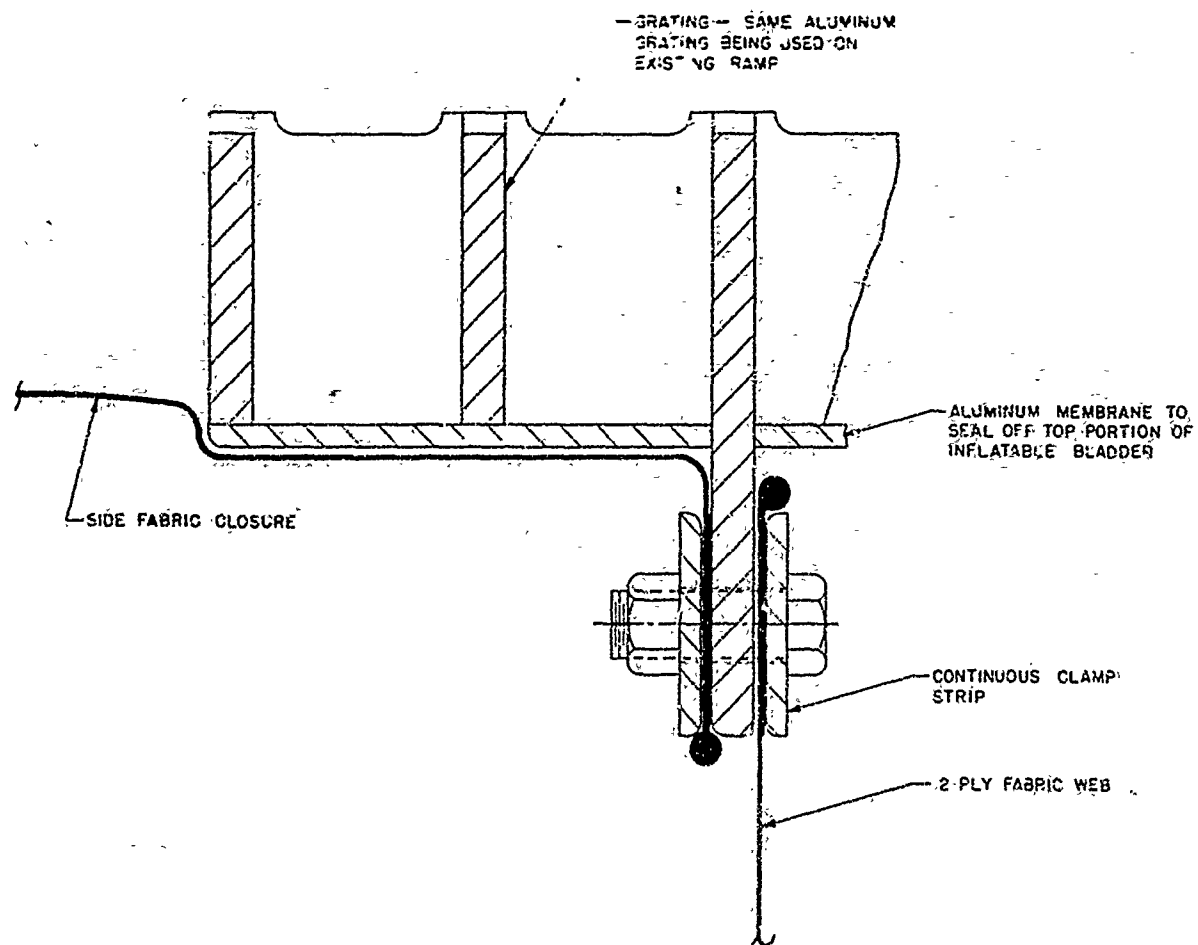
INFLATION 3.6 PSI

SECTION AT MIDSPAN

FIGURE 9



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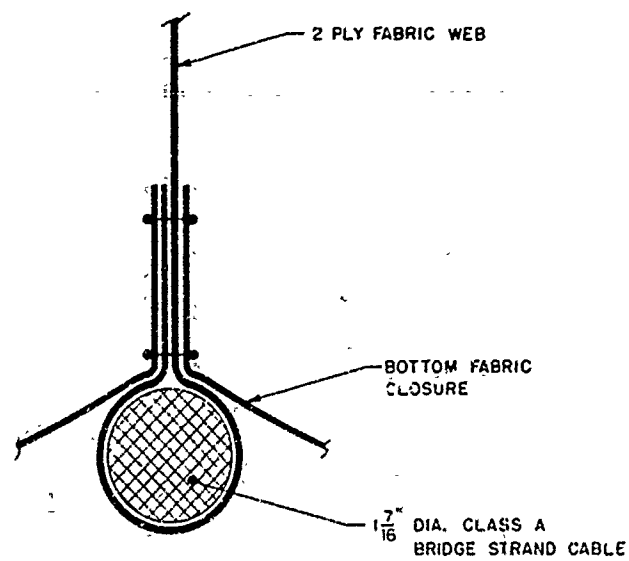


DETAIL A

MEMBRANE TO
PORTION OF
BLADDER

CLAMP

WEB



DETAIL B

FIGURE 10



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(required to support tank loading) would be required to resist local buckling or severe deflection under the tracks. It should be noted this design pressure is a little conservative, since the area of contact was considered to be the width of the deck by the length of the track. Actually, the deck will distribute the load in the longitudinal direction something greater than the track length, as well as across the ramp.

The actual theory of how the stresses are distributed in the structure is outlined on Pages D 27 and D 28. Basically, because of the parabolic shape of the cable band, the inflation pressure creates a tensile load along the cables, which in turn transmit a compressive load to the deck. The stresses due to bending moment then are simply determined by computing the moment at any point as the load moves along the ramp and dividing by the depth of the section at that point. The summation of these stresses due to inflation pressure and bending moment then dictate the maximum compressive and tensile loads in the structure. Knowing the allowable compressive stress that the deck is capable of supporting, along with the inflation pressure of 3.6 psi, it was found that a minimum depth of 124 inches at mid-span is required. For a slight cushion, the design depth at mid-span was considered to be 130 inches.

Based on this depth (130 inches), and a span of 110 feet, a computer print out on Page D 31 shows the total compressive and tensile loads on the structure as a 60 ton tank moves along. A brief summary of stresses is shown on Page D 32 and, with 16 cables spaced at 12-inch centers, 1 7/16 inch diameter, Class A, Bridge Strand Stainless Steel

Cables are required. These cables in turn are attached to a bulkhead at each end of the ramp which transfers the load into the deck (see Figures 7 thru 10).

The fabric stresses in the outer skin of the inflatable bladder are simply a function of inflation pressure, and the theory of hoop tension applies. That is, the fabric stress is a function of inflation pressure and radius of curvature. On this basis then (reference Page D 37), it was found that the maximum fabric stress in the side and bottom closures is 255.7 pounds per inch and, with a factor of safety of three, the required fabric strength is 707 pounds per inch.

The analysis of the shear distribution along the ramp is similar to that in the dual-wall beam. The webs transfer the shear force between the cables which are in tension, and the deck that is in compression. It is assumed that by using a two-ply bias web fabric, the stresses will be transferred along a 45° line. Using this concept, and assuming that the minimum depth of section that is required to transmit the full shear load is 52 inches deep (see Page D 38), it was found that the actual stress in the straight ply due to inflation pressure was 43.3 pounds per inch, and that the stress in the bias ply due to shear was 110.5 pounds per inch. Applying a factor of safety of three, the required strength in the straight ply is 130 pounds per inch and 332 pounds per inch in the bias ply.

Further discussion on fabric types most suitable to meet these requirements will be outlined later in this section.

Deflection under load is another important design considered, and again it is difficult to arrive at an exact theoretical solution (see Appendix F). Based on the assumption that the fabric portion of the ramp does very little to influence deflection, basic elastic beam theory was applied, and it was determined that approximately a 1 1/2 inch deflection could be expected under the 60 ton tank loading. Exactly how realistic these values are is difficult to assess at this time.

Because of areas of uncertainty in the design, specifically, the actual distribution of the shear forces and the deflection, a 1/10th scale model of the concept was constructed and tested. Design notes on scaling down the various parameters are shown in Appendix E.

An optimum load for the model will consist of a 1200-pound load distributed over an area 19 1/4 by 17 1/2 inches. The inflation pressure required to resist this load is 3.6 psi. These conditions then, would simulate the actual full size bow ramp under a 60-ton tank loading.

The test model, see photos 5 and 6, was constructed of two ply, lightweight fabric with sixteen 1/8 inch diameter coated cables, which were bonded to the webs (see detail B, Figure 10). These cables were in turn attached behind the bulkhead to the deck. The deck in the model was constructed of 6061-T6 aluminum, 1/16" thick, which again simulated the allowable compressive stress of the full scale deck. The deck in the model did not have the transverse rigidity that the bars create in the actual full size decking, however; therefore, a frame was constructed to distribute the load across the width of the ramp when under test.

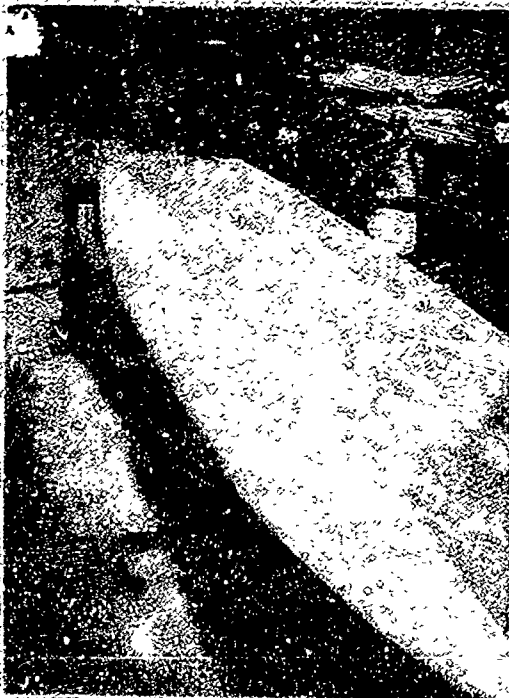


PHOTO 5

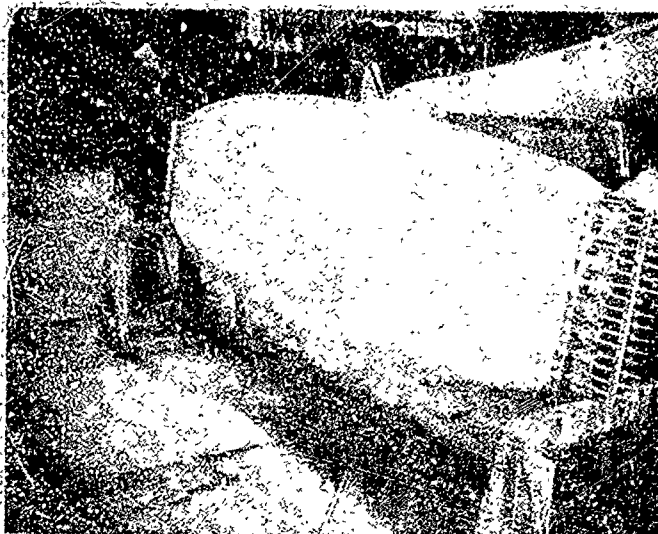


PHOTO 6

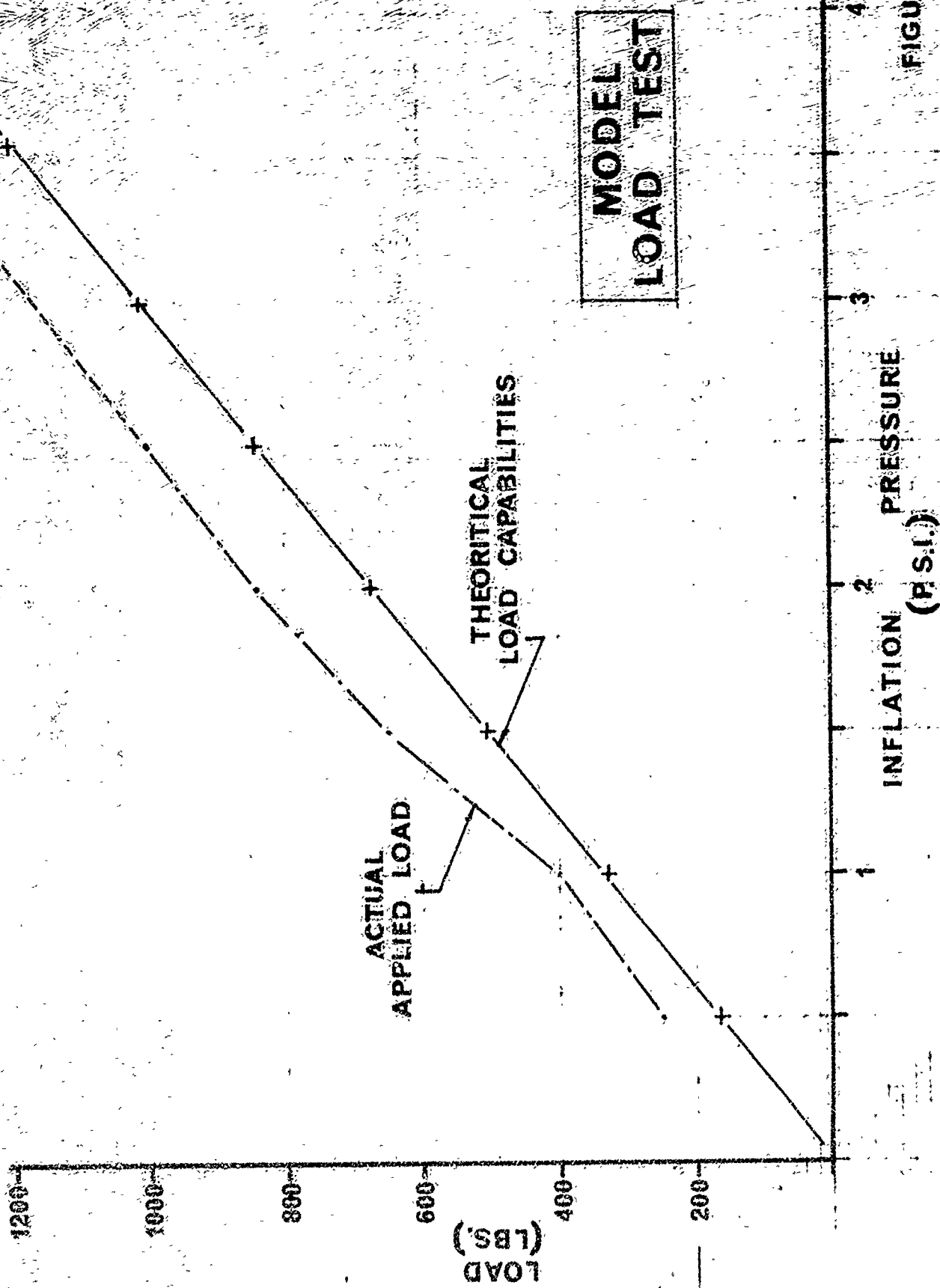


FIGURE 11

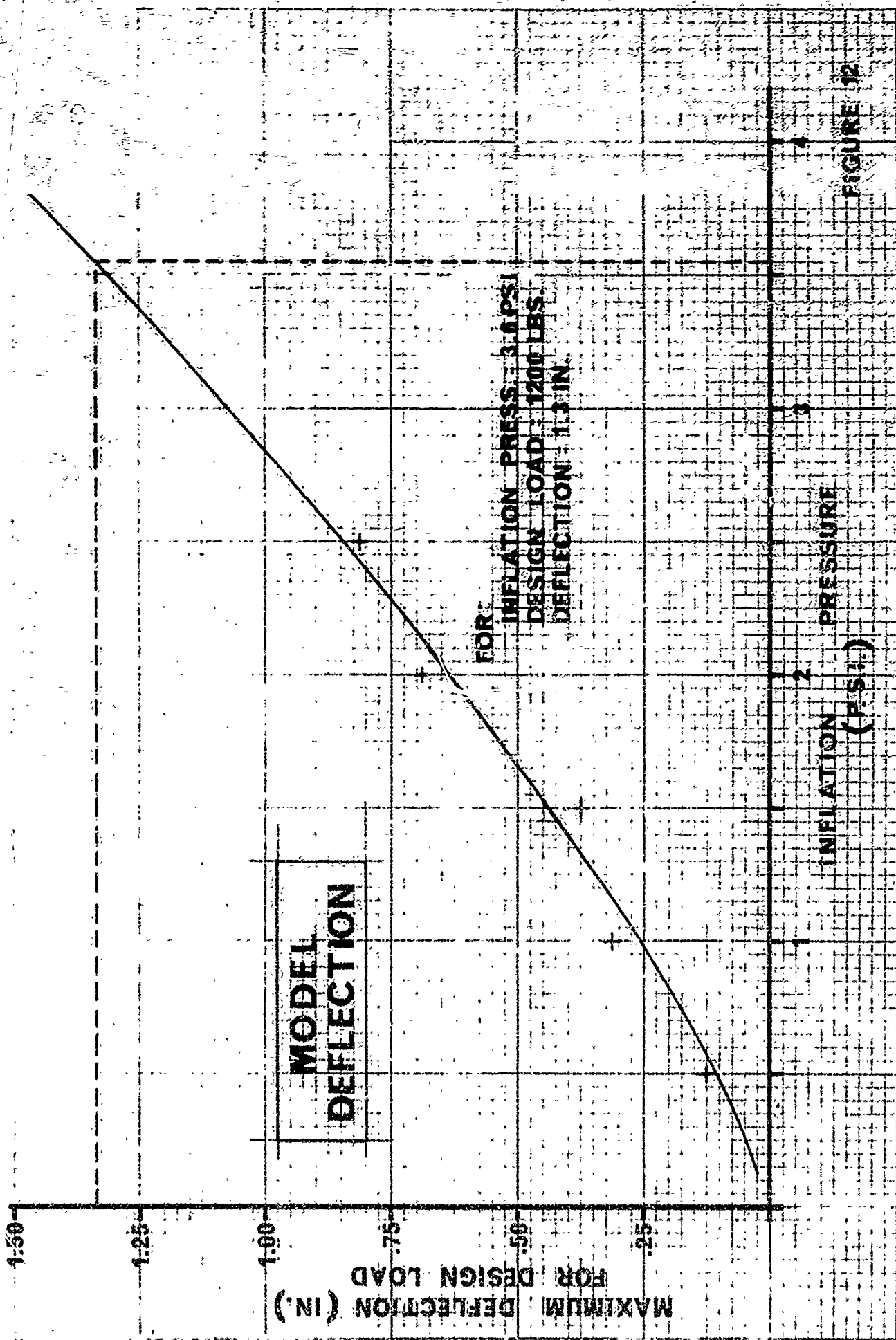


FIGURE 12

Upon running the test and loading the model under different loads for increasing pressures, the following results were obtained. See Figures 11 and 12. In all cases investigated for varying inflation pressures, the model was able to support a load in excess of the theoretical design load. Since the model was only tested up to 2.5 psi, a projected curve indicates that under 3.6 psi the model will easily support the 1200-pound load (see Figure 11).

Deflection of the model under various loads and inflation pressures was also recorded. Figure 12 shows the maximum deflection of the bottom side of the model with the maximum design load at midspan. Again projecting this curve indicates that under an inflation pressure of 3.6 psi and the load of 1200 pounds, an anticipated deflection would be 1.3 inches. It was also observed that when the ramp was overloaded, local failure or buckling of the deck in the immediate area of the load was created. When the load was removed, the deck sprang back to its original position with no apparent damage to the structure.

Relating the information gathered from the scale model back to the full size inflatable ramp, it was concluded that the theory used to analyze the structure, as far as load-carrying capacity was concerned, is conservative and correct. The maximum deflection to be anticipated on the inflatable bow ramp when under the 60-ton tank loading, however, is approximately 13 inches. This does not agree with the elastic beam theory used earlier which indicated a 1 1/2 inch deflection. The difference here might be explained by the fact that elastic beam theory excludes shear deflection from its equations. Extensive discussion on bending or elastic deflection versus shear deflection is noted in Appendix F. In any event, the value of 13 inches falls between the value obtained from elastic theory and the value obtained by the shear deflection equations.

Since Concept No. 10, from a design point of view, appears to be feasible, some further discussion on fabric types and pressurization systems that meet the requirements is necessary.

Fabric Selection

The selection of a coated fabric composite is dependent on many criteria. The most important of these are breaking strength, tear resistance, air-holding, sea water resistance, and maximum retention of properties over extended periods of use and/or storage. The selection of Concept 10 makes the choice of a composite a bit easier, eliminating the new and exotic fibers required to fulfill the unusually high strength requirements of the other preliminary conceptual designs.

The ultimate coated fabric chosen is identified by Birdair's designation: 2N5H42 for the webs, and 2N14N58 for the side and bottom closures. The first digit indicates that the composite is made of two plies of coated fabric, in this case one is placed at a 45° bias to the straight ply (in the case of a single ply material the first digit is not used). The second digit indicates the base fabric used (e.g., N = nylon). The next digit(s) is the weight of the uncoated fabric in oz./sq. yd. The next digit is the coating (e.g., N = Neoprene; H = Hypalon; V = Vinyl). The next digit(s) is the total coated weight of the composite (in oz./sq. yd.).

The type of fiber selected is determined by the properties of the fabricated end item. Natural fibers (cotton, wool) are not considered because of their very low strength and poor wet properties. There are many synthetics to choose from: polyamide (commonly known as nylon) and polyester (typically, Dacron, Trevira, Diolen) being the strongest.

Their availability in continuous filament also is in their favor. Fiberglass, especially the more flexible beta-glass fiber, is also a possible choice. Nylon was chosen primarily because of its ready availability in the weight range desired, cost, and satisfactory past performance. Tables 1, 2, 3, and 4 at the end of this section describe the properties and construction of this 5 oz./sq. yd. and 14 oz./sq. yd. nylon fabric.

The neoprene coating selected was chosen from those most commonly used in coated fabric composites used in inflatables, specifically urethane (poly-), vinyl (polyvinyl chloride), Hypalon (chlorosulfinated polyethylene) and neoprene. Urethane coatings with the correct balance of properties are used in life rafts, vests, and emergency slides. They exhibit excellent air-holding properties, but are typically used in very thin film (approximately 0.001 in. thick) type coatings on fine lightweight fabrics. Actually, thicker films as dictated by the end use requirements and use on a heavier base fabric would (1) be excessive in cost and (2) tend to degrade because of their thicker cross-section.

Vinyls provide a good balance of properties with their ease of fabrication and low cost being the major considerations. These are the main reasons this material is used in thousands of commercial air-supported structures (swimming pool enclosures, tennis court covers, warehouses, fieldhouses, etc.). However, vinyl does not lend itself to two-plying, mentioned earlier and described more fully later on in this section, and its abrasion resistance, though good, is second to the elastomers mentioned in the next two paragraphs.

Hypalon (chlorosulfonated polyethylene) offers the best combination of properties for this application. Detrimental factors are: (1) high cost of coated fabric due to difficult coating process, (2) difficulty in fabrication, and (3) stiffness of end product.

As stated previously, neoprenes (2N5N42 and 2N14N58) are the current choices. They lie somewhere between vinyl and Hypalon in all properties and yet offer outstanding performance through a wide temperature range. They allow two-plying and though seaming is not easy, by the same token it is not excessively difficult, producing breaking strengths equivalent across a seam at a minimum equal to the strength of the base fabric itself.

Two-plying has been mentioned several times. Essentially, this involves bonding of layers of fabric together. Sometimes, as in the case of two straight plies, this is done to increase the tensile strength of the composite twofold over a single ply of fabric. For this project, one layer is laid and bonded at an angle of 45° to another straight ply. While increasing the strength slightly, it offers the optimum of resistance to tear propagation in the event the unit is punctured. This is due to the bias ply stretching around the puncture and allowing the stresses to distribute themselves around the hole. Typically, tear resistance as tested by the trapezoidal tear test method are in excess of 300 lbs.

BIRDAIR STRUCTURES, INC PRODUCT SPECIFICATION RECORD

SPEC. NO.	REV
115	A

TYPE	PURCHASE SPECIFICATION						SHT 1 OF 1
SUBJECT							
5 oz./sq. yd. NYLON FABRIC							
BY	QC	ENG	MFG	OTHER	REV. DATE	REV. DATE	ISSUE DATE
JEB	DOL		ATB			5/29/60	9/22/64

BASE FABRIC

Style:	West Point Pepperell SH 520, or equivalent
Type:	Filament Nylon
Weight:	5 oz./sq. yd.
Thread Count:	22 x 22 1/2
Yarn Numbers:	840/1
Weave:	Plain
Grab tensile (nominal):	410 x 430
Gauge (approx.):	.013
Finish:	Scoured and heat set in tenter frame

TABLE 1

bts

BIRDAIR STRUCTURES, INC PRODUCT SPECIFICATION RECORD

SPEC. NO. 2N5H42	REV
---------------------	-----

TYPE PERFORMANCE SPECIFICATION						SHT! OF 1	
SUBJECT 2 PLY, 45° BIAS, NEOPRENE-COATED NYLON FABRIC							
BY JED	QC OOL	ENG HSP JG	MFG ATB	OTHER	REV. DATE	REV. DATE	ISSUE DATE 9/23/69

COATED FABRIC

The fabric shall be coated to provide a black, non-staining, cementable, soft and pliable coated fabric base, coated for high adhesion. The two ply, 45° bias material shall be overlapped as required to develop full strength of the base fabric across the bias seam. Distance between bias lap centers must be held uniform within ±2 inches. No accumulation is allowed.

PROPERTIES	REQUIREMENT	TEST METHOD
Coated weight, oz./sq. yd.	42 +3 -0	Birdair LP-60 Fed. Std. 191, Mtd 5041
Coating Distribution, oz./sq. yd. Gauge (approx.), in.	20-8-4 0.034	
Coating Adhesion, lbs./in.	10 Min.	Birdair LP-62 Fed. Std. 191, Mtd 5970
Ply Adhesion, lbs./in.	10 Min.	Birdair LP-63 Fed. Std. 191, Mtd 5950
Strip Tensile, Warp & Fill, lbs./in.	300 Min.	Birdair LP-51 Fed. Std. 191, Mtd 5102
Elongation, 24 hrs., % @ 30 lbs./in. load	W F 3.0 Max. 6.0 Max.	Birdair LP-59
Trapezoidal Tear, W & F, lbs.	200 Min.	Birdair LP-54 Fed. Std. 191, Mtd 5136
Dead Load, 1 in. wide, 1 1/2" lap joint 150 lbs. W & F at R.T., hrs. 75 lbs. W & F at 160° F., hrs.	4 Minimum 4 Minimum	Birdair LP-56 Birdair LP-57
H ₂ O absorption, %	6 Max.	Birdair LP-66

OTHER REQUIREMENTS

Surface to be essentially dust free to facilitate cementability. If dust is used, it is to be a 25/75 mixture of talc and zinc stearate.

Staining is evaluated by painting with 0.003 in. of white Radalon paint. Painted surface is exposed for 48 hrs., 6 inches from No. RS-276W G.E. sunlamp. Color should not be darker than Fed. Std. No. 595, Color No. 37778.

This material is to be uniformly coated with flat and smooth surfaces, free from stains, bare spots, or other defects that would impair physical strength or weatherability.

bts

TABLE 2

BIRDAIR STRUCTURES, INC

PRODUCT SPECIFICATION RECORD

SPEC. NO.	REV
N14	

TYPE		PURCHASE SPECIFICATION					SHT 1 OF 1	
SUBJECT								
14 oz./sq. yd. NYLON FABRIC								
BY	QC	ENG	MFG	OTHER	REV. DATE	REV. DATE	ISSUE DATE	
JED	DOL		ATB				10/1/71	

BASE FABRIC

Style: J. P. Stevens Style 38601, or equivalent

Type: Filament Nylon

Weight: 14 oz./sq. yd.

Thread Count: 43 x 42

Yarn Numbers: 840/1

Weave: Plain

Strip Tensile (nominal): 625 x 525

Gauge (approx.): 0.024

Finish: Scoured and heat set in tenter frame.

TABLE 3

BIRDAIR STRUCTURES, INC. PRODUCT SPECIFICATION RECORD

SPEC. NO. 2014N50	REV. 1
----------------------	-----------

TYPE PERFORMANCE SPECIFICATION						SHEET 1 OF 1	
SUBJECT 2 PLY, NEOPRENE-COATED NYLON, 1 PLY, 45° BIAS							
BY JEB	QC	ENG	MFG	OTHER	REV. DATE	REV. DATE	ISSUE DATE 10/1/71

2014N50 is a composite material manufactured from two plies (1 ply 45° bias) of 24 oz./sq. yd. (approx.) woven nylon fabric coated with a black, non-staining, cementable, soft and pliable neoprene compound to a total weight of 58 oz./sq. yd. The neoprene coating is manufactured to provide good joint strength, flexibility, low R.F. loss, maximum retention of physical properties and good weatherability. The two ply, 45° bias material is overlapped as required to develop full strength of the base fabric across the bias seam. The Tedlar PVF film is used to prolong the useful life of the neoprene-coated fabric and to promote water runoff during rainfall.

PROPERTIES	REQUIREMENT	TEST METHOD
Gauge (approx.), in.	0.055	----
Strip Tensile, lbs./in., Warp & Fill	800 min.	Birdair LP-51, 51A
Coating Adhesion, Dry & Wet, lbs./in.	15	Birdair LP-62 F.T.M.S. 191 Mtd. 5970
Ply Adhesion, lbs./in.	15 min.	Birdair LP-63 F.T.M.S. 191 Mtd. 5950
Elongation, 24 hrs., % (@ 50 lbs./in. load)	W F 5 max. 8 max.	Birdair LP-59
Trapezoidal Tear, W & F, lbs.	250 min.	Birdair LP-54 F.T.M.S. 191 Mtd. 5136
Water Absorption, %	1.5 max.	Birdair LP-66
Dead Load, 1 in. wide, 2 3/4 in. lap joint 400 lbs. W & F at R.T., hrs. 200 lbs. W & F at 160° F., hrs.	4 minimum 4 minimum	Birdair LP-56 Birdair LP-57
Cold Flexibility (180° over 1/8" diameter rod at -40° F.)	No cracks evident under 5X magnification	Birdair LP-68

TABLE 4

bts

Inflation System

The inflation system for the ramp of Concept 10 will require a blower capable of producing a relatively large volume of air at the necessary pressure. Several fans can be immediately discarded as not suited. The propeller and axial type fans are incapable of the required pressures. Centrifugal fans of the **ventilation** type are also incapable of the pressure required.

The positive displacement class of air handling machines in general do not produce suitable volumes.

A blower suited to the inflation requirements is a centrifugal, multi-stage blower employing backward curved, forward curved wheels, or combinations of these wheels. The blower can be assembled with the proper selection of wheels to match the performance requirements quite closely.

The characteristics of performance with respect to overload tendencies, stability, etc. are determined by the necessary wheel combination. For purposes of this investigation, a Hoffman blower, Model 38404, has been selected. This unit requires 60 HP input at 3000 cfm.

As pointed out, the actual characteristics of the machine are dictated by the combination of forward and backward curved wheels required. The use of all backward curved wheels will result in self-limiting load characteristics. All forward curved wheels will not be load limiting. In each case the stability characteristics of pressure delivery at the low flow level must be determined after the unit is assembled.

Control of the inflation system is relatively simple, consisting of a motor starting device, pressure indicator, and any necessary duct restrictors, as determined by the blower characteristics. The blower will operate continuously for the time the ramp is in use.

It should be noted that the volume requirement can change rapidly as in the case of projectile puncture, and that greater volume from the main inflation system would be required to maintain operable pressures.

Therefore, an equivalent secondary blower would be desirable for emergency standby service. The ship air system is not suitable as an inflation source because of the very limited volume available.

The manifold ducting for inflation purposes can also be used for deflation of the ramp. It is assumed at this time that a manual exchange of ducts would be made to interchange the intake and discharge connections to the inflatable.

Blower Size

The flow capacity necessary to satisfy the 10 minute requirement can be determined, assuming 65% of the inflation period will be used to fill the cell with air and the remaining 35% of the time is allowed for pressurizing the unit.

$$\frac{V}{T} = \text{CFM}$$

$$\text{CFM} = \frac{17954}{10 (.65)}$$

$$\text{CFM} = 2762$$

Because of the possibility of overload characteristics, a restricting orifice will be assumed in the duct system. The diameter of the orifice is determined for the free flow condition, or when the entire blower

pressure output is across the orifice. This condition exists during the filling period.

$$D_o = \sqrt{\frac{Q}{(5.976) (K) \sqrt{h/\rho}}}$$

$$= \sqrt{\frac{2762}{(5.976) (.6) \sqrt{3.6 / (.03613) (.075)}}}$$

$$= 4.59, \text{ use } 4.625''$$

D_o = Orifice diameter

Q = Flow CFM

K = .6

h = pressure " H_2O

ρ = density of air

A blower capable of 3.6 psig and 2800 cfm is shown on the following sheets (Figures 13 and 14).

The time required for inflation can be estimated using successive increments of pressure from 0 psig to full inflation of 3.6 psig.

The example of calculating the required time for inflation is shown in Appendix G.

The time necessary to inflate the cell from flat to a fully pressurized condition can be estimated by obtaining the time required by the blower to supply the air necessary to fill and then pressurize the cell over a finite pressure increase. This time was found to be 9.2 min.

The total weight of air required to fill and pressurize the ramp is:

$$W = \frac{PV}{RT}$$

W = weight of air in pounds

P = absolute pressure psf

V = Volume of the inflatable

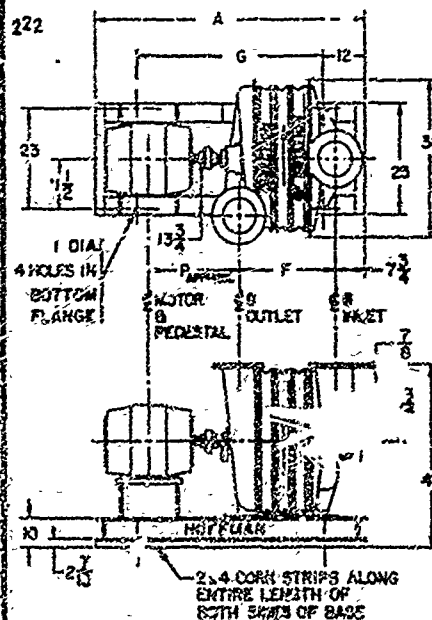
R = gas constant - air = 53.3

T = temperature °R

GENERAL DIMENSIONS IN INCHES

UNITS
38401-38407
38401A-38407A

UNIT SIZE	MOTOR FRAME	BASE	PEDESTAL	A	F	G	P
38401	215T	384076	384082	60	11 3/8	48	17 1/2
	215T	384076	384082	60	11 3/8	38	18 1/8
	254T	384078	384083	60	11 3/8	38	20 1/8
	258T	384078	384083	60	11 3/8	38	21 1/8
38402	215T	384076	384082	60	16 1/16	38	15 1/4
	254T	384078	384083	60	16 1/16	38	20 1/4
	258T	384078	384083	60	16 1/16	38	21 1/8
	264TS	384078	384084	60	16 1/16	38	20 5/8
	286TS	384078	384084	60	16 1/16	38	21 3/8
	324TS	384078	384085	64	16 1/16	38	22 1/8
38403	254T	384077	384083	72	20 3/8	25	20 1/4
	254T	384077	384083	72	20 3/8	48	21 1/8
	254TS	384077	384084	72	20 3/8	48	20 5/8
	258TS	384077	384084	72	20 3/8	48	21 3/8
	324TS	384077	384085	72	20 3/8	48	22 1/8
	328TS	384077	384085	72	20 3/8	48	22 7/8
38404	254T	384077	384083	72	24 11/16	48	21 1/8
	254T	384077	384083	72	24 11/16	48	20 5/8
	254TS	384077	384084	72	24 11/16	48	21 3/8
	324TS	384077	384085	72	24 11/16	48	22 1/8
	328TS	384077	384085	72	24 11/16	48	22 7/8
	384TS	384077	384086	72	24 11/16	48	23 1/8
38405	384TS	384078	384086	84	24 11/16	60	23 5/8
	404TS	384078	384087	84	24 11/16	60	24 7/8
	254TS	384077	384084	72	29	48	20 5/8
	286TS	384078	384084	72	29	48	21 5/8
	324TS	384078	384085	84	29	60	22 1/8
	328TS	384078	384085	84	29	60	22 7/8
38406	384TS	384078	384086	84	29	60	23 1/8
	385TS	384078	384086	84	29	60	23 5/8
	404TS	384078	384087	84	29	60	24 7/8
	405TS	384078	384087	84	29	60	25 5/8
	444TS	384079	384088	96	33 5/16	72	27 3/8
	445TS	384079	384088	96	33 5/16	72	28 3/8
38407	254TS	384077	384084	84	37 5/8	60	21 3/8
	124TS	384076	384085	84	37 5/8	60	22 1/8
	324TS	384078	384085	84	37 5/8	60	22 7/8
	384TS	384079	384086	96	37 5/8	72	23 1/8
	385TS	384079	384086	96	37 5/8	72	23 5/8
	404TS	384079	384087	96	37 5/8	72	24 7/8
	405TS	384079	384087	96	37 5/8	72	25 5/8
	444TS	384079	384088	96	37 5/8	72	27 3/8
	445TS	384079	384088	96	37 5/8	72	28 3/8



NOTES:

1. UNIT SHAFT SIZE 1 7/8 DIA. 3/4 X 3/16 KEY.
2. UNIT CONNECTIONS (INLET & OUTLET) 8 I.D., 18 1/2 O.D., 3/4 - 10 TAP 5 HOLES ON 11 - 3/4 S.C. STRADDLING 3'S.
3. P DIMENSION BASED ON COUPLING WITH 1/8 GAP.
4. PEDESTAL IS WELDED TO BASE.
5. FOR MOTOR FRAME SIZES NOT LISTED CONSULT HOFFMAN OFFICE.

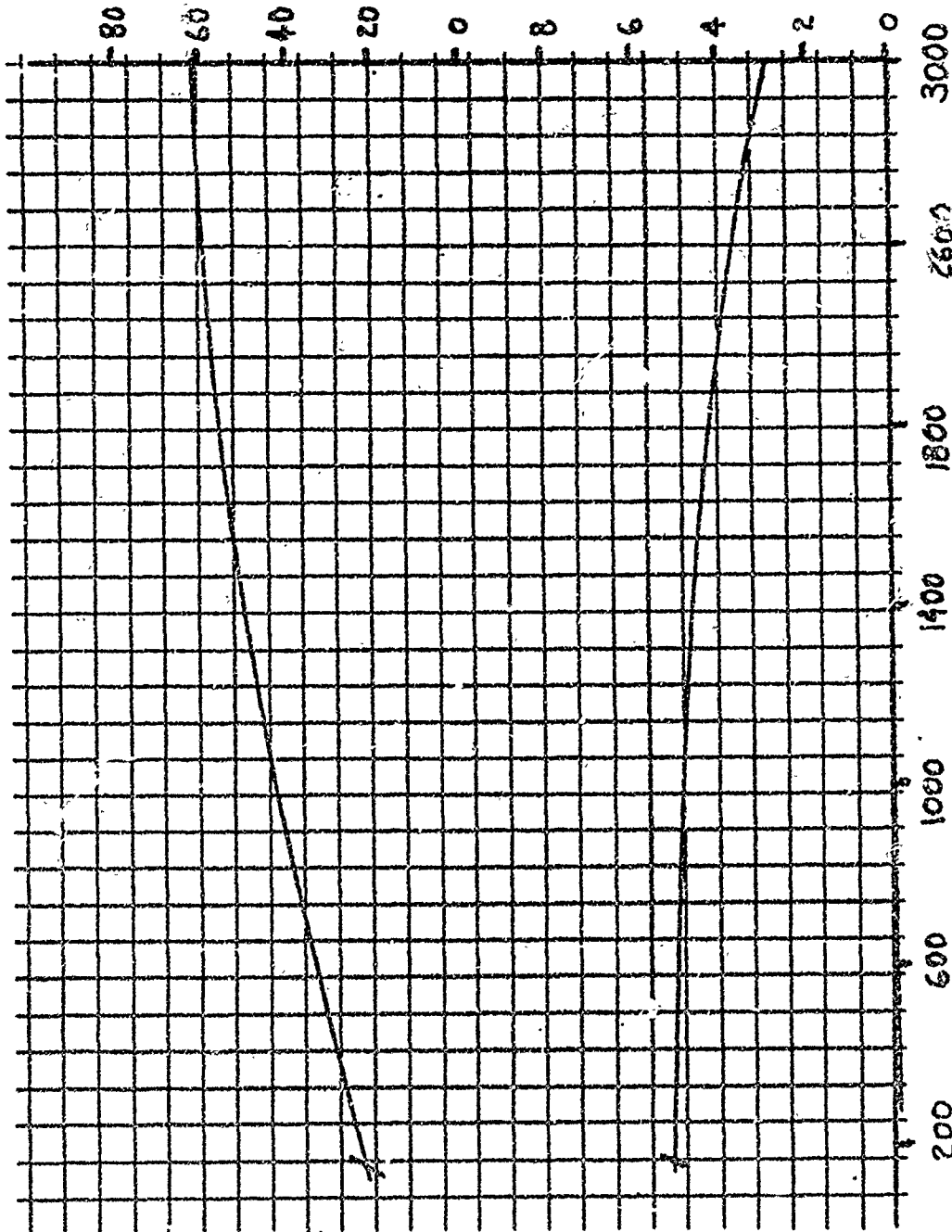
FIGURE 13

 HOFFMAN AIR & FILTRATION Div.
 CLARKSON INDUSTRIES, INC., NEW YORK, NY

BY J. J. H. DATE 1-25-68 DRAWN BY AX-1338

HORSEPOWER - INPUT TO BLOWER

PRESSURE (PSIG)



INLET AIR VOLUME

PERFORMANCE CURVES
CENTRIFUGAL BLOWER 38404A
FRAME 384A
SPEED 3550 RPM
ATMOSPHERE 14.7% 68°F

FIGURE 14

CONCLUDING REMARKS

To analyze the overall feasibility of Concept No. 10, the advantages and disadvantages of the concept are listed below with specific reference to the design parameters.

Advantages

1. Fabric strengths required can be handled with fabric types that are presently available and within the proper limits of workability and handling.
2. Pressurization requirements are well within the range of systems available to meet these requirements.
3. The cellular construction created by the webs enables the system to be compartmentized. That is, if damage occurs in one area, only that cell will be affected, and the remaining ones will remain inflated.
4. The deck material, while performing a structural function in the system, will also satisfy the rigid requirements for the effects of traction under track and wheel loading.
5. The maximum deflection under a 60-ton tank loading falls within allowable limits and will not increase the gradient significantly.
6. When the inflatable ramp is stowed on the main deck, it will occupy an area approximately 110 ft. long, 18 ft. wide, and 2 ft. high. It can be easily anchored for the effects of green seas.
7. The size of the inflation blowers required are rather small (84" L x 38" W x 47" H) and can be stowed in a compact location.
8. The system does not require intermediate support mechanisms, enabling the inflatable ramp to assume various angles of inclination.

9. Vehicle clearance at transition areas on each end of the ramp appears to be satisfactory.
10. The total weight of the inflatable ramp is 20.7 short tons, compared to 36.6 short tons in the existing ramp, which is effecting 43% weight reduction in ramp structure.

Disadvantages

1. The method of operation required to deploy and retract the inflatable bow ramp is basically the same as the method used on the existing bow ramp. The main cells of the ramp must, however, be inflated and deflated when resting on the deck level of the ship. Handling prior to this operation will severely damage the structure because of its lack of stiffness. The side closure panels must be inflated and deflated when in the extended position because of clearance problems when retracting the ramp between the derricks of the ship (see Figure 4). These requirements, however, pose no serious problems, other than a nuisance in the cycle of operation.
2. The sliding of the inflatable ramp along the ship's deck when being deployed or retracted could cause severe abrasion to the fabric belly. Possibly a sliding mechanism could be placed under the belly of the ramp when being winched along the ship's main deck.
3. The method of attaching the inflatable ramp to the ship would be similar to the method presently used. This idea is relatively simple and allows the ramp to accommodate the various rotational angles that are required.

4. The one design parameter that requires negative buoyancy of the extended end in 4 ft. of water with 5 ft. breaking waves and 30-knot winds acting on the structure is difficult to attain (negative buoyancy not required when using the causeway). Since the structure wants to float, it is necessary to actually anchor the end down when there is no load on the ramp. As the vehicles approach the extended end, they will in turn sink the ramp to the bottom.

It is our opinion then, after reviewing the advantages and disadvantages of Concept No. 10, that from a design point of view, the idea of creating an inflatable ramp which will span 110 feet and carry a 60-ton load is feasible. The method of attaching the inflatable ramp to the ship and operating the ramp does present some problems, however.

In complying with the contractual requirements, a preliminary cost and time schedule was developed for Concept No. 10. See Tables 5 and 6 on the following pages.

CUSTOMER U.S. NAVYDATE 4/17/73 EST. BY ARDESCRIPTION INFLATABLE ROW RAMP - DESIGN, DEVELOP AND MANUFACTURE (1) PROTOTYPE

RFQ. OR DWG. NO.

DIRECT ENG.	DATE	MH	COST	RATE	MH	COST	RATE	MH	COST
PRINCIPAL ENG.									
PROJECT ENG.	7.45	1700	12,665						
DRAFTING	5.05	1700	8,585						
QUAL. ASSURANCE	5.25	120	630						
SUB-TOTAL									
O.H. @ %									
DIRECT MFG.									
ENG. TECH.	4.55	100	455						
SHOP	3.90	6000	23,400						
LAB	4.15	200	830						
SUB-TOTAL			46,565						
O.H. @ 200 %			93,130						
MATERIALS & PURCH. PARTS			80,000						
OTHER DIRECT CHARGES									
COMM.									
IN-FRT .7% Material			560						
O.T. PREMIUM 1/2% D.L.			1,863						
RENTALS									
PER DIEM									
TRAVEL									
TOTAL COSTS			222,118						
Fee - 10%			22,212						
TOTAL PRICE			\$244,330						

TABLE 5

PRELIMINARY SCHEDULE
DESIGN & DEVELOPMENT OF PROTOTYPE BOW RAMP

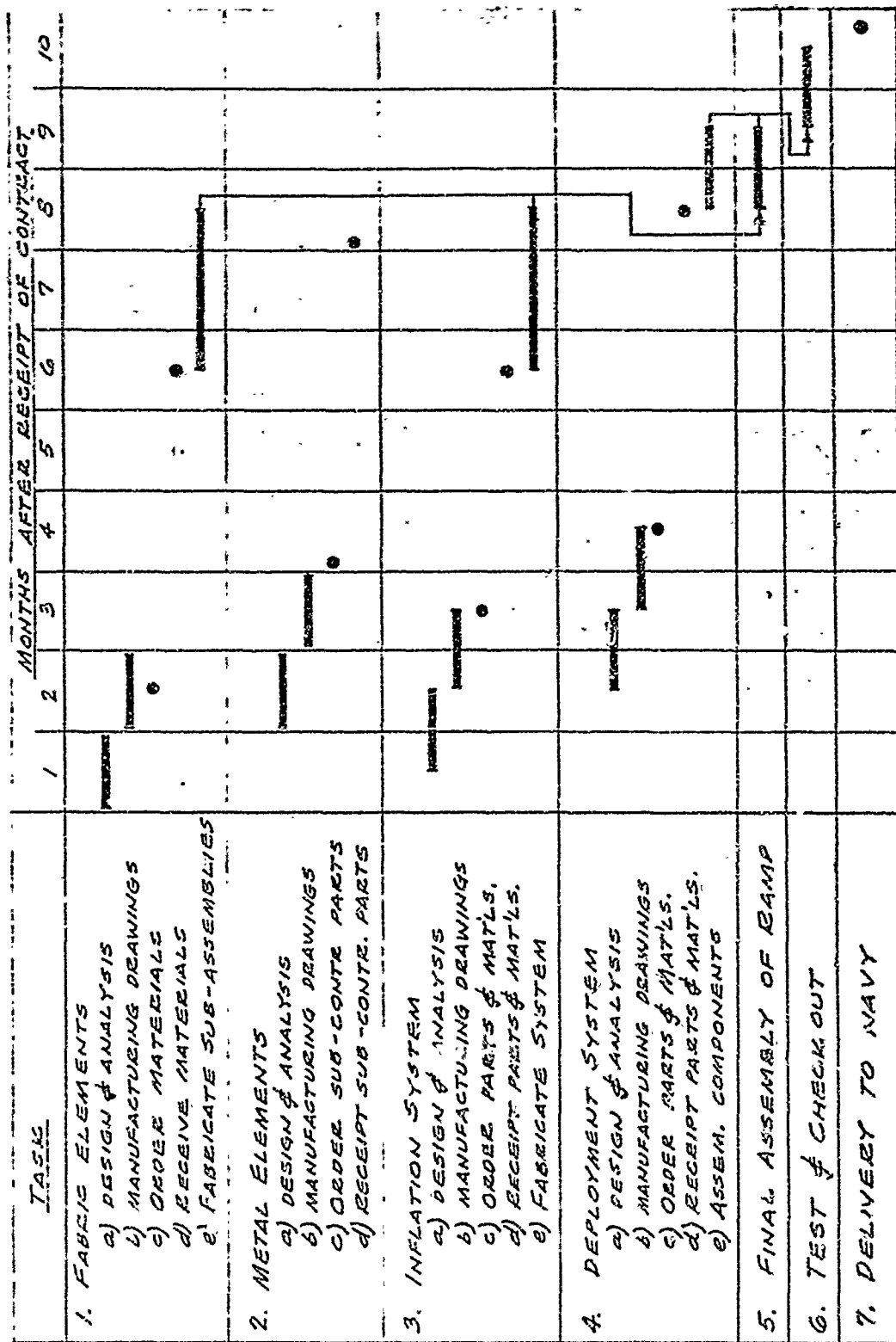


TABLE 6

GENERAL CONCLUSION

In complying with the design parameters that were outlined at the beginning of the report, ten conceptual configurations of an inflatable bow ramp were developed, with two of the concepts undergoing a refined and more detailed design analysis.

With reference to Figure 3, all of the concepts except Nos. 2 and 10 were dropped from further design analysis and considered infeasible for the reasons listed earlier in the report. Concepts Nos. 2 and 10 underwent a refined design analysis and their feasibility was evaluated by listing the advantages and disadvantages of each.

As noted on Page 25, after reviewing the advantages and disadvantages of Concept 2, it is our opinion that this concept (dual-wall beam with supports) is infeasible with respect to its present application. If, however, shorter spans with reduced loads were considered, this concept might prove to be very feasible.

Upon reviewing the advantages and disadvantages of Concept No. 10 (compression deck with inflatable bladder), it was concluded that the concept does have some possibilities. From a design point of view, the concept appears to be feasible insofar as developing an inflatable bow ramp system which will carry the 60-ton load over the 110 ft. span.

It should also be noted that this concept allows a 43% savings in weight over the existing ramp. The feasibility of this concept was further strengthened by building and testing a 1/10th scale model which carried loads in excess of the design loads.

The method of attaching this concept to the ship and operating the inflatable ramp, although not infeasible, does present some problems.

The methods recommended for attaching and operating the inflatable ramp are similar to that used on the existing bow ramp.

Therefore, it is our opinion that from an operational point of view, Concept No. 10 is impractical in that no improvements or advantages over and above the methods being used to deploy and retract the existing bow ramp are evident. Possibly, further study in this area will create new and easier operational techniques.

If, however, easier operational techniques were developed, it would be feasible to develop an inflatable bow ramp similar to Concept No. 10 which will support a 60-ton load moving over a 110 ft. span.

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20. "OPTIMUM STIFFNESS INFLATED MATTRESS BEAMS"
J. Webb, College of Aeronautics,
Dept. of Aircraft Design (England), September 1969

APPENDIX - A

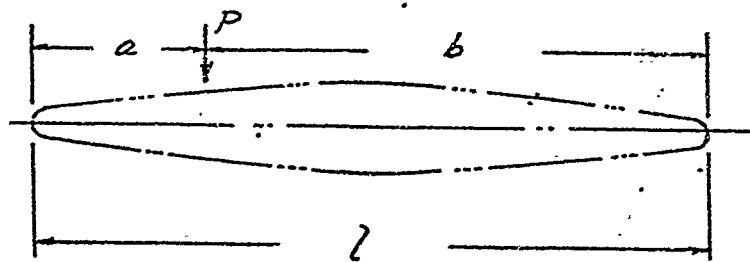
LOAD

AND

MOMENT

CALCULATIONS

INVESTIGATE BENDING MOMENT AS LOAD MOVES
ACROSS THE RAMP.



$$\text{MOMENT (MAX)} = \frac{Pab}{l} = PK_1 l$$

(@ PT. OF LOAD)

$\frac{a}{l}$	$\frac{b}{l}$	$\frac{l}{l}$	$K_1 = \frac{ab}{l}$
.1	.9	1	.09
.2	.8	1	.16
.3	.7	1	.21
.4	.6	1	.24
.5	.5	1	.25

CONSIDER GOTON TANK MOVING ALONG RAMP:
 $L = 110 \text{ FT.} = 1320 \text{ IN.}$ $P = 120,000 \text{ LBS.}$

PT. ALONG RAMP

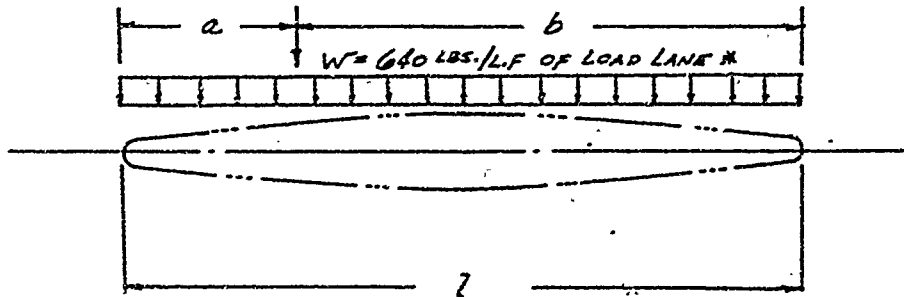
$\frac{a}{l}$	K_1	$M = PK_1 l \text{ (IN-LBS.)}$
11'	.09	14,256,000
22'	.16	25,344,000
33'	.21	33,264,000
44'	.24	38,016,000
55'	.25	39,600,000

SINCE MANY VEHICLES HAVE A WEIGHT OF AROUND
 60,000 LBS., THE MOMENT IN BENDING PRODUCED BY
 THESE VEHICLES IS $\frac{1}{2}$ OF THE MOMENT BASED ON
 THE 120,000 LB. LOAD.

INVESTIGATE A.A.S.H.O. H 20 LOADING FOR MAXIMUM BENDING MOMENT.

(LOAD INFORMATION REFERENCED FROM "STANDARD
SPECIFICATIONS FOR HIGHWAY BRIDGES, AASHO -
NINTH EDITION 1965, PAR. 1.2.5)

$P = 18,000 \text{ LBS. (FOR MOMENT) **}$



H20-44 } STD. LOADING
H520-44 } DESIGNATION

* STANDARD LOAD LANE 10 FT. WIDE.

** 26,000 LB. CONCENTRATED LOAD FOR SHEAR.

MOMENT MAX. = $M(\text{UNIFORM}) + M(\text{MOVING CONCENTRATED})$

$$M_{(\text{MAX.})} = \frac{(W)(a)(b)}{2} + \frac{P(a)(b)}{2}$$

$$W = 640 \text{ LBS./L.F.} = 53.33^{\#}/\text{L.F.}$$

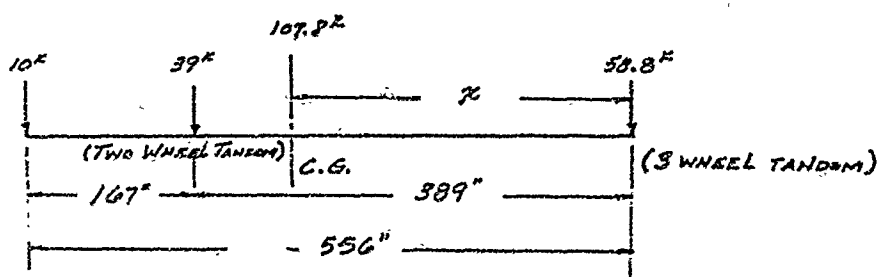
$$= \frac{W l^2}{2} K_1 + P K_1 l$$

a	K_1	$\frac{W K_1 l^2}{2}$	$P K_1 l$	$M_{\text{TOTAL}} (\text{IN-LBS.})$
11'	.09	4,179,000	2,138,000	6,317,000
22'	.16	7,430,000	3,802,000	11,232,000
33'	.21	9,751,000	4,990,000	14,741,000
44'	.24	11,144,000	5,702,000	16,846,000
55'	.25	11,616,000	5,940,000	17,556,000

INVESTIGATE MAXIMUM BENDING MOMENT CREATED BY TRACTOR, LOW BOY, DOZER COMBINATION.

Q.) DISTRIBUTION OF LOADS:

	<u>FRONT AXIL TRACTOR</u>	<u>REAR AXIAL TRACTOR</u>	<u>REAR AXIAL TRAILER</u>
Wt. of TRACTOR	10 ^K	10.5 ^K	
Wt. of TRAILER		5.0 ^K	11.8 ^K
Wt. of DOZER (2/3 TO REAR AXIL)		23.5 ^K	17.0 ^K
<u>TOTAL</u>	<u>10^K</u>	<u>39.0^K</u>	<u>58.8^K</u>



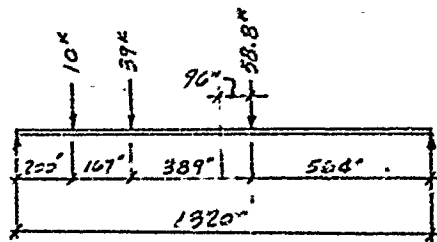
LOCATE CENTER OF GRAVITY OF LOADS:

<u>FORCE (K)</u>	<u>LEVER ARM (")</u>	<u>MOMENT (K")</u>
39	389	15,171
10	556	5,560
		<u>20,731</u>

$$X = \frac{20,731}{107.8K} = 192.3"$$

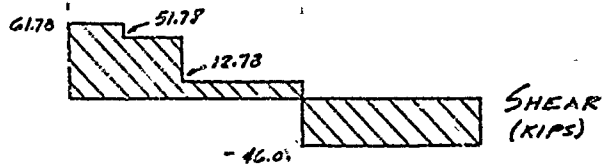
FOR MAXIMUM BENDING MOMENT, THE CENTER LINE OF THE RAMP SHOULD BE MIDWAY BETWEEN THE CENTER OF GRAVITY AND THE NEAREST CONCENTRATED LOAD.

b) SHEAR & MOMENT DIAGRAM:

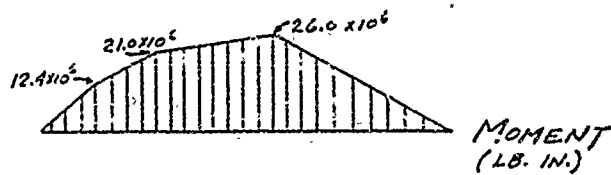


$$110' \times 12 = 1320"$$

8.49	1.51
28.16	10.84
25.13	38.67
<u>61.78 K</u>	<u>46.02 K</u>



[NOTE: MAX. SHEAR OCCURS WITH LARGEST WHEEL LOAD AT SUPPORT]

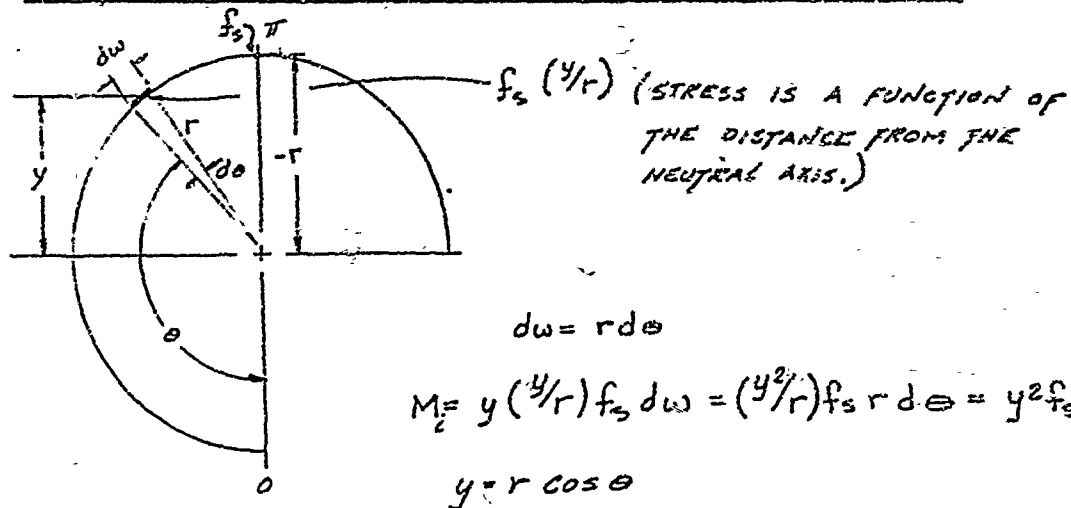


* NOTE: IF LOAD IS CONSIDERED AS A CONCENTRATED FORCE AT MIDSPAN, MAX. BENDING MOMENT IS:

$$M = \frac{PL}{4} = \frac{(107.8 K)(110 FT.)}{4} = 2964 KIP-FT$$

$$= 35.6 \times 10^6 LB-IN.$$

DERIVATION OF DUAL WALL EQUATIONS:



$$dw = r d\theta$$

$$M_i = y (y/r) f_s dw = (y^2/r) f_s r d\theta = y^2 f_s d\theta$$

$$y = r \cos \theta$$

WHERE:

$$f_s = \text{FABRIC STRESS} \quad M_i = f_s r^2 \cos^2 \theta d\theta$$

$$M_i = \text{INCREMENTAL MOMENT} \quad M_r = \int_0^\pi f_s r^2 \cos^2 \theta d\theta$$

$$\begin{aligned} M_r = \text{TOTAL RESISTIVE MOMENT} &= r^2 f_s \int_0^\pi \cos^2 \theta d\theta \\ &= r^2 f_s \left[\frac{1}{2} \sin \theta \cos \theta + \frac{1}{2} \theta \right]_0^\pi \\ &= r^2 f_s \left[\pi/2 \right] \end{aligned}$$

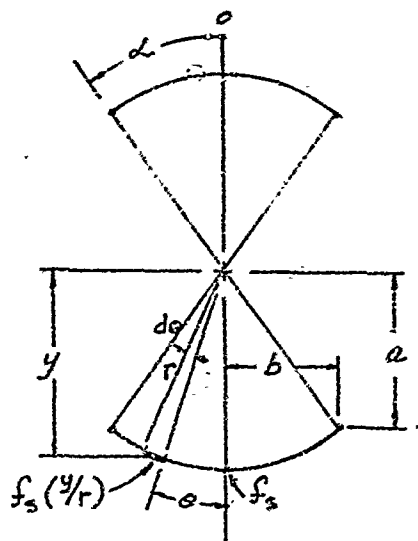
$$\begin{aligned} M_r &= r^2 f_s \pi/2 \\ &\text{OR} \\ &= (d/2)^2 f_s \pi/2 \end{aligned}$$

$$M_r = \frac{d^2 \pi f_s}{8}$$

FOR FULL CIRCLE (OR BOTH SIDES)

$$M_r = 2 \left(\frac{d^2 \pi f_s}{8} \right)$$

$$M_r = \frac{d^2 \pi f_s}{4}$$



$$M_i = f_s(y/r) y (r d\theta)$$

$$= f_s y^2 d\theta$$

$$y = r \cos \theta$$

$$(\text{FOR } 1/4 \text{ CELL}) \quad M_i = \int_0^\alpha f_s r^2 \cos^2 \theta d\theta$$

$$(\text{PER CELL}) \quad M_r = 4 f_s r^2 \int_0^\alpha \cos^2 \theta d\theta$$

$$M_r = 4 f_s r^2 \left[\frac{1}{2} \sin \theta \cos \theta + \frac{1}{2} \theta \right]_0^\alpha$$

$$M_r = 2 f_s r^2 \left[\sin \theta \cos \theta + \theta \right]_0^\alpha$$

$$\alpha = \sin^{-1}(b/r) \text{ OR } \alpha = \cos^{-1}(a/r)$$

$$M_r = 2 f_s r^2 \left[(b/r)(a/r) + \sin^{-1}(b/r) \right]$$

$$M_r = 2 f_s r^2 \left[ab/r^2 + \sin^{-1}(b/r) \right]$$

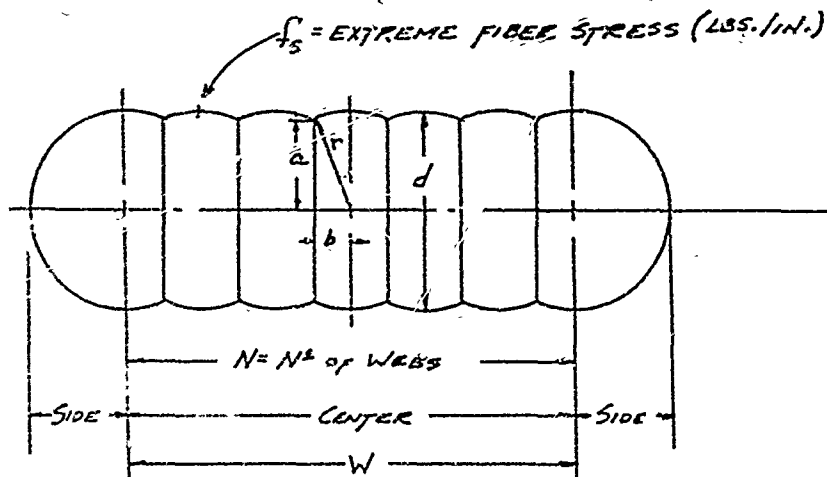
$$(\text{PER CELL}) \quad \underline{M_r = 2 f_s [ab + r^2 \sin^{-1}(b/r)]}$$

OR

$$f_s = \frac{M_r}{2 [ab + r^2 \sin^{-1}(b/r)]}$$

TOTAL RESISTIVE BENDING MOMENT -

NO HORIZONTAL REACTION IN WEBS:
 (∴ MAX. BENDING RESISTANCE AS ALL
 PRESSURIZATION PRETENSION IS CARRIED
 BY SKINS AT MAX. MOMENT DISTANCE
 FROM THE NEUTRAL AXIS)



$$\text{TOTAL } M_r = \underbrace{N^2 f_s [ab + r^2 \sin^{-1}(b/r)]}_{\text{CENTER SECTION}} + \underbrace{\frac{\pi d^2 f_s}{4}}_{\text{SIDES}}$$

$$= \underbrace{N^2 b}_{\text{WIDTH OF CENTER}} [f_s a + f_s r^2/b \sin^{-1}(b/r)] + \frac{\pi d^2 f_s}{4}$$

$$M_r = W [f_s a + f_s (r^2/b) \sin^{-1}(b/r)] + \frac{\pi d^2}{4} (f_s)$$

OR

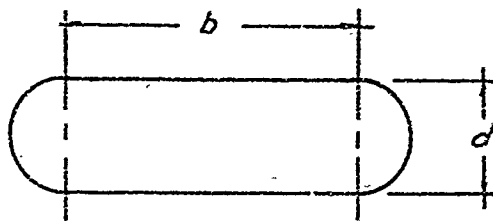
$$f_s = \frac{M_r}{W [a + (r^2/b) \sin^{-1}(b/r)] + \pi d^2/4}$$

COMPARISON TO FLAT PLATE THEORY USED
BY THE MILITARY AND ENGINEERING ESTABLISHMENT
OF CHRISTCHURCH, ENGLAND.

(REFER TO REF. NO. 1)

BASIC FLAT PLATE THEORY

REF. NO. 1 PG. 7



ASSUMPTION:

NEGLECT EFFECTS OF
WEBS TO CARRY BENDING
MOMENT.

MOMENT OF RESISTANCE TO BENDING IS MADE
UP OF TWO COMPONENTS:

1) FLAT TOP AND BOTTOM PORTIONS OF SKIN

$$M_r = f_s \times b \times d$$

M_r = MOMENT OF RESISTANCE
 f_s = STRESS IN SKIN PER
UNIT WIDTH OF FABRIC
(TENSION OR COMPRESSION)

2) SEMI-CIRCULAR EDGES OF SKIN

$$M_r = f_s \times \pi d^2 / 4$$

$$\therefore \text{TOTAL RESISTIVE MOMENT} = f_s (bd + \pi d^2 / 4)$$

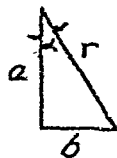
(FLAT PLATE THEORY)

BIRDAIR'S DUALWALL EQUATION:

$$M_r = W [f_s a + f_s (r^2/b) \sin^{-1}(b/r)] + \frac{\pi d^2}{4} (f_s)$$

(REFER TO PAGE B-3 FOR NOMENCLATURE)

COMPARISON OF DUAL WALL EQUATION TO FLAT PLATE THEORY



$$r^2 \underbrace{\sin^{-1}(b/r)}_{\alpha} = r^2 \alpha$$

IN FLAT PLATE THEORY

$$r \rightarrow a$$

$$\alpha \rightarrow 0$$

$$\text{AS } r \rightarrow a$$

$$r^2 \alpha = ar\alpha$$

$$\text{AS } \alpha \rightarrow 0$$

$$b = r\alpha$$

$$ar\alpha \rightarrow ab$$

$$M_r = W [f_s a + f_s (r^2/b) \sin^{-1}(b/r)] + \frac{\pi d^2}{4} (f_s)$$

$$\text{SINCE } r^2 \sin^{-1}(b/r) \rightarrow ab$$

$$M_r = W [f_s a + f_s ab/b] + \frac{\pi d^2}{4} (f_s)$$

$$\text{SINCE } W = \text{WIDTH} = b$$

$$M_r = b (f_s a + f_s a) + \frac{\pi d^2}{4} (f_s)$$

$$\text{SINCE } a = d/2$$

$$\underline{M_r = f_s (bd + \pi d^2/4)}$$

AGREES WITH FLAT PLATE
THEORY.

APPENDIX - C

PRELIMINARY

DESIGN

CALCULATIONS

CONCEPT No 1

AND

CONCEPT No 2

DUAL-WALL BEAM

WITH OR WITHOUT

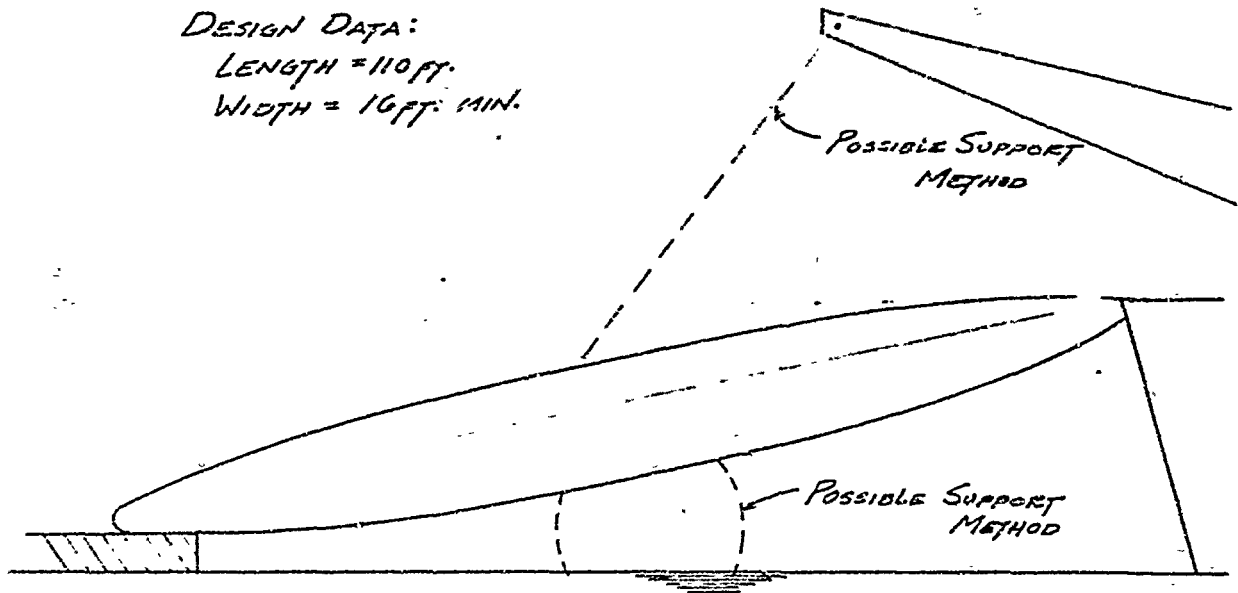
INTERMEDIATE SUPPORTS

DUAL-WALL BEAM CONCEPT:

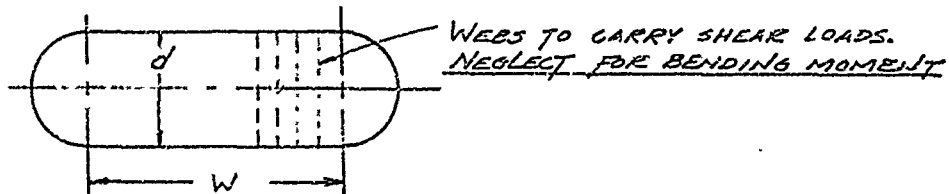
DESIGN DATA:

LENGTH = 110 FT.

WIDTH = 10 FT. MIN.



ANALYZE FIRST AS A FLAT PLATE WITH NO
SUPPORT MECHANISM



$$F = pA$$

$$A = wd + \pi d^2/4$$

$$C = \text{CIRCUMFERENCE} = 2W + \pi d$$

$$S_L (\text{INFLATION STRESS - LONGITUDINAL}) = \frac{F}{C}$$

$$S_L = \frac{(wd + \pi d^2/4) \cdot p}{2W + \pi d}$$

$$S_t (\text{INFLATION STRESS - TRANSVERSE}) = p d/2$$

C-1

STRESS DUE TO BENDING MOMENT:

$$f_s = \frac{M}{A} = \frac{M}{wd + \pi d^2/4}$$

TO PREVENT WRINKLING $s_i = f_s$ (LONGITUDINAL)

$$\frac{(wd + \pi d^2/4)p}{2w + \pi d} = \frac{M}{wd + \pi d^2/4}$$

$$w = 16 \text{ FT} = 192 \text{ IN.}$$

$$\frac{(192d + \pi d^2/4)p}{384 + \pi d} = \frac{M}{192d + \pi d^2/4}$$

$$M = \frac{(192d + \pi d^2/4)^2 p}{384 + \pi d} \quad \text{(FLAT PLATE APPROACH)} \\ \text{(MOST EFFICIENT)}$$

MAX. LONGITUDINAL FABRIC STRESS = $s_i + f_s$

SINCE $s_i = f_s$

MAX. LONGITUDINAL FABRIC STRESS = $2 s_i$

BENDING MOMENTS:

SIMPLY SUPPORTED - 60 TON LOAD @ MIDSPAN:

$$M = \frac{Pl}{4} = \frac{(120,000 \text{ LBS})(110 \text{ FT})(12)}{4} = \underline{39,600,000 \text{ LB.-IN.}}$$

SIMPLY SUPPORTED WITH SUPPORT @ CENTER - 60 TON LOAD @ QUARTER SPAN

$$M = \frac{19}{64}(P)(l/2) = \left(\frac{19}{64}\right)(120,000)(55)(12) = \underline{16,088,000 \text{ IN.-LBS.}}$$

X:SUJERSEARCH

01/10/ '73 10:18

LOGIN: 1507BRD.C

ID= F

IBASIC

>10 PRINT "M(IN-LBS)=:"

>20 INPUT N

>30 FOR D=50 TO 300 STEP 50

>40 F=M/((192*D)+((3.14*D*D)/4))

>50 P=(F*(384*(3.14*D))/((192*D)+((3.14*D*D)/4))

>60 S1=P*(D/2)

>70 S=2*F

>80 PRINT D,F,S,S1,P

>90 NEXT D

>100 END

>RUN

10:22 01/10

M(IN-LBS)= 232600000

	f_s FABRIC STRESS BENDING MOM. (LBS./IN.)	f_t MAX. FABRIC STRESS (LBS./IN.)	S_1 TRANS. FABRIC STRESS (LBS./IN.)	P INPL. PRESS. (LBS./IN. ²)
50 DEPTH	3424.86	6649.73	4006.17	160.247
100 (IN)	1463.96	2927.91	1888.80	37.7760
150	852.300	1704.60	1176.30	15.6840
200	567.335	1134.37	822.555	8.22555
250	407.985	815.969	614.210	4.91368
300	308.772	617.544	478.867	3.19245

100 HALT

>RUN

10:23 01/10

M(IN-LBS)= 216088000

50	1391.39	2782.79	1627.56	65.1022
100	594.750	1189.50	767.349	15.3470
150	346.258	692.515	477.886	6.37181
200	230.487	460.974	334.173	3.34173
250	165.749	331.498	249.530	1.95614
300	125.442	250.883	194.546	1.29697

100 HALT

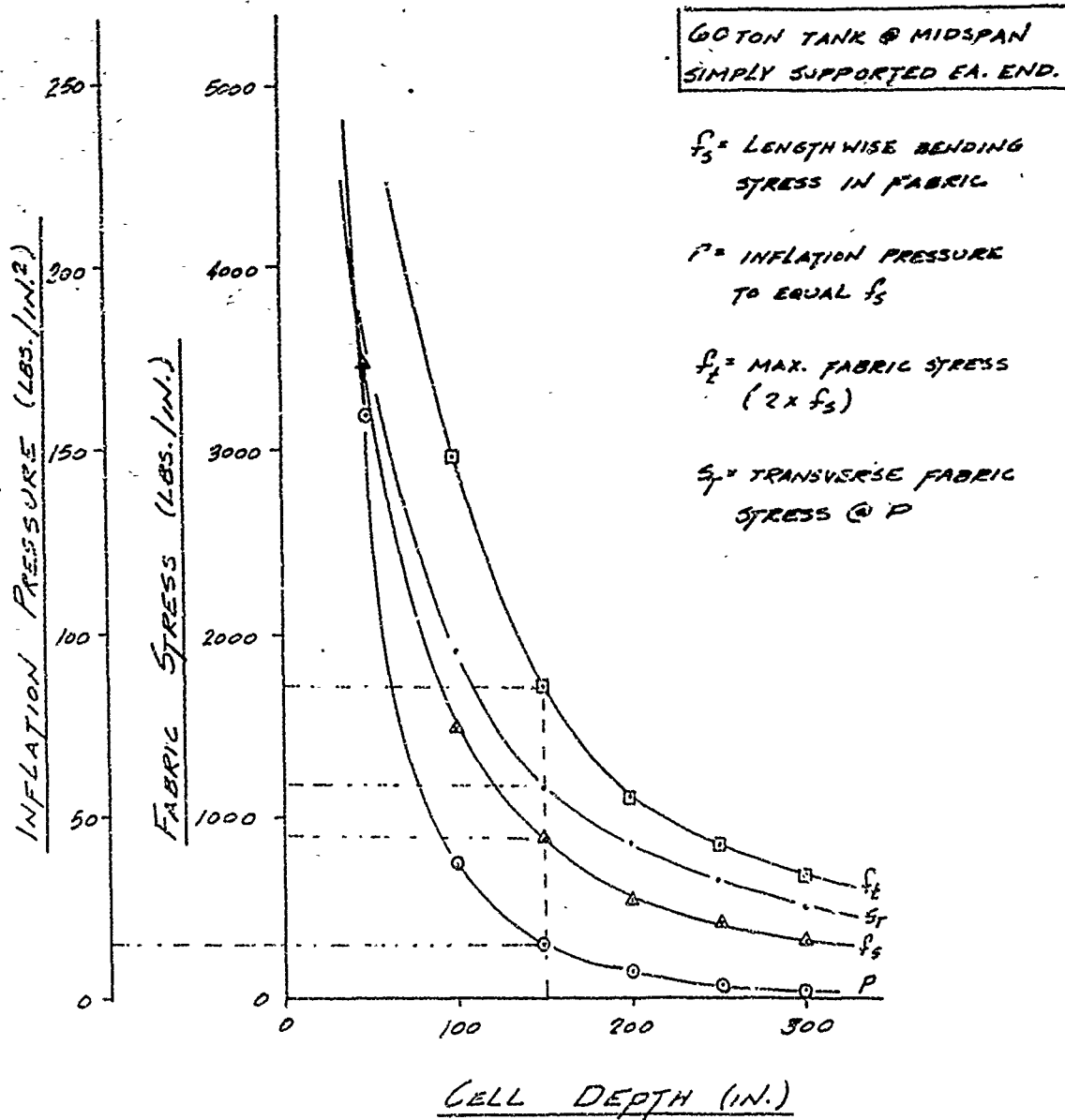
>SYS

IBYE

01/10/ '73 10:24

CLT 5

CCU 0.008



FOR $D = 150$ IN.

$$f_s = 852 \text{ LBS./IN.}$$

$$P = 15.7 \text{ LBS./IN.}^2$$

$$f_t = 1704 \text{ LBS./IN.}$$

$$s_r = 1176 \text{ LBS./IN.} \quad C-4$$

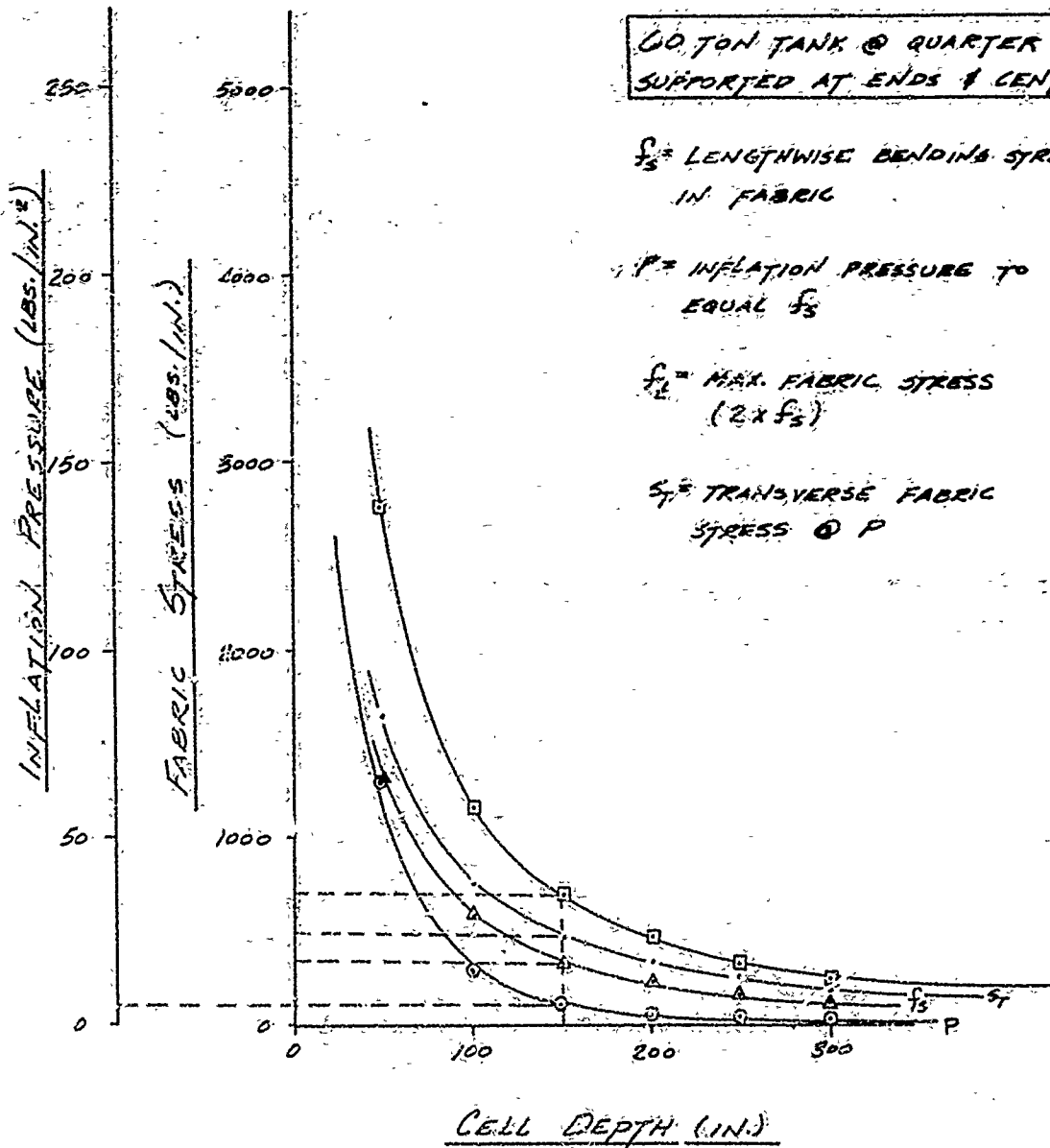
CO TON TANK @ QUARTER SPAN
SUPPORTED AT ENDS & CENTER

f_s = LENGTHWISE BENDING STRESS
IN FABRIC

P = INFLATION PRESSURE TO
EQUAL f_s

f_t = MAX. FABRIC STRESS
($2 \times f_s$)

s_T = TRANSVERSE FABRIC
STRESS @ P



FOR $D = 150$ IN.

$$f_s = 346 \text{ lbs./in.}$$

$$P = 6.6 \text{ lbs./in.}^2$$

$$f_t = 692 \text{ lbs./in.}$$

$$s_T = 478 \text{ lbs./in.} \quad C = 5$$

COMPUTERSEARCH

01/10/ '73 13:20

112GIN: 1567BRD.C.

ID# 2

1BASTC

>10 PRINT"P(PSI)=";

>20 INPUT P

>30 FOR D=20 TO 300 STEP 20

>40 X=(1925D+.7854*D*2)*2

>50 Y=384*3*14159*2

>60 M=X*P/Y

>70 PRINT D,M

>80 NEXT D

>90 END

>RUN

13:24 01/10

P(PSI)= 718

MOMENT (IN.-lbs.)

20	DEPTH	617934.
40	(in.)	2.50718E+06
60		5.75303E+06
80		1.04667E+07
100		1.67737E+07
120		2.48078E+07
140		3.47080E+07
160		4.65167E+07
180		6.06785E+07
200		7.70394E+07
220		9.58468E+07
240		1.17249E+08
260		1.41393E+08
280		1.68430E+08
300		1.98508E+08

>90 HALT

>RUN

13:25 01/10

P(PSI)= 76.4

20		247174.
40		1.00287E+06
60		2.30121E+06
80		4.18669E+06
100		6.70948E+06
120		9.92311E+06
140		1.38832E+07
160		1.86467E+07
180		2.42714E+07
200		3.08158E+07
220		3.83387E+07
240		4.62994E+07
260		5.65573E+07
280		6.73721E+07
300		7.94033E+07

>90 HALT

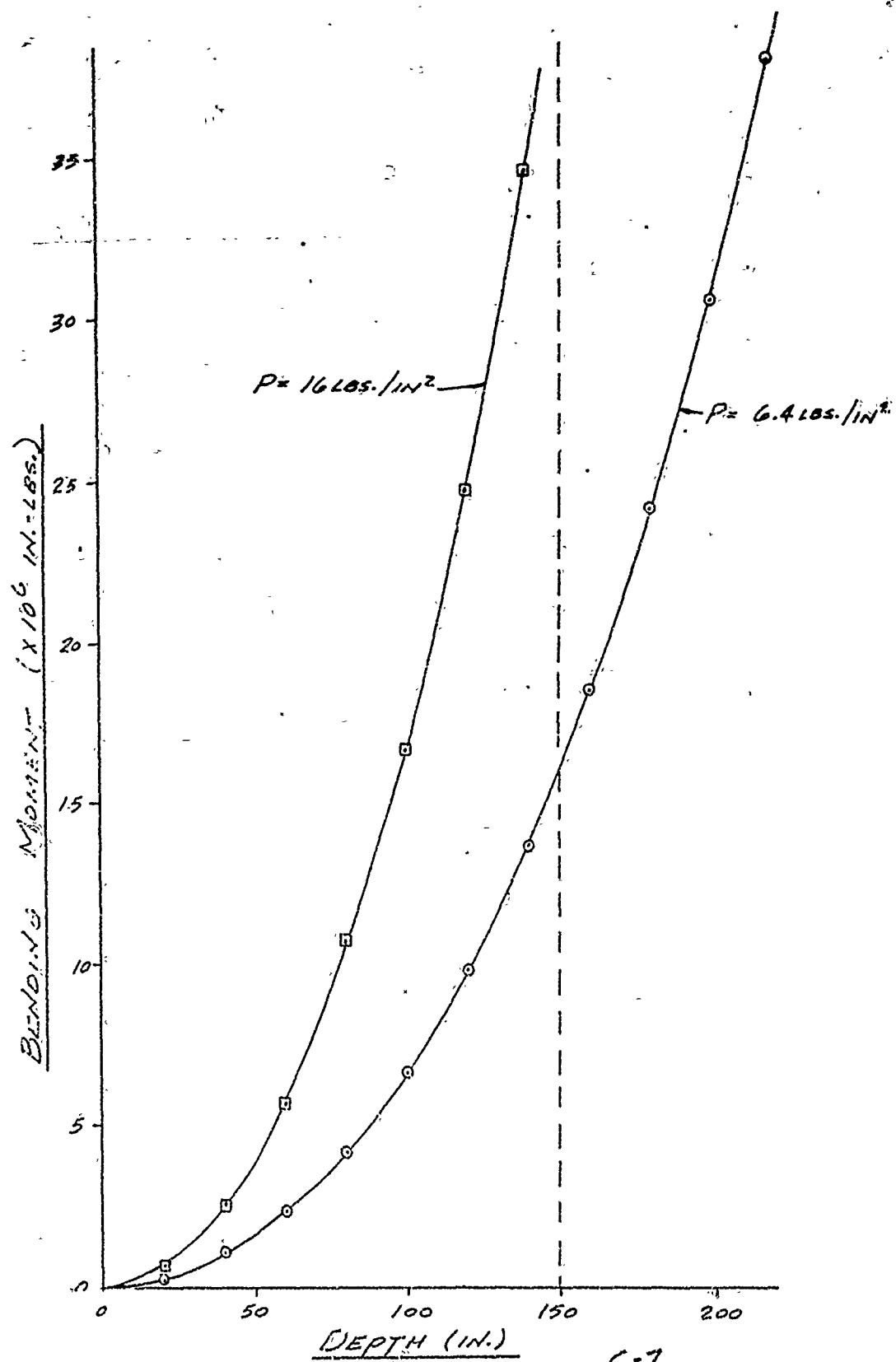
>SYS

1BYE

01/10/ '73 13:26

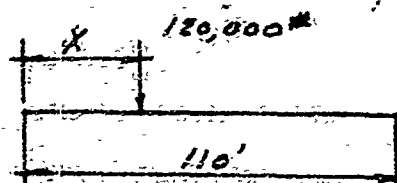
CIT 6

C-6



C-7

VNXXXXOC



USERSEARCH

01/10/ '73 14:45

!LOGIN: 1507BRD,C,

?

!LOGIN: 1507BRD,C,

ID= D

!BASIC

>10 FOR X=0 TO 720 STEP 120

>20 M=((120000*X)*(1320-X))/1320

>30 PRINT X,M

>40 NEXT X

>50 END

>RUN

14:47 01/10

MOMENT (IN-LBS.)

DEPTH (FROM GRAIN)

0	0	1.30909E+07	85" = 7.33'
10' 120		2.35636E+07	118" = 9.83'
20' 240		3.14182E+07	135" = 11.25'
30' 360		3.66545E+07	142" = 11.83'
40' 480		3.92727E+07	150" = 12.50'
50' 600		3.92727E+07	150" = 12.50' MAX.
60' 720			

DISTANCE

50 HALT ALONG RAMP

>SYS

!BYE

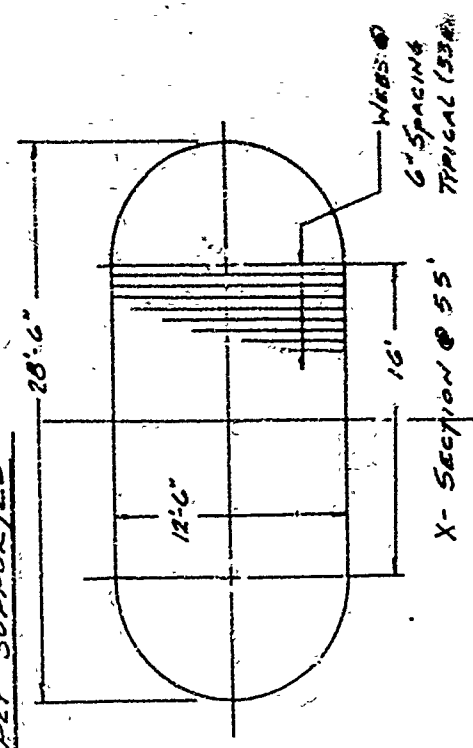
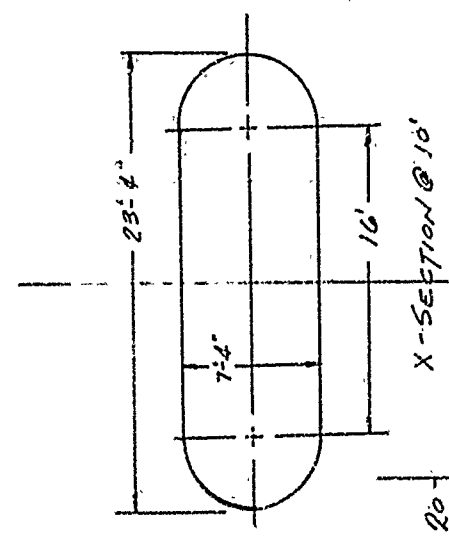
01/10/ '73 14:47

CLT 1

CCU 0.010

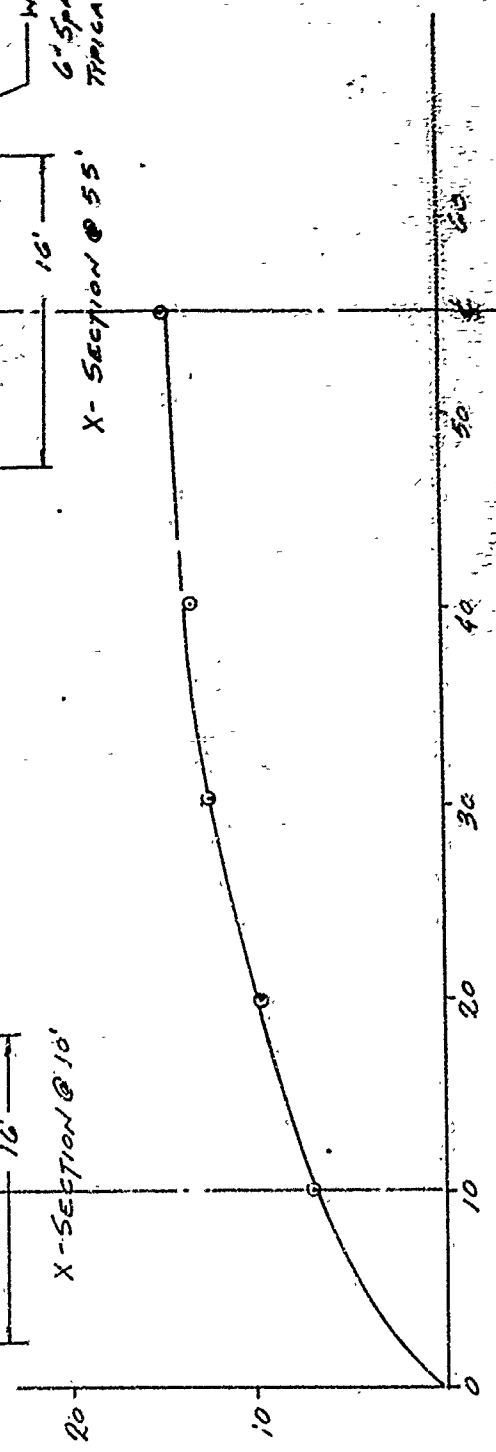
RAMP SIZE TO CARRY BENDING MOMENT

- INITIAL WRINKLE THEORY
- INFLATION PRESS. = 16 LBS./IN²
- MAX. LOAD = 60 TONS (CONCENTRATED ANY PLACE ALONG RAMP)
- ENDS SIMPLY SUPPORTED



6-2

DEPTH OF RAMP (FT.)



DISTANCE ALONG RAMP (FT.)

COMPUTERSEARCH

01/11/ '73 08:41

!LOGIN: 1507BRD,C,

ID= B

!BASIC

>10 FOR A=0 TO 660 STEP 60

>20 X=(120000*A*(660-A))/(4*660+3)

>30 Y=((4*660+2)-(A*(660+A)))

>40 M=X*Y

>50 X1=(120000*A*(660-A))/(4*660+2)

>60 Y1=660+A

>70 M1=X1*Y1

>80 PRINT A,M,M1

>90 NEXT A

>100 END

>RUN

08:44 01/11

	M @ LOAD (LB.-IN.)	M @ CNTR. (LB.-IN.)	DEPTH REQ. AT POINT OF LOAD	MAX. DEPTH @ CNTR. FOR MAX. MOMENT @ CNTR.
0	0	0		
60 5'	6.38317E+06	1.78512E+06	97" = 8.08'	
120 10'	1.11489E+07	3.48099E+06	128" = 10.67'	
180 15'	1.43459E+07	4.99835E+06	142" = 11.83'	
240 20'	1.60553E+07	6.24793E+06	150" = 12.50'	
300 25'	1.63907E+07	7.14050E+06	150" = 12.50'	
360 30'	1.54981E+07	7.58678E+06	148" = 12.33'	107" = 8.92'
420 35'	1.35561E+07	7.49752E+06	138" = 11.50'	
480 40'	1.07757E+07	6.78347E+06	125" = 10.42'	
540 45'	7.40015E+06	5.35537E+06	105" = 8.75'	
600 50'	3.70548E+06	3.12397E+06	75" = 6.25'	
660 55'	0	0		

100 HALT

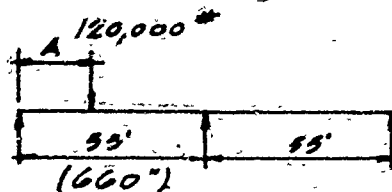
>SYS

!BYE

01/11/ '73 08:45

CLT 4

CCU 0.013

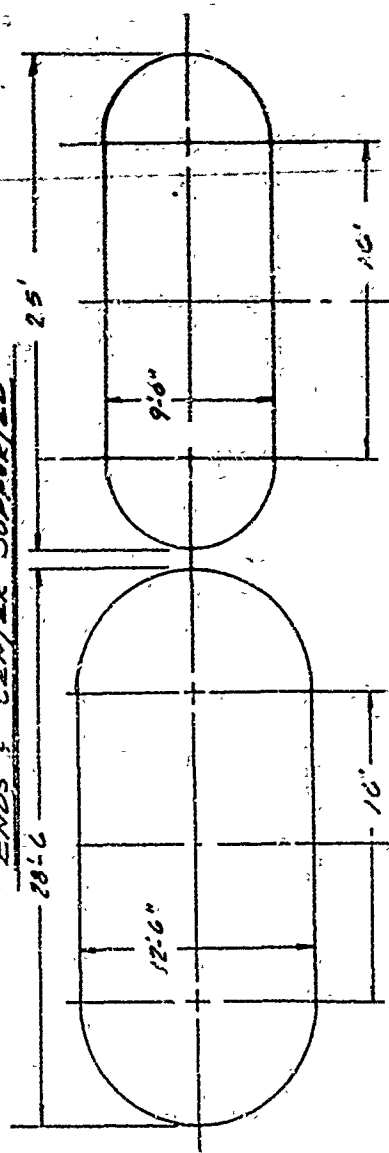


$$P = 6.4 \text{ LB.}/\text{IN}^2$$

RAMP SIZE TO CARRY BENDING MOMENT

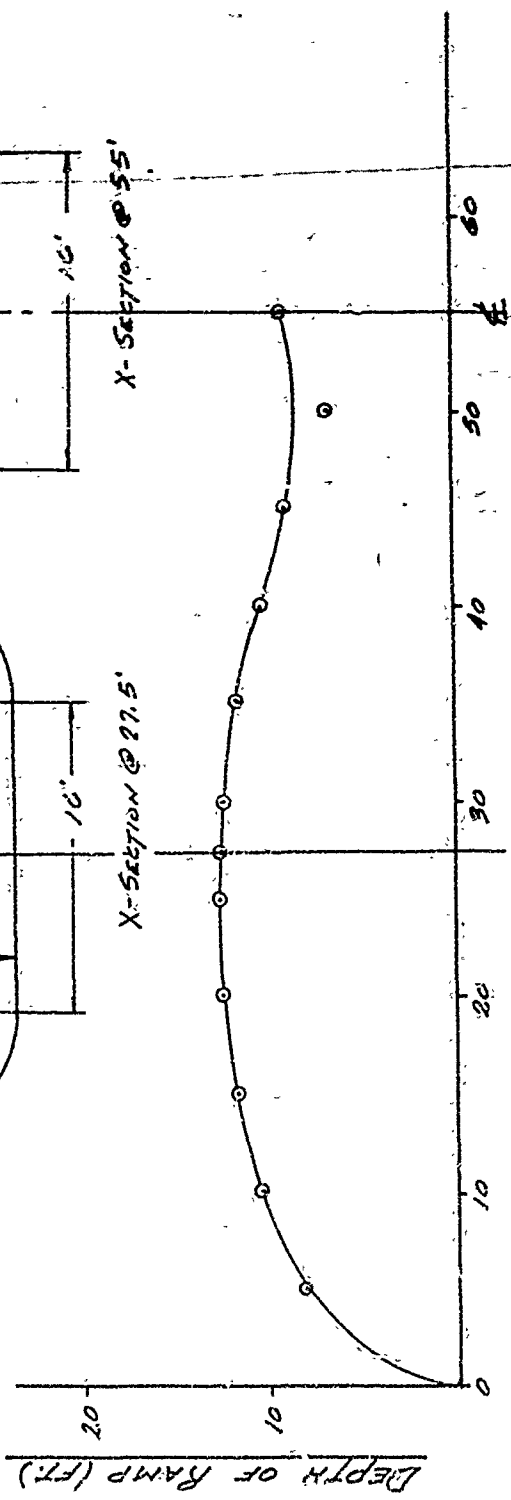
- INITIAL WRINKLE THEORY
- INFLATION PRESS. = 6.4 LBS./IN.²
- MAX. LOAD = 60 TONS (CONCENTRATED ANYPLACE ALONG RAMP)

" ENDS & CENTER SUPPORTED



X-SECTION @ 27.5'

X-SECTION @ 55'



DISTANCE ALONG RAMP (FT.)

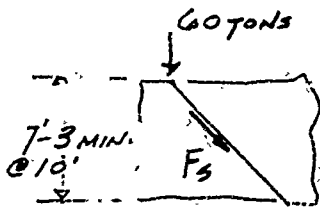
SHEAR STRESSES:

MAX. SHEAR OCCURS NEAR THE SUPPORT

MAX. VERTICAL SHEAR FORCE AT ULTIMATE CONDITIONS =
60 TONS

TENSILE LOAD AT 45°

$$\text{LOAD} = \sqrt{2} \times 60 \text{ TONS} \times 2000 \text{ LBS/TON} = 169,705 \text{ LBS.} = F_s$$



IF WEBS ARE SPACED AT 6"

$$\text{N}^\circ \text{ OF SPACES} = \frac{16 \times 12}{6} = 32$$

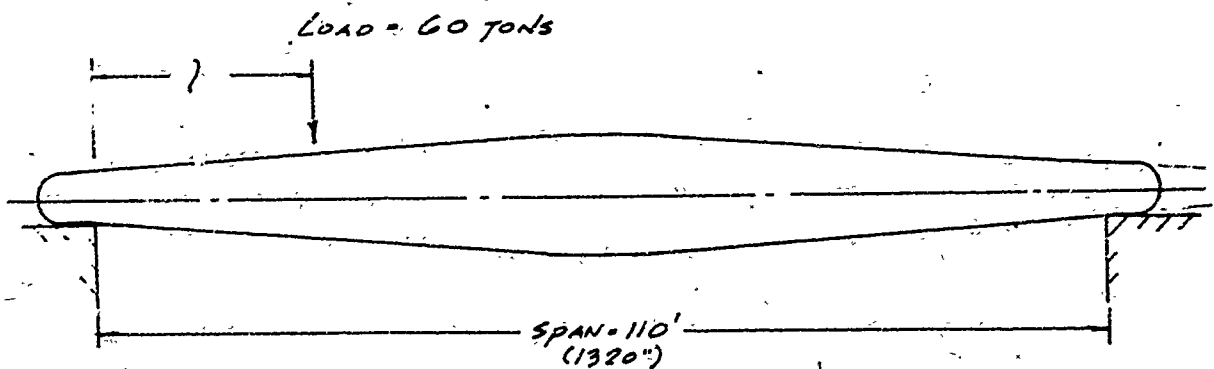
$$\text{N}^\circ \text{ OF WEBS} = 32 + 1 = 33 \text{ WEBS}$$

$$\text{FORCE IN EA. WEB} = \frac{169,705}{33} = 5143 \text{ LBS.}$$

$$\text{STRESS PER WEB} = \frac{5143 \text{ LBS.}}{(\sqrt{2})(87'')} = 41.80 \text{ LBS./IN.}$$

(ON BIAS)

DEFLECTION FOR DUAL WALL BEAM-CONCEPT N^o 1



$$\delta = \frac{(P)(x)}{PA}$$

DEFLECTION

WHERE:

P = SHEAR FORCE

A = CROSS-SECTIONAL AREA
AT POINT OF LOAD

p = INFLATION PRESSURE

x = DISTANCE FROM LOAD TO SUPPORT

$$P \text{ (SHEAR FORCE)} = \frac{(\text{LOAD})(110-x)}{110} = \frac{(\text{LOAD})(1320-x)}{1320}$$

FOR MAX. BENDING MOMENT, INFLATION PRESS. REQ.
IS 16 LBS./IN.²

MAX. FABRIC STRESS (LONGITUDINAL) = 1704 LBS./IN.

FOR DEPTH OF SECTION, REFERENCE FIGURE N^o 1

$$A = (192)(D) + \pi D^2/4 \quad D = \text{DEPTH OF SECTION}$$

$$\delta = \frac{(\text{LOAD})(1320-x)(x)}{(1320)(p)[192D + \pi D^2/4]}$$

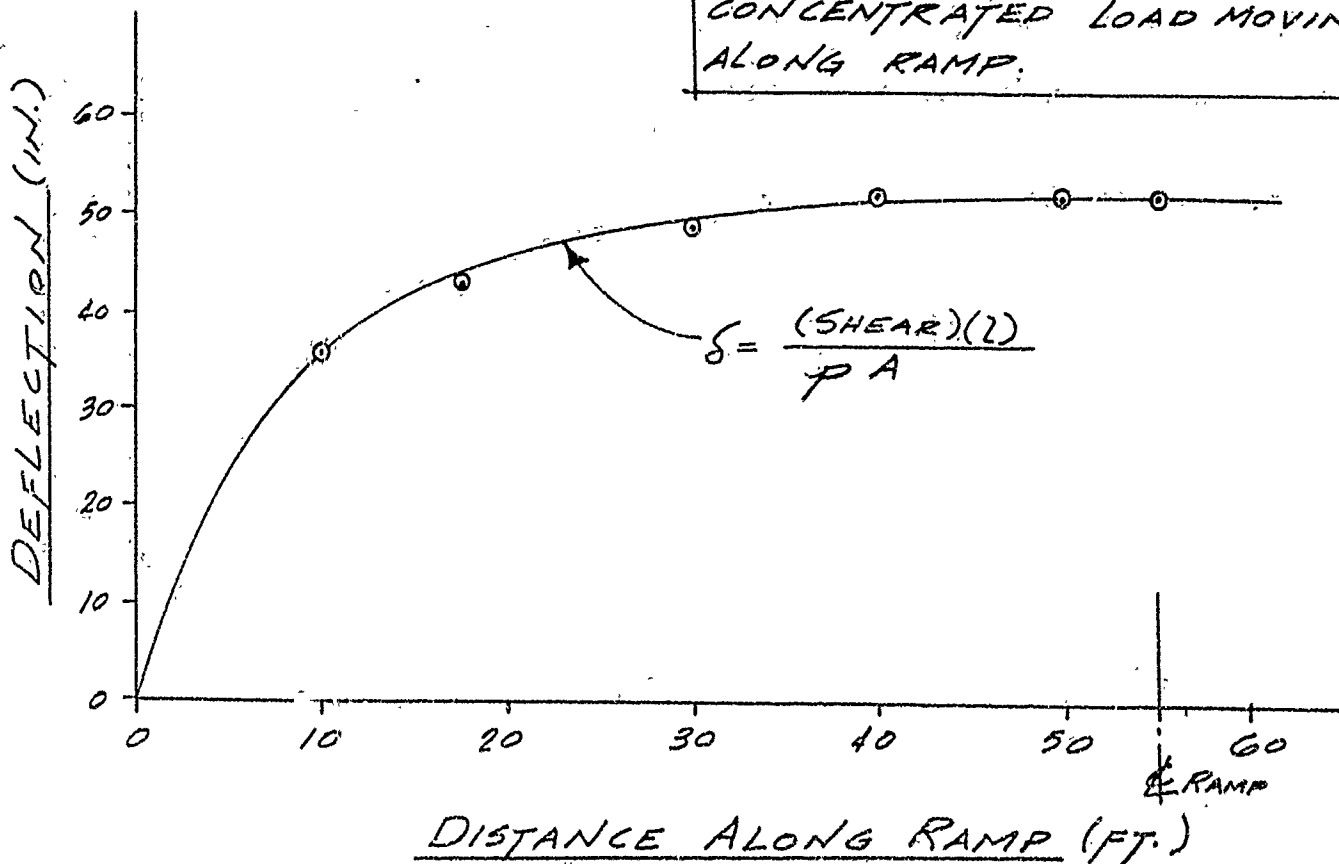
SUBSTITUTING FOR p = 16 LBS./IN.²
LOAD = 120,000 LBS

$$\delta = \frac{5.682 \ell (1320 - \ell)}{192 D + .785 D^2}$$

FROM FIGURE NO 1

ℓ (IN.)	D (IN.)	δ (IN.)
120	88	35.6
240	118	43.4
360	135	48.8
480	143	52.7
600	150	52.8
660	150	53.3

DEFLECTION-FOR 60TON
CONCENTRATED LOAD MOVING
ALONG RAMP.



CONCEPT No. 1

OVERALL DIMENSIONS: 28'-6" WIDE x 12'-6" DEEP

FABRIC STRESS: 1704 LBS./IN.

INFLATION PRESS: 16 LBS./IN.²

$$Vol. = (16)(12.5) + (\pi)(12.5)^2/4 = 323$$

$$(16)(7.25) + (\pi)(7.25)^2/4 = 157$$

$$480 \div 2 = 240 \times 110 = 26,400 \text{ c.f.}$$

$$SURFACE AREA: (32) + (\pi)(12.5) = 71.3$$

$$(32) + (\pi)(7.25) = 54.8$$

$$126.1 \div 2 = 63 \times 110 = 6930 \text{ s.f.}$$

CONCEPT No. 2

OVERALL DIMENSIONS: 28'-6" WIDE x 12'-6" DEEP

FABRIC STRESS: 692 LBS./IN.

INFLATION PRESS: 6.4 LBS./IN.²

$$Vol. = (16)(12.5) + (\pi)(12.5)^2/4 = 323$$

$$(16)(9) + (\pi)(9)^2/4 = 207$$

$$530 \div 2 = 265 \times 110 = 29,150 \text{ c.f.}$$

$$SURFACE AREA: 32 + (\pi)(12.5) = 71.3$$

$$32 + (\pi)(9) = 60.3$$

$$131.6 \div 2 = 65.8 \times 110 = 7238 \text{ s.f.}$$

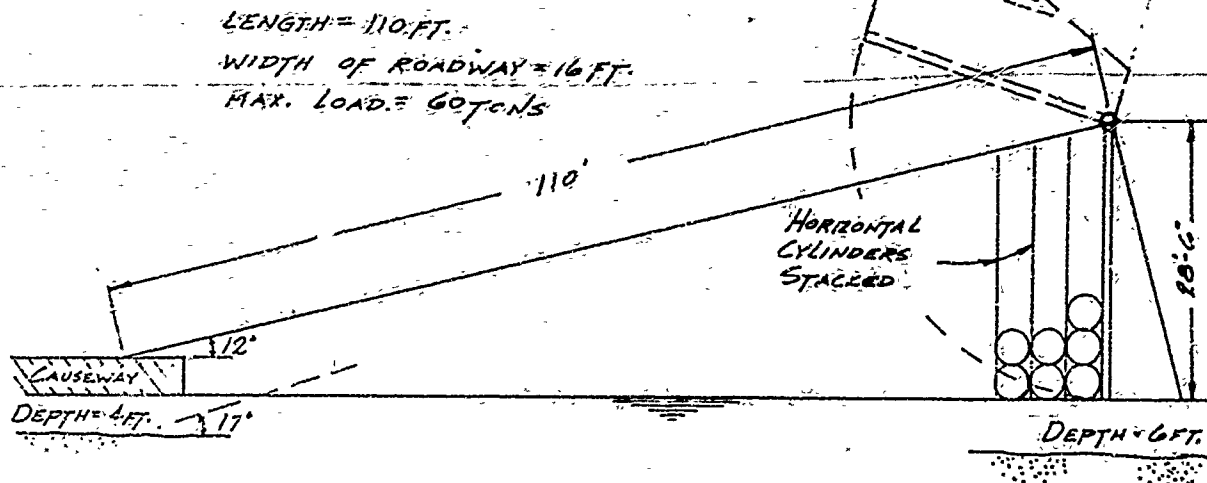
CONCEPT № 3

DUAL-WALL WEDGE

C-15a

DUAL WALL WEDGE CONCEPT:

DESIGN DATA:



DESIGN ASSUMPTIONS:

- 1) AVERAGE WATER DEPTH = 5 FT.
- 2) INFLATION PRESSURE REQD. TO RESIST LOCAL BENDING ONLY, CREATED BY TIRE OR TRACK FOOTPRINT LOADS.

CRITICAL LOADINGS:

60 TON TANK - 13 LBS./IN² = 346 LBS./IN. (PER TRACK LENGTH)
30,000 LB. TRUCK CRANE - 60-70 LBS./IN² (TIRE PRESSURE)
SCRAPER (MODEL 627 CAT) - 45-50 LBS./IN² (TIRE PRESSURE)

WHEEL LOADING CRITICAL - ASSUME 60 LBS./IN² REQD.
FOR LITTLE OR NO LOCAL DEFLECTION.

VOLUME OF WEDGE: (APPROX.)

$$\frac{1}{2}(110)(30)(20) = 33,000 \text{ FT}^3$$

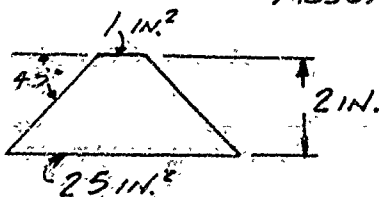
MAXIMUM FABRIC STRESS IN A CYLINDER DUE TO INFLATION LOAD IS:

$$S = p r \quad \begin{array}{l} p = \text{INFLATION PRESSURE} \\ r = \text{RADIUS OF CYLINDER} \end{array}$$

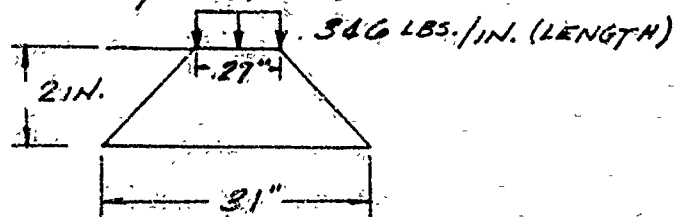
SINCE INFLATION PRESSURE (60 LBS./IN²) IS RELATIVELY HIGH, VERY SMALL DIAMETER CYLINDERS WILL BE REQUIRED IN ORDER TO KEEP THE FABRIC STRESS WITHIN LIMITS.

DECREASE INFLATION PRESSURE BY DISTRIBUTING WHEEL LOADS THROUGH A DECKING OR ROADWAY SURFACE.

ASSUME DECKING THICKNESS = 2 IN. *



TIRE DISTRIBUTION



TRACK DISTRIBUTION

$$\text{TIRE PRESSURE} = 60 \text{ LBS./UNIT IN}^2 \div 25 \text{ IN}^2 = 2.4 \text{ LBS./IN}^2$$

$$\text{TRACK PRESSURE} = \frac{(346 \text{ LBS./IN.})(2.27 \text{ IN.})}{31 \text{ IN.}} = 301.4 \text{ LBS./IN}$$

$$= \frac{301.4 \text{ LBS./IN.}}{31 \text{ IN.}} = 9.7 \text{ LBS./IN}^2$$

∴ CRITICAL INFLATION PRESSURE IS 10 LBS./IN²

* IT IS ASSUMED THAT THE DECK DOES NOT DISTRIBUTE THE LOCAL LOADING ACROSS THE WIDTH OF THE RAMP

COMPUTERSEARCH

12/19/ '72 10:40

!LOGIN: 1507BRD,C,

!ID* D

!BASIC

>10 FOR D= 20 TO 100 STEP 5

>20 LET S=10*(D/2)

>30 PRINT D,S

>40 NEXT D

>50 END

>RUN

10:42 12/19 FABRIC STRESS (LBS./IN.)

20 CELL DIA. 100

25 (IN.) 125

30 150

35 175

40 200

45 225

50 250

55 275

60 300

65 325

70 350

75 375

80 400

85 425

90 450

95 475

100 500

50 HALT

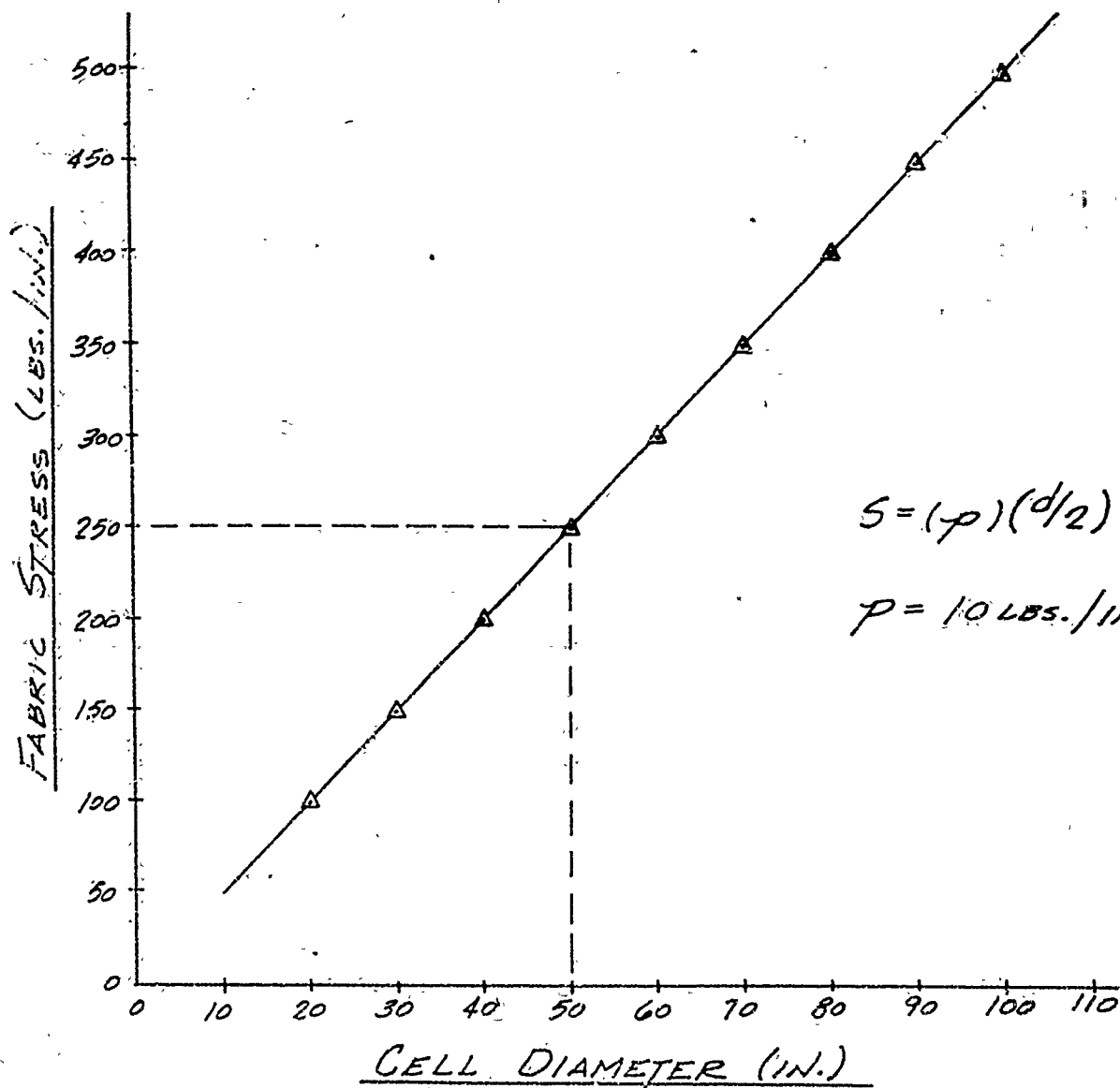
>SYS

!BYE

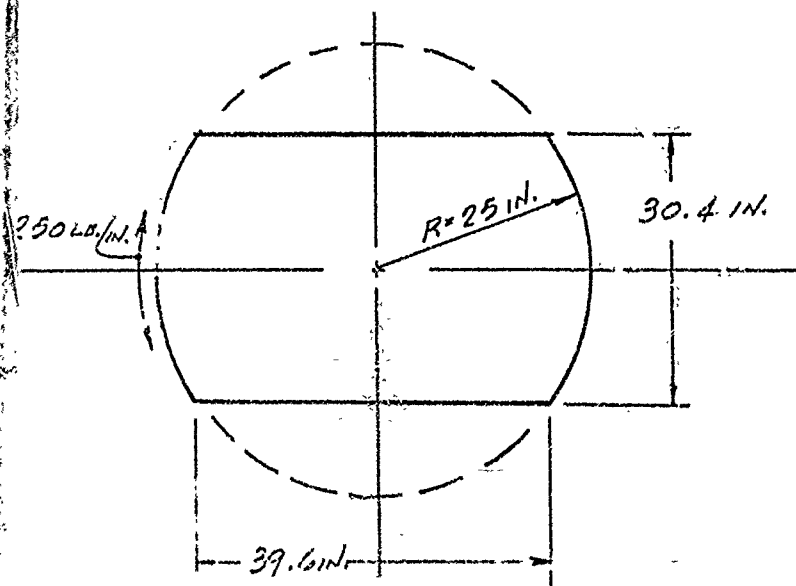
12/19/ '72 10:42

CLT 2

CCU: 0.009

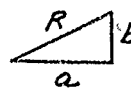


CELL CONFIGURATION:



DUAL WALL ANALYSIS:

RATIO $a/b = 1.3$ OR GREATER



$$a = 1.3b$$

$$R^2 = a^2 + b^2$$

$$R^2 = (1.3b)^2 + b^2$$

$$R^2 = 1.69b^2 + b^2$$

$$R^2 = 2.69b^2$$

$$b = (R^2/2.69)^{1/2}$$

$$b = ((25)^2/2.69)^{1/2}$$

$$b = 15.24 \text{ IN.}$$

$$a = 19.82 \text{ IN.}$$

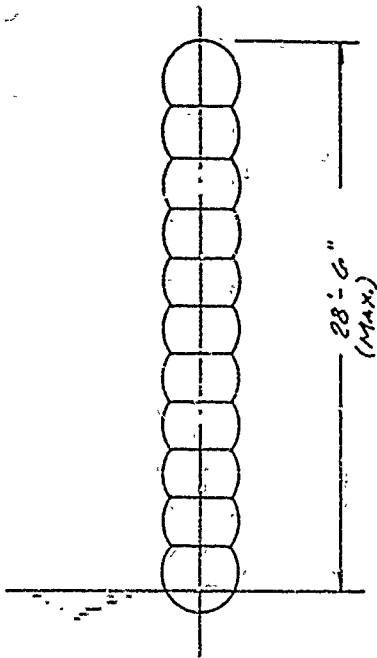
SIZE LIMITATIONS:

MAX. HEIGHT = $23'6" = 342 \text{ IN.}$

MIN. HEIGHT = 50 IN.

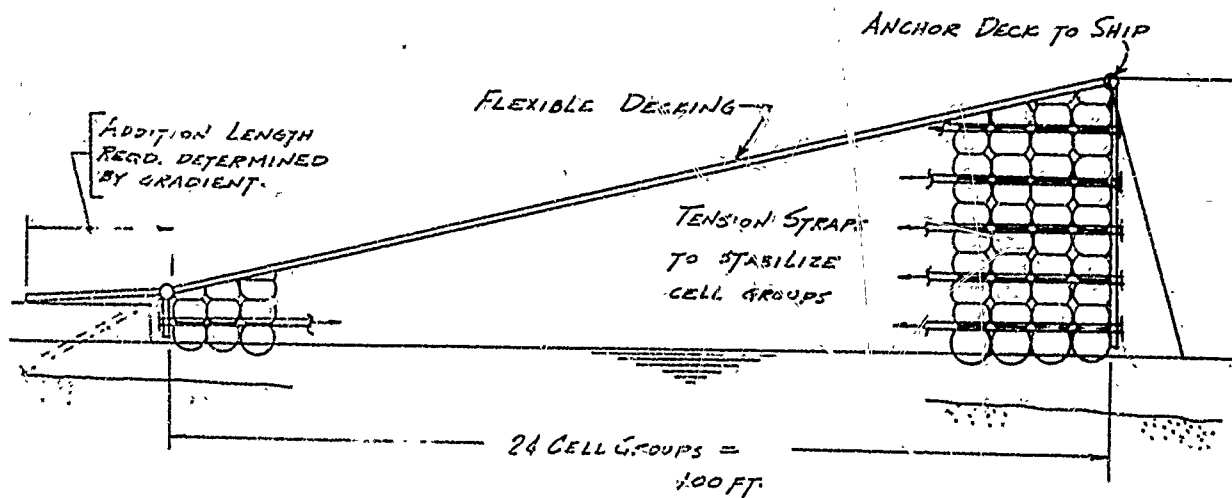
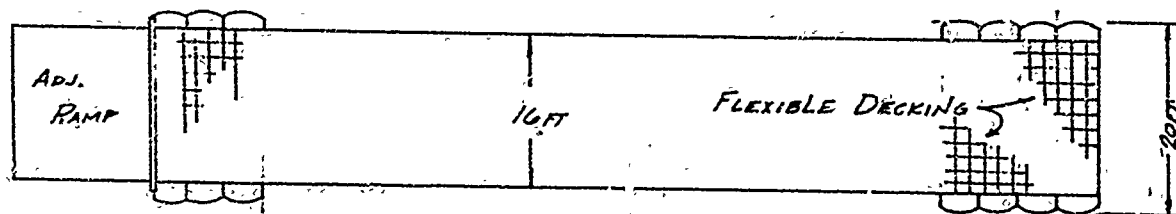
WEB SPACES @ $30.4 = 304 \text{ IN.}$

2 ENDS @ $25 = \frac{50 \text{ IN.}}{354 \text{ IN.}}$



WIDTH OF EACH DUAL WALL PANEL = 20 FT.
($10 \text{ FT. MIN. ROADWAY REQD.}$)

LENGTH OF RAMP
($24 \text{ CELL PANEL(S)})(50 \text{ IN/PANEL}) = 1200 \text{ IN.} = 100 \text{ FT.}$



EFFECTS OF WIND AND WAVES:

WIND:

$$30 \text{ KNOTS} \times 1.15 = 34.5 \text{ M.P.H.}$$

$$\text{IMPACT PRESSURE} = .02 \text{ LBS./IN}^2 \times 144 = 2.88 \text{ #/FT}^2$$

(FROM GRAPH W1.1 IN HANDBOOK)

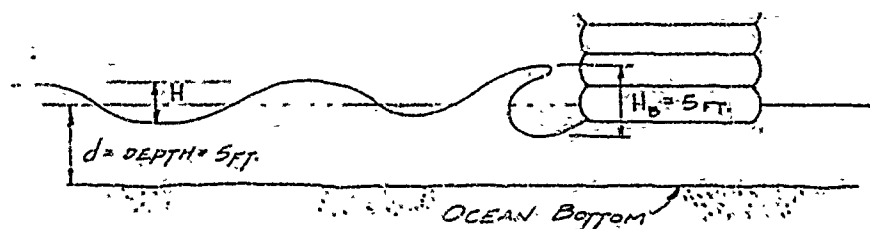
$$\text{APPROX. AREA OF CONTACT} = (1/2)(28.5)(110) = 1570 \text{ FT}^2$$

WAVES:

ASSUMPTIONS:

- 1) 5 FT. BREAKING WAVES
- 2) 5 FT. AVERAGE DEPTH OF WATER
- 3) PERIOD BETWEEN CRESTS IS 10 SEC.

(REF. ENCLOSURE ON DYNAMIC FORCES ON WATERFRONT STRUCTURES)



$$d = 5 \text{ FT.}$$

$$H_b = 1.3 H \quad H = \frac{5}{1.3} = 3.83 \text{ FT.}$$

1) FIG. C

$$L = 130 \text{ FT.}$$

2) FIG. B

$$V = 12.5 \text{ FT./SEC.}$$

3) FIG. D

$$E = 12,230 \text{ FT. LBS./FT.}$$

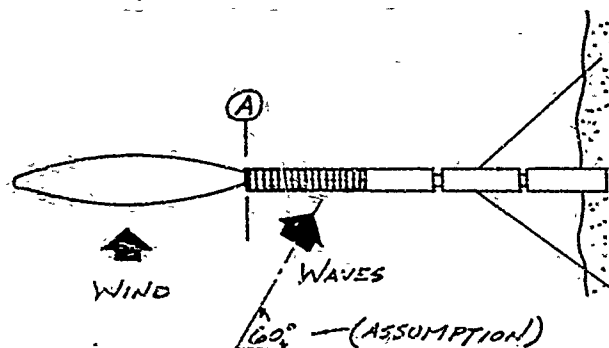
WAVES (CONT.)

$$\therefore F = \frac{KE}{V^2} \quad K = 96.6$$

$$= \frac{(96.6)(12,000)}{(12.5)^2}$$

$$F = 7400 \text{ LBS/LIN. FT.}$$

DYNAMIC FORCE OF WAVES HITTING THE
RAMP BROADSIDE. (90°)



MOMENT AT POINT A WITH SHIP HELD STATIONARY AND
RAMP FREE TO ROTATE AT CAUSEWAY OR BEACH END.

$$M = (2.88)(1570)(110/2) + (7400)(\sin 60^\circ)(110)(55)$$

$$= 165,772 \quad + \quad 38,771,957$$

(WIND) (WAVES)

$$M = 38,937,729 \text{ LB.-FT.}$$

ANCHORING SYSTEM REQD. TO HOLD RAMP IN POSITION

WATERFRONT STRUCTURES—DYNAMIC FORCES

DYNAMIC FORCES ON STRUCTURES DUE TO BREAKING WAVES — SIMPLIFIED METHOD*

EXAMPLE

Observations Required

1. H — maximum wave height, feet.
2. t_1, t_2, t_3 — range of time for two successive crests to pass a given point during periods of maximum waves — seconds.
3. Obtain depths from hydrographic charts.

Formulas

$$d_b = 1.3H \text{ in feet}$$

$$H_b = 1 \text{ to } 2.5H \text{ in feet}$$

$$F = \frac{KE}{V^2} \text{ in lb. per lin. ft.}$$

$$K = 1.5 \times 2g = 96.6$$

Given: 9-ft. waves passing at intervals of 7 to 11 seconds.

Procedure

1. Compute breaking depth of wave $1.3 \times 9 = 11.7$ ft. Waves will break on structure located in 11.7 ft. of water.
2. With values of t and d_b , find length of breaking waves, L , on Fig. C.
3. Using values of t and d_b , find velocity of breaking waves, V , on Fig. B.
4. Using values of L and H , find wave energy, E , from Fig. D.
5. Using previous values, find dynamic wave force, F , lb. per lin. ft. of width of structure.

GIVEN		FIND				
H , ft.	t , sec.	(1) $d_b =$ 1.3H ft.	(2) $L =$ ft, Fig. B.	(3) $V =$ f.p.s., Fig. C.	(4) $E =$ ft./lb. Fig. D.	(5) $F =$ $\frac{KE}{V^2} =$ lb./lin. ft.
9	7	11.7	130	18.3	84,000	24,200
9	9	11.7	170	18.9	93,500	25,400
9	11	11.7	210	18.9	105,000	28,200

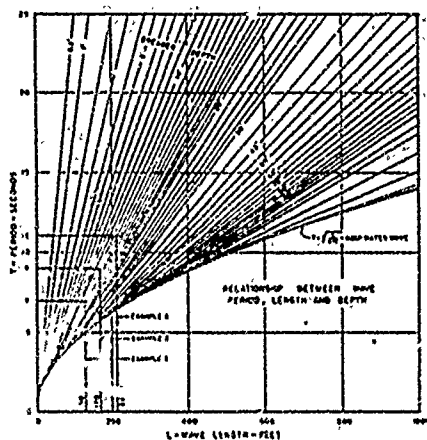


FIG. C

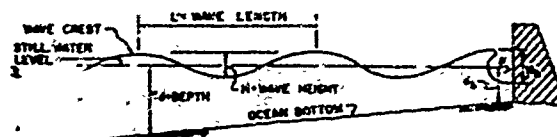


FIG. A

Nomenclature

- d_b = breaker depth L = wave length
 H_b = breaker height E = wave energy per foot of crest, ft.-lb./ft.
 F = dynamic wave force on structure V = velocity of wave, f.p.s.

Wave Forces

1. Breaking on structure:
 - (a) Dynamic — approaches initial force of wave.
 - (b) Hydrostatic — Height of wave.
2. Broken waves:
 - (a) Dynamic — Dissipated force of broken wave.
 - (b) Hydrostatic — Height of wave.
3. Unbroken wave:
 - (a) Hydrostatic — Standing wave.

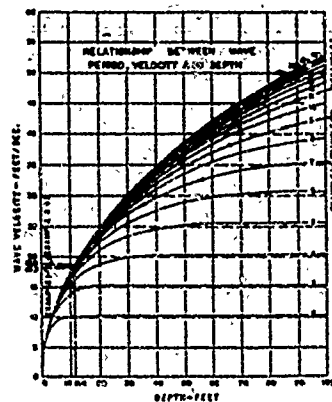


FIG. B

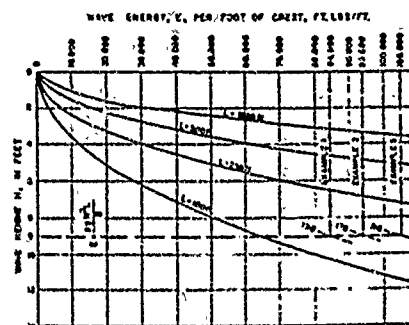
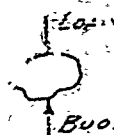


FIG. D

*By the author. For more exact methods of computing wave forces, see Technical Report No. 4, Beach Erosion Board, Office of the Chief of Engineers, Dept. of the Army.

INVESTIGATE BUOYANCY



BUOYANCY WT. OF
WATER DISPLACED

3. $\text{LOAD} = \text{VOL. OF WATER DISPLACED} \times \text{DENSITY OF WATER}$

$$L = V \gamma$$

$$\gamma (\text{SEA WATER}) = 64 \text{ LBS./FT}^3$$

FOR PRELIMINARY DESIGN, NEGLECT WT. OF FABRIC, AND DECK.
ASSUME STRUCTURE FLOATS AT WATER SURFACE.

$$V = L/\gamma$$

$$V = (W)(L')(S)$$

W = WIDTH OF SUBMERGED RAMP

L' = LENGTH OF SUBMERGED RAMP

S = SUBMERGED DEPTH

ASSUME LOAD IS DISTRIBUTED OVER 45° ANGLE SPREAD THROUGH
THE AIR STRUCTURE, (USED TO DETERMINE L') AS LOAD
MOVES ALONG THE RAMP.

THEREFORE, GREATEST SUBMERGENCE OCCURS AT BEACH
OR CAUSEWAY END OF THE RAMP.

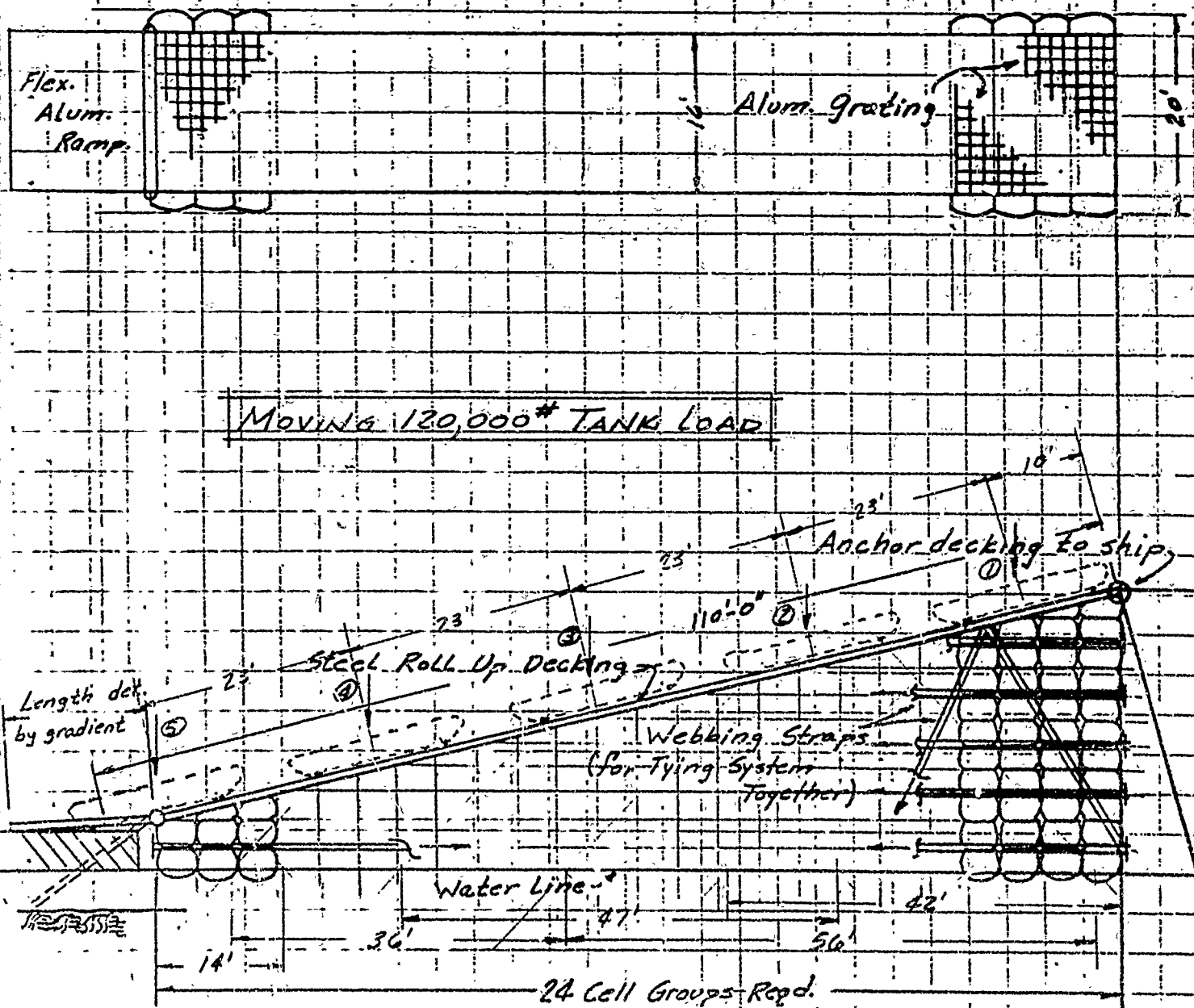
$$V_1 = L/\gamma = 120,000 \text{ LBS.} / 64 \text{ LBS./FT}^3 = 1875 \text{ FT}^3 \text{ (LOAD CONDITION NO. 1)}$$

$$V_2 = 60,000 \text{ LBS.} / 64 \text{ LBS./FT}^3 = 937 \text{ FT}^3 \text{ (LOAD CONDITION NO. 2)}$$

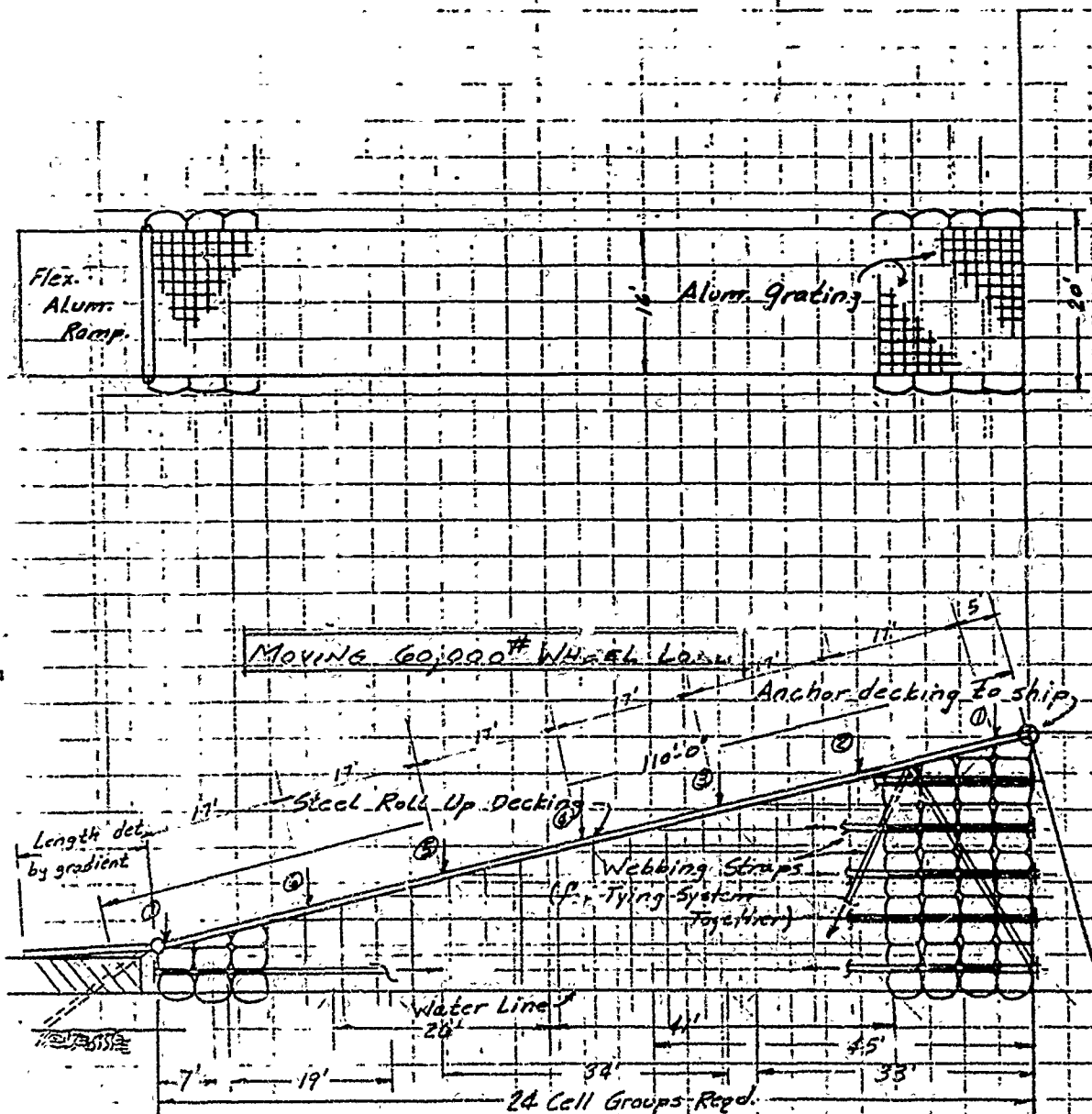
$$S = V/(20)(L')$$

LOAD CONDITION NO. 1 (120,000 LBS.)

<u>LOAD LOCATION</u>	<u>L' (FT.)</u>	<u>S (FT.)</u>
1	42	2.2
2	56	1.7
3	47	2.0
4	36	2.6
5	14	6.7



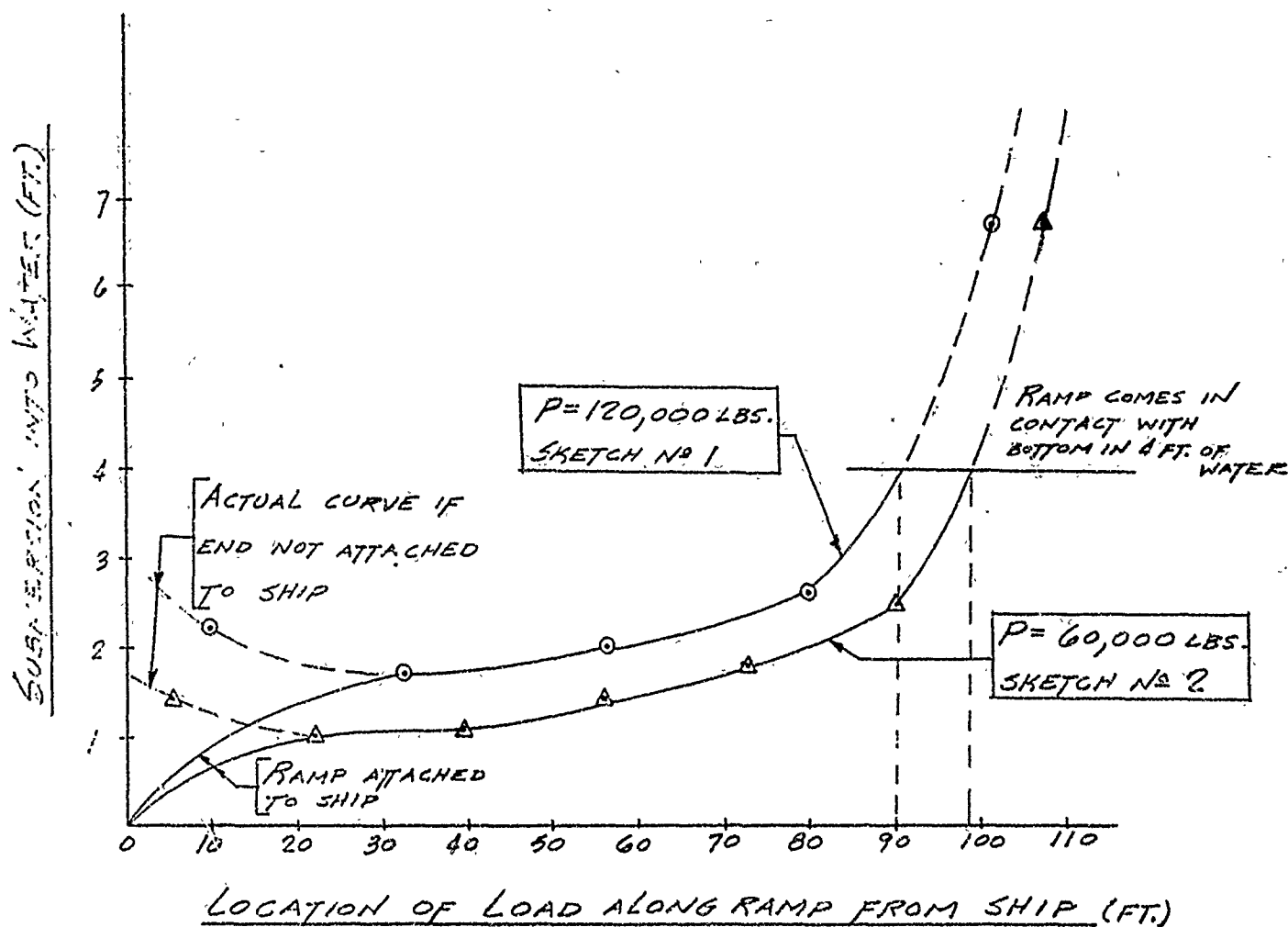
SKETCH No. 1



SKETCH NO. 2

LOAD CONDITION No 2 (60,000 LBS.)

<u>LOAD LOCATION</u>	<u>L' (FT.)</u>	<u>S (FT.)</u>
1	33	1.4
2	45	1.0
3	41	1.1
4	34	1.4
5	26	1.8
6	19	2.5
7	7	6.7



OVERALL DIMENSIONS - 20 FT WIDE X 28'-6" H.

FABRIC STRESS - 250 LBS./IN

INFLATION PRESS. = 10 LBS./IN²

VOL. = $\frac{1}{2}(110)(30)(20) = 33,000 \text{ ft}^3$

SURFACE AREA = $(24)(2)(17)(20) + (2)(\frac{1}{2})(110)(30) = 19,620 \text{ SF}$

CONCEPT № 4

DUAL-WALL TUNNEL

C-29a

DUAL WALL TUNNEL CONCEPT

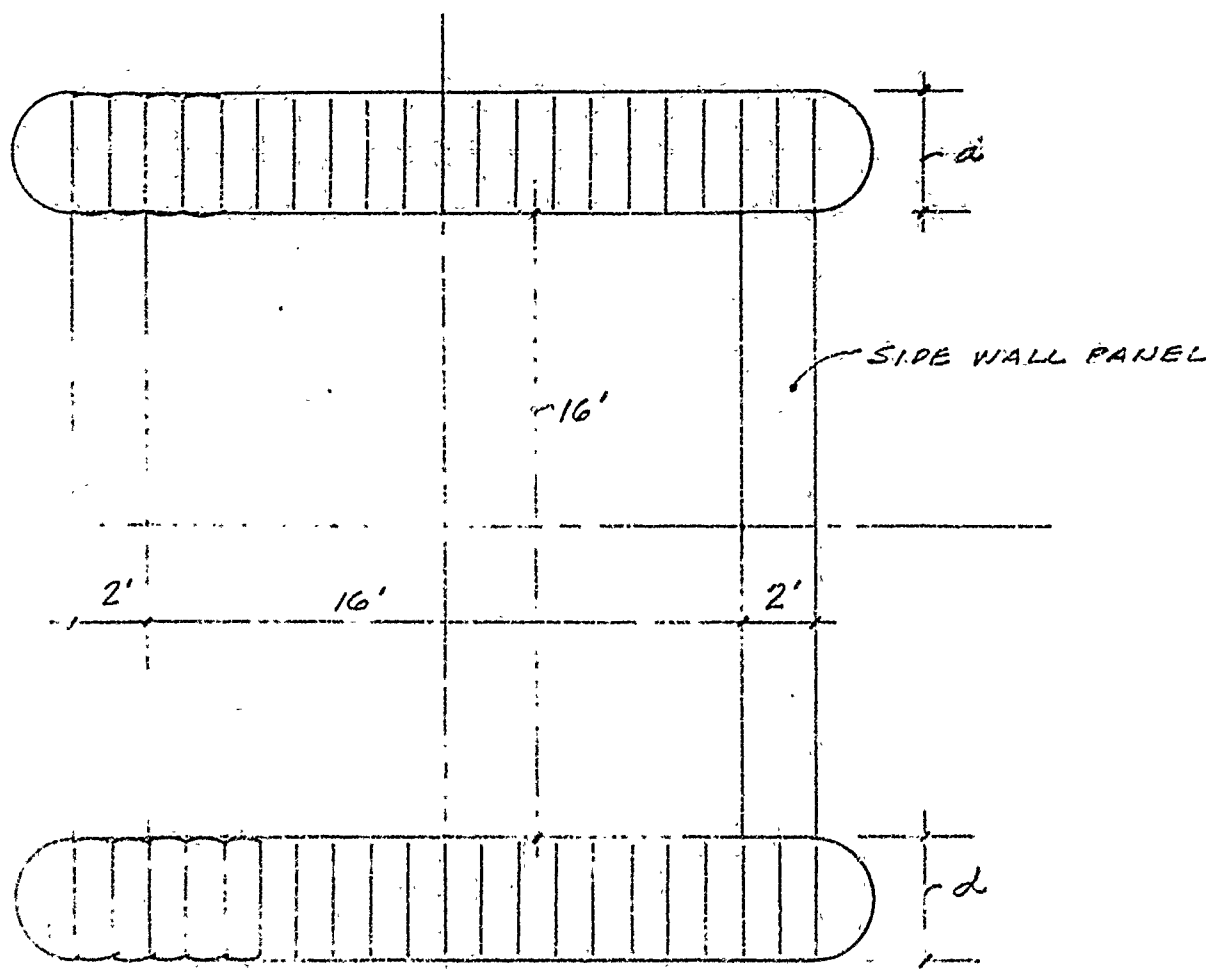
DESIGN DATA:

INSIDE WIDTH - 16 FT.
INSIDE HEIGHT - 16 FT.
LENGTH - 110 FT.
LOAD - 60 TONS

MAXIMUM BENDING MOMENT WITH TANK AT MID SPAN IS

$$M = \frac{PL}{4} = \frac{120000(110)}{4} = 3,300,000 \text{ FT. LBS.}$$

TUNNEL CROSS SECTION:

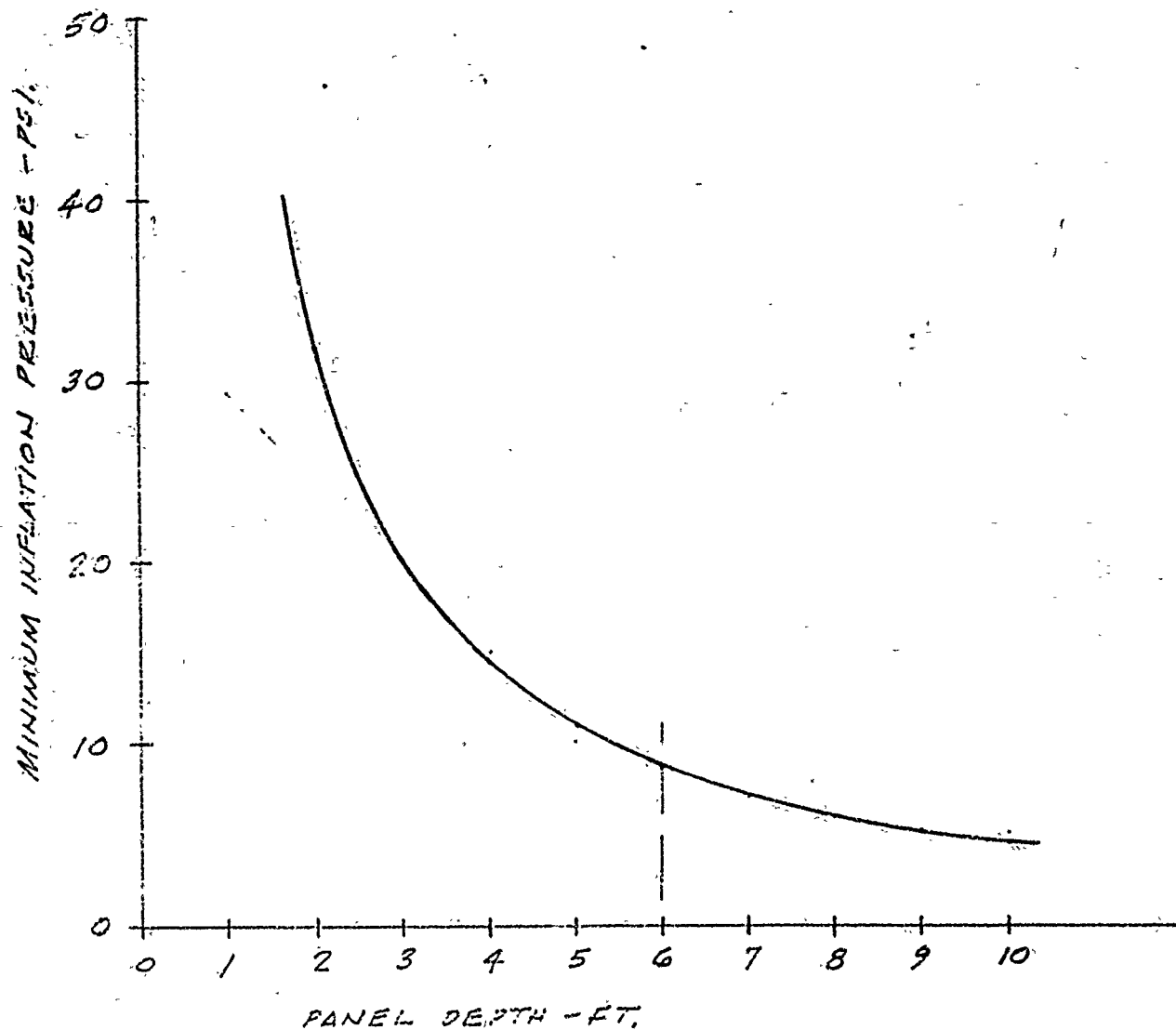


MOMENT CAPABILITY -

$$M = P(20)d(16+d) = 3,300,000$$

$$P = \frac{3,300,000}{20(d)(16+d)} = \frac{165,000}{d(16+d)} \text{ IN PSF.}$$

$$P = \frac{1745.83}{d(16+d)}$$



TRANSVERSE FABRIC STRESS

$$S_T = 12 \frac{P d}{2} = 6 P d$$

LONGITUDINAL STRESS (MAX.)

$$S_{L_M} = 12 P d$$

WEB STRESS

$$S_W = 12 P$$

ZRSEARCH

12/06/ '72 15:40

!LOGIN: 1507BRD,C,

ID= D

!BASIC

>10 FOR D = 1 TO 10

>20 LET P = 1145.83/(D*(16+D))

>30 LET S1 = 6*P*D

>40 LET S2 = 12*P*D

>50 LET S3 = 12*P

>60 PRINT D,P,S1,S2,S3

>70 NEXT D

>80 END

>RUN

15:44 12/06

D

S_T

S_{LM}

S_W

D- 1	67.4218	404.411	808.821	808.821
2	31.8286	381.943	763.887	381.943
3	20.1023	361.841	723.682	241.227
4	14.3229	343.749	687.498	171.874
5	10.9127	327.380	654.760	130.952
6	8.68053	312.499	624.998	104.166
7	7.11696	298.912	597.824	85.4035
8	5.96786	286.457	572.915	71.6144
9	5.09258	274.999	549.998	61.1109
10	4.40704	264.422	528.845	52.8845

80 HALT

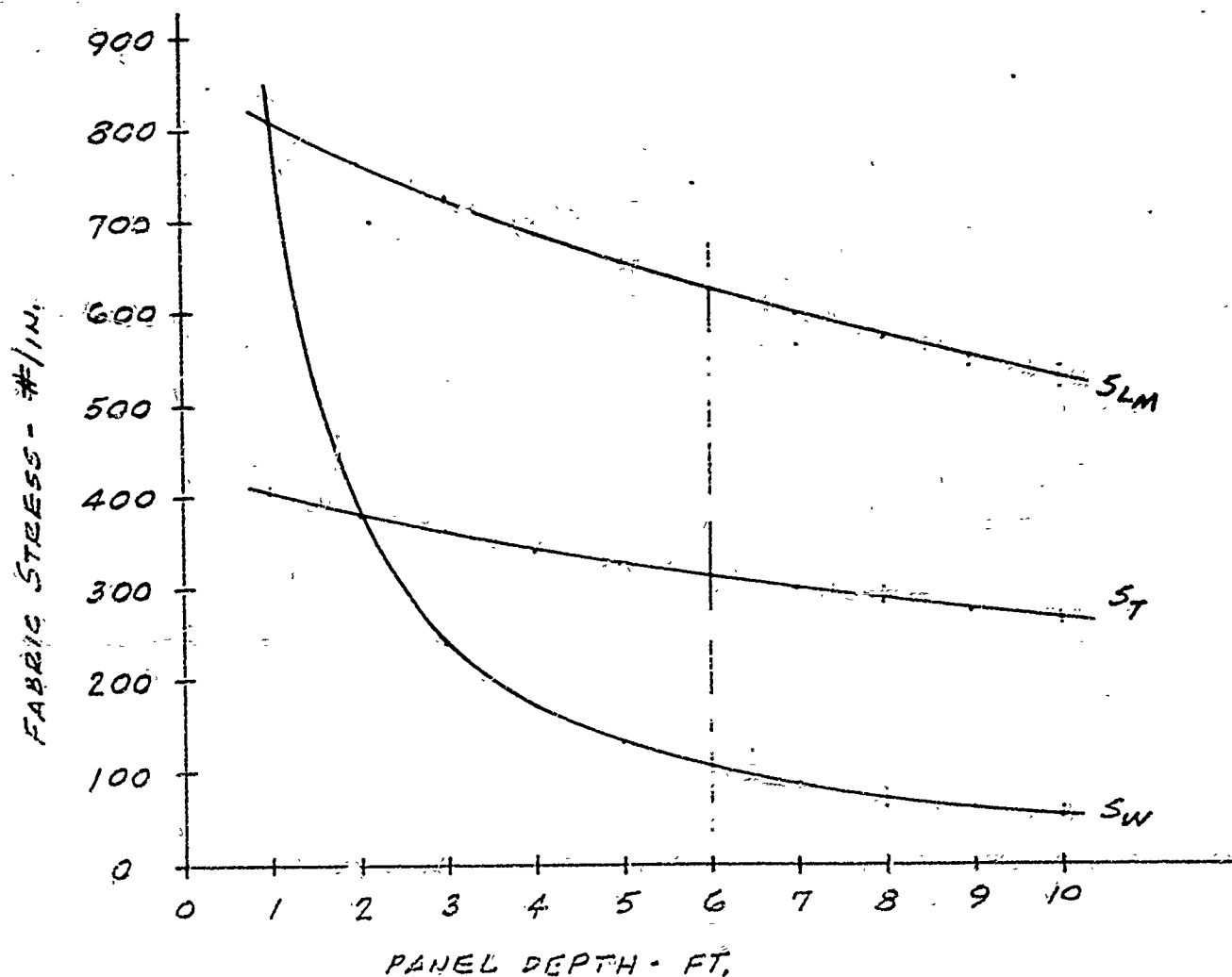
>SYS

!BYE

12/06/ '72 15:45

CLT 5

CCU 0.012



IN CONSIDERATION OF PRESSURE AND STRESSES, AN "OPTIMUM" CELL DEPTH WOULD APPEAR TO BE APPROX. 6 FT. FABRIC COULD BE USED IN THE LOWER PANEL TO REDUCE S_{LM} BELOW S_T THUS S_T IS THE CONTROLLING FACTOR IN DETERMINING FABRIC STRENGTH REQ'TS.

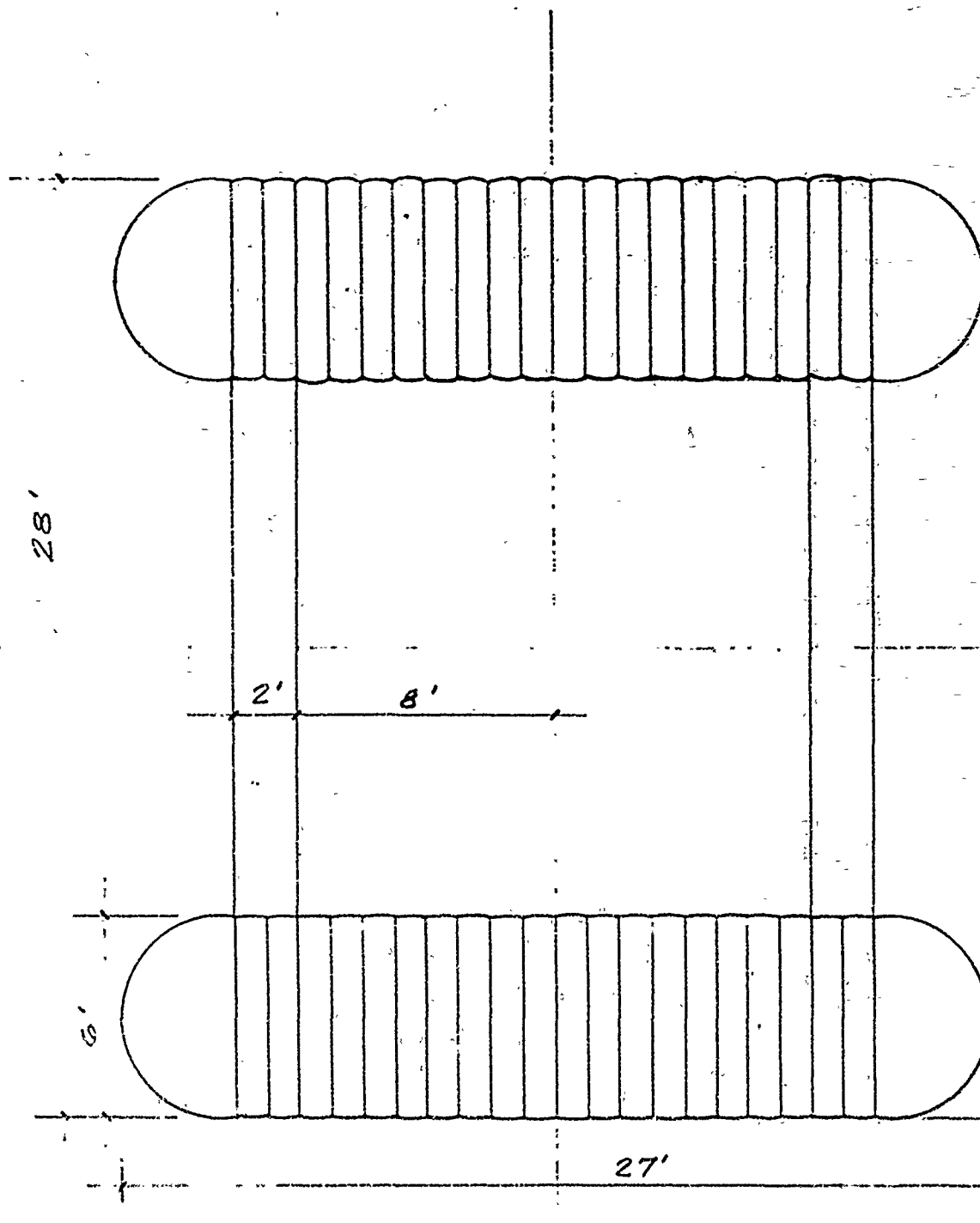
FOR A 6 FT. PANEL DEPTH:

PRESSURE = 8.68 PSI. MIN.

FABRIC STRESS = 312 #/in.

FABRIC STRENGTH (F.S. = 4) = 1250 #/in.

WEB LOAD = 104 #/in.



CROSS SECTION OF RAMP

OVERALL DIMENSIONS - 27 FT. W X 28 FT. HT.

FABRIC STRESS - (NO CABLES) = 624 LBS./IN.

WIND PRESSURE = 8.68 LBS./IN²

$$\text{VOLUME} = [(2)(6) + (\pi)(6)^2/4](110) \times 2 + (2)(2)(6)(110) = 40,980 \text{ FT}^3$$

$$\text{SURFACE AREA} = [42 + (\pi)(6)](110)(2) + (32)(110)(2) = 20,427 \text{ FT}^2$$

CONCEPT № 5

ARCH

WITH

SUSPENDED DECK

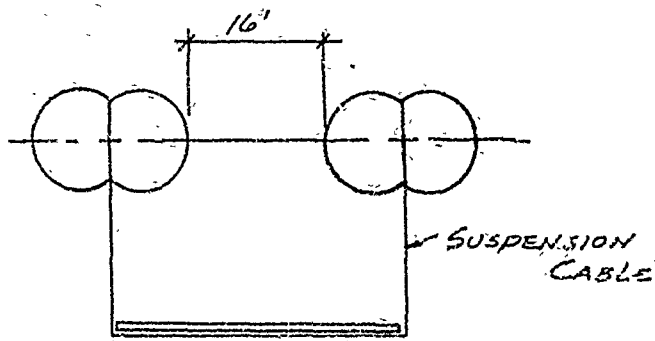
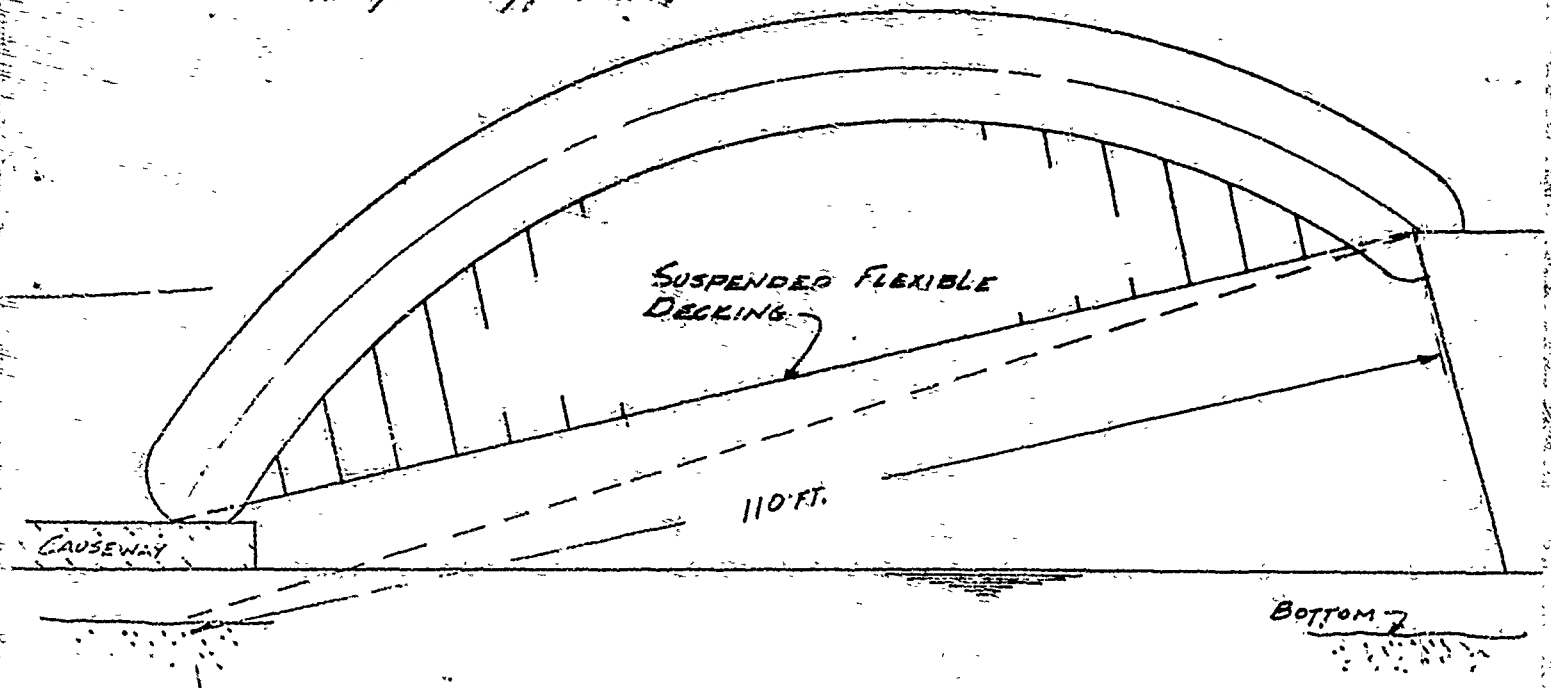
C-34a

INFLATABLE ARCH CONCEPT:

DESIGN DATA:

LENGTH = 110 FT.

WIDTH = 16 FT. (MIN.)



GEOMETRY:

MOST ECONOMICAL RISE TO SPAN RATIO VARIES .25 TO .30

TYPES OF ARCHES:

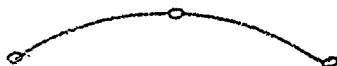
a) NO HINGE



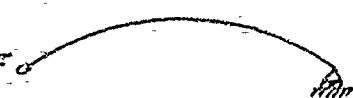
b) TWO HINGE



c) THREE HINGE



d) HINGE & ROLLER



— MOST APPLICABLE
(RESTRAIN ENDS FROM HOR.
MOVEMENT WITH DECK
SYSTEM)

ANALYSIS OF A TWO HINGED PARABOLIC ARCH - REF. TEXT
"FRAMES AND ARCHES" BY LEONTOVICH 1959 MCGRAW HILL

ASSUME HEIGHT TO SPAN RATIO = .25
 FOR $L = 110$ FT. $f = \text{HEIGHT} = 27.5$ FT.

$S (\text{LENGTH OF PARABOLIC ARCH}) = 1.148 (110) = 126$ FT (pg. 451)

CRITICAL LOADING:

ASSUME $\frac{1}{2}$ OF LOAD CARRIED BY EACH ARCH

60 TON TANK - TRACK LENGTH = 14.5 FT. \pm

$120,000 \text{ LBS.} / 14.5 \text{ FT.} = 8275 \text{ LBS./FT.} \div 2 = 4138 \text{ LBS./FT. PER ARCH}$

ASSUME D.L. OF DECK = 362 LBS./FT.

4500 LBS./FT. TOTAL LOAD

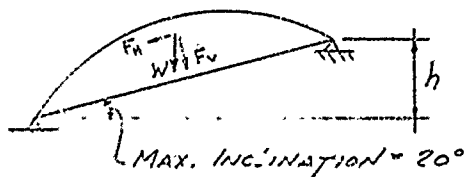
CABLE SPACING:

TRY 5'-0"

LOAD PER CABLE = $(4500 \text{ LBS./FT.})(5 \text{ FT.}) = 22,500 \text{ LBS.}$

$\frac{3}{4}$ " 6X19 IPS CABLE - BREAKING STRENGTH = 46.4 KIPS

F.S. = $\frac{46,000}{22,500} = 2.06$



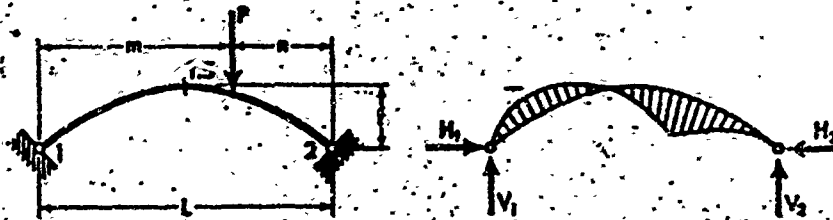
NOTE:

As h GOES TO ZERO, F_v APPROACHES W WHICH CREATES MAX. MOMENT & SHEAR.

As h INCREASES, F_h REACHES A MAX. @ 20° AND MUST BE CARRIED IN THE DECK.

1.111 F.C.R.E. = DESIGN LOAD = 22,500 LBS. PER CABLE -
 3 CABLES LOADED AT ONE TIME
 1/1 TANK MOVING ALONG RAMP

9-12. Vertical Concentrated Load on Arch



$$H_1 = H_2 = \frac{5PL}{8f} \left[1 - 2\left(\frac{m}{L}\right)^2 + \left(\frac{m}{L}\right)^3 \right]$$

$$V_1 = \frac{Pm}{L} \quad V_2 = P - V_1$$

When $x \leq m$ $M_x = \frac{Pnx}{L} - H_1 y$

When $x > m$ $M_x = Pm\left(1 - \frac{x}{L}\right) - H_1 y$

When $x \leq m$ and $\frac{L}{2}$

$$N_x = H_1 \cos \varphi + P \frac{n}{L} \sin \varphi \quad (9-16)$$

$$Q_x = -H_1 \sin \varphi - P \frac{n}{L} \cos \varphi$$

When $x \leq m$, but $\geq \frac{L}{2}$

$$N_x = H_1 \cos \varphi - P \frac{n}{L} \sin \varphi \quad (9-17)$$

$$Q_x = H_1 \sin \varphi + P \frac{n}{L} \cos \varphi$$

When $x \geq m$, but $\leq \frac{L}{2}$

$$N_x = H_1 \cos \varphi - P \frac{m}{L} \sin \varphi \quad (9-18)$$

$$Q_x = -H_1 \sin \varphi - P \frac{m}{L} \cos \varphi$$

For Notations and Constants, see Arts. 9-1 and 9-2

When $x \geq m$ and $\frac{L}{2}$

$$N_x = H_1 \cos \varphi + P \frac{m}{L} \sin \varphi \quad (9-19)$$

$$Q_x = H_1 \sin \varphi - P \frac{m}{L} \cos \varphi$$


```

IMPLICIT REAL(A-H,K-Z),INTEGER(I,J)
OUTPUT(6)*
OUTPUT(6)*1
OUTPUT(6)*
OUTPUT(6)*
OUTPUT(6)*
OUTPUT(6)*
OUTPUT(6)*
OUTPUT(6)*
OUTPUT(6)*
OUTPUT(6)*
OUTPUT(6)*
OUTPUT(6)*
OUTPUT(102)'ENTER DATA IN FORM-P,L,F,SMI,XI'
OUTPUT(102)'P,L,F,SMI,XI'
READ(101,999)P,L,F,SMI,XI
OUTPUT(102)P,L,F,SMI,XI
999 FORMAT(5F)
SM=SMI
2 C1=(SM/L)
H=((5.*P*L*SM)/(8*F*L))*((1-(2*((C1)**2))+((C1)**3))
V2=P*SM/L
V1=P-V2
WRITE(6,1007)
WRITE(6,1005)P,SM
WRITE(6,1008)
WRITE(6,1002)H
WRITE(6,1003)V1
WRITE(6,1004)V2
WRITE(6,1006)
X=0
5 Y=4*I*(1-(X/L))*(X/L)
SN=L-SM
THETA=ATAN((4*F/L)*(1-(2*X/L)))
K1=P*SM/L
K=P*SN/L
IF (X-SM)10,10,20
10 IF (X-(L/2))30,30,40
20 IF (X-(L/2))50,50,60
30 M=(P*SN*X/L)-(H*Y)
N=(H*COS(THETA))+(K*SIN(THETA))
Q=(-H*SIN(THETA))+(K*COS(THETA))
GO TO 70
40 M=(P*SN*X/L)-(H*Y)
N=(H*COS(THETA))-(K*SIN(THETA))
Q=(H*SIN(THETA))+(K*COS(THETA))
GO TO 70
50 M=(P*SM*(1-(X/L)))-(H*Y)
N=(H*COS(THETA))-(K1*SIN(THETA))
Q=(-H*SIN(THETA))-(K1*COS(THETA))
GO TO 70

```

ARCH2H*

WALLACE-PHILLIPS*

NOV.28,1971

THIS PROGRAM ANALYZES A TWO HINGED
PARABOLIC ARCH WITH A CONCENTRATED LOAD
MOVING ACROSS THE ARCH. REF. TEXT "FRAMES
AND ARCHES", BY LEONTOVICH, 1959, MCGRAW-
HILL, PG 135, FOR DIAGRAMS AND EQUATIONS.
SM=SMALL M=LOCATION OF P FROM LT.SUPT.(FT)
X=INCREMENT FROM LT. SUPPORT TO RT.(FT)
M=MOMENT AT INCREMENT X(KIP-FT)
N=AXIAL FORCE IN ARCH (KIPS) AT INCREMENT X
Q=SHEARING FORCE IN ARCH (KIPS) AT INCRMT X

```

GO TO 70
60 M=(P*SM*(1-(X/L)))-(H*Y)
   N=(H*COS(THETA))+(K1*SIN(THETA))
   Q=(H*SIN(THETA))-(K1*COS(THETA))
   GO TO 70
70 WRITE(6,1001)SM,X,M,N,Q
   X=X+XI
   IF (X-L)5,5,80
80 SM=SM+SMI
   TEST=(L/2)+SMI
   IF (SM-TEST)2,2,100
1001 FORMAT(5X,F6.1,5X,F6.1,5X,F8.2,5X,F8.3,5X,F8.3,/)
1002 FORMAT('THE HORIZONTAL REACTION H1=H2=',F8.3,'KIPS'//)
1003 FORMAT('THE SHEAR AT THE LEFT SUPPORT V1=',F8.3,'KIPS'//)
1004 FORMAT('THE SHEAR AT THE RIGHT SUPPORT V2=',F8.3,'KIPS'//)
1005 FORMAT(1H1'WHEN THE LOAD P',F8.3,'IS',F6.1,'FT FROM LT. SUPT.'//)
1006 FORMAT(8X,'SM',10X,'X',9X,'M',14X,'N',12X,'Q',/)
1007 FORMAT(//)
1008 FORMAT('*****')
100 END

```

RCP2H 12/25/72 9:30

1 -	1.000	:						
2 -	2.000	:	1					
3 -	3.000	:						
4 -	4.000	:						
5 -	5.000	:						
6 -	6.000	:						
7 -	7.000	:						
8 -	8.000	:						
9 -	9.000	:						
10 -	10.000	:						
11 -	11.000	:						
12 -	12.000	:						
13 -	13.000	:						
14 -	14.000	:						
15 -	15.000	:						
16 -	16.000	:						
17 -	17.000	:	1	WHEN THE LOAD P	22.500 IS	5.0 FT	FROM LT. SUPT.	
18 -	18.000	:						
19 -	19.000	:						
20 -	20.000	:						
21 -	21.000	:						
22 -	22.000	:						
23 -	23.000	:						
24 -	24.000	:						
25 -	25.000	:						
26 -	26.000	:						
27 -	27.000	:						
28 -	28.000	:						
29 -	29.000	:						
30 -	30.000	:						
31 -	31.000	:						
32 -	32.000	:						
33 -	33.000	:						
34 -	34.000	:						
35 -	35.000	:						
36 -	36.000	:						
37 -	37.000	:						
38 -	38.000	:						
39 -	39.000	:						
40 -	40.000	:						
41 -	41.000	:						
42 -	42.000	:						
43 -	43.000	:						
44 -	44.000	:						
45 -	45.000	:						
46 -	46.000	:						
47 -	47.000	:						
48 -	48.000	:						
49 -	49.000	:						
50 -	50.000	:						
51 -	51.000	:						
52 -	52.000	:						
53 -	53.000	:						
54 -	54.000	:						

RCH2H 12/25/72 9:30

55 -	55.000	:	5.0	110.0	.00	1.077	*2.524
56 -	56.000	:					
57 -	57.000	:					
58 -	58.000	:					
59 -	59.000	:					
60 -	60.000	:	: WHEN THE LOAD P 22.500 IS 10.0 FT FROM LT. SUPT.				
61 -	61.000	:					
62 -	62.000	:					
63 -	63.000	:	: *****				
64 -	64.000	:	: THE HORIZONTAL REACTION H1,H2= 5.033KIPS				
65 -	65.000	:					
66 -	66.000	:					
67 -	67.000	:	: THE SHEAR AT THE LEFT SUPPORT V1= 20.455KIPS				
68 -	68.000	:					
69 -	69.000	:					
70 -	70.000	:	: THE SHEAR AT THE RIGHT SUPPORT V2= 2.045KIPS				
71 -	71.000	:					
72 -	72.000	:					
73 -	73.000	:	SM	X	M	N	Q
74 -	74.000	:					
75 -	75.000	:					
76 -	76.000	:	10.0	.0	.00	18.022	10.905
77 -	77.000	:					
78 -	78.000	:	10.0	10.0	158.79	16.848	12.644
79 -	79.000	:					
80 -	80.000	:	10.0	20.0	101.73	3.148	*4.428
81 -	81.000	:					
82 -	82.000	:	10.0	30.0	53.83	3.735	*3.945
83 -	83.000	:					
84 -	84.000	:	10.0	40.0	15.07	4.317	*3.298
85 -	85.000	:					
86 -	86.000	:	10.0	50.0	-14.54	4.827	*2.493
87 -	87.000	:					
88 -	88.000	:	10.0	60.0	*34.99	4.827	*2.493
89 -	89.000	:					
90 -	90.000	:	10.0	70.0	*46.29	4.317	*3.298
91 -	91.000	:					
92 -	92.000	:	10.0	80.0	*48.45	3.735	*3.945
93 -	93.000	:					
94 -	94.000	:	10.0	90.0	*41.45	3.148	*4.428
95 -	95.000	:					
96 -	96.000	:	10.0	100.0	*25.30	2.600	*4.770
97 -	97.000	:					
98 -	98.000	:	10.0	110.0	.00	2.112	*5.005
99 -	99.000	:					
100 -	100.000	:					
101 -	101.000	:					
102 -	102.000	:					
103 -	103.000	:	: WHEN THE LOAD P 22.500 IS 15.0 FT FROM LT. SUPT.				
104 -	104.000	:					
105 -	105.000	:					
106 -	106.000	:	: *****				
107 -	107.000	:	: THE HORIZONTAL REACTION H1,H2= 7.405KIPS				
108 -	108.000	:					

RCH2H 12/28/72 9:30

109 -	109.000	:					
110 -	110.000	:	THE SHEAR AT THE LEFT SUPPORT V1= 19.432KIPS				
111 -	111.000	:					
112 -	112.000	:					
113 -	113.000	:	THE SHEAR AT THE RIGHT SUPPORT V2= 3.068KIPS				
114 -	114.000	:					
115 -	115.000	:					
116 -	116.000	:	SM	X	H	N	Q
117 -	117.000	:					
118 -	118.000	:					
119 -	119.000	:	15.0	.0	.00	18.976	8.504
120 -	120.000	:					
121 -	121.000	:	15.0	10.0	127.00	18.036	10.351
122 -	122.000	:					
123 -	123.000	:	15.0	20.0	154.97	4.600	-6.564
124 -	124.000	:					
125 -	125.000	:	15.0	30.0	83.90	5.471	-5.857
126 -	126.000	:					
127 -	127.000	:	15.0	40.0	25.29	6.336	-4.908
128 -	128.000	:					
129 -	129.000	:	15.0	50.0	-17.85	7.096	-3.726
130 -	130.000	:					
131 -	131.000	:	15.0	60.0	-48.54	7.096	-3.726
132 -	132.000	:					
133 -	133.000	:	15.0	70.0	-65.75	6.336	-4.908
134 -	134.000	:					
135 -	135.000	:	15.0	80.0	-69.51	5.471	-5.857
136 -	136.000	:					
137 -	137.000	:	15.0	90.0	-59.80	4.600	-6.564
138 -	138.000	:					
139 -	139.000	:	15.0	100.0	-36.63	3.788	-7.064
140 -	140.000	:					
141 -	141.000	:	15.0	110.0	.00	3.066	-7.405
142 -	142.000	:					
143 -	143.000	:					
144 -	144.000	:					
145 -	145.000	:					
146 -	146.000	:	1 WHEN THE LOAD P 22.500 IS 20.0 FT FROM LT. SPT.				
147 -	147.000	:					
148 -	148.000	:					
149 -	149.000	:	*****				
150 -	150.000	:	THE HORIZONTAL REACTION H1=H2= 9.613KIPS				
151 -	151.000	:					
152 -	152.000	:					
153 -	153.000	:	THE SHEAR AT THE LEFT SUPPORT V1= 18.409KIPS				
154 -	154.000	:					
155 -	155.000	:					
156 -	156.000	:	THE SHEAR AT THE RIGHT SUPPORT V2= 4.091KIPS				
157 -	157.000	:					
158 -	158.000	:					
159 -	159.000	:	SM	X	H	N	Q
160 -	160.000	:					
161 -	161.000	:					
162 -	162.000	:	20.0	.0	.00	19.814	6.220

RCP24 12/25/72 2:30

163	163.000					
164	164.000	20.0	10.0	36.70	19.097	8.161
165	165.000					
166	166.000	20.0	20.0	210.89	27.593	10.376
167	167.000					
168	168.000	20.0	30.0	117.50	7.058	7.702
169	169.000					
170	170.000	20.0	50.0	41.68	8.197	6.476
171	171.000					
172	172.000	20.0	50.0	-26.71	9.203	4.944
173	173.000					
174	174.000	20.0	40.0	-57.62	9.203	4.944
175	175.000					
176	176.000	20.0	70.0	-81.05	8.197	6.476
177	177.000					
178	178.000	20.0	80.0	-57.00	7.058	7.702
179	179.000					
180	180.000	20.0	90.0	-75.48	5.913	5.412
181	181.000					
182	182.000	20.0	100.0	-46.48	4.849	5.251
183	183.000					
184	184.000	20.0	110.0	.00	3.904	9.690
185	185.000					
186	186.000					
187	187.000					
188	188.000					
189	189.000	WHEN THE LOAD p 22.500 IS 25.0 FT FROM LT. SUPP.				
190	190.000					
191	191.000					
192	192.000	***** THE HORIZONTAL REACTION H1, H2 = 11.613 kips *****				
193	193.000					
194	194.000					
195	195.000					
196	196.000	THE SHEAR AT THE LEFT SUPPORT V1 = 17.386 kips				
197	197.000					
198	198.000					
199	199.000	THE SHEAR AT THE RIGHT SUPPORT V2 = 5.114 kips				
200	200.000					
201	201.000					
202	202.000	SM	X	M	N	Q
203	203.000					
204	204.000					
205	205.000	25.0	.0	.00	20.506	4.082
206	206.000					
207	207.000	25.0	10.0	58.29	19.998	6.102
208	208.000					
209	209.000	25.0	20.0	157.69	19.132	8.433
210	210.000					
211	211.000	25.0	30.0	155.71	8.457	9.461
212	212.000					
213	213.000	25.0	40.0	62.34	9.859	7.989
214	214.000					
215	215.000	25.0	50.0	-9.31	11.103	6.144
216	216.000					

C-43

RLH2H 12/28/72 9130

217	217.000	25.0	60.0	-61.05	11.103	-6.144
218	218.000					
219	219.000	25.0	70.0	-91.07	9.859	-7.289
220	220.000					
221	221.000	25.0	80.0	-99.98	8.457	-9.461
222	222.000					
223	223.000	25.0	90.0	-87.77	7.052	-10.549
224	224.000					
225	225.000	25.0	100.0	-54.44	5.750	-11.312
226	226.000					
227	227.000	25.0	110.0	.00	4.596	-11.828
228	228.000					
229	229.000					
230	230.000					
231	231.000					
232	232.000	1 WHEN THE LOAD P 22.500 IS 30.0 FT FROM LT. SPT.				
233	233.000					
234	234.000					
235	235.000	*****				
236	236.000	THE HORIZONTAL REACTION H1-H2= 13.370 KIPS				
237	237.000					
238	238.000					
239	239.000	THE SHEAR AT THE LEFT SUPPORT V1= 16.364 KIPS				
240	240.000					
241	241.000					
242	242.000	THE SHEAR AT THE RIGHT SUPPORT V2= 6.136 KIPS				
243	243.000					
244	244.000					
245	245.000	SM	X	M	N	Q
246	246.000					
247	247.000					
248	248.000	30.0	.0	.00	21.025	-2.117
249	249.000					
250	250.000	30.0	10.0	-42.09	20.710	-5.198
251	251.000					
252	252.000	30.0	20.0	-108.49	20.065	-6.627
253	253.000					
254	254.000	30.0	30.0	-199.20	18.945	-9.364
255	255.000					
256	256.000	30.0	40.0	-89.22	11.284	-9.438
257	257.000					
258	258.000	30.0	50.0	-3.55	12.760	-7.322
259	259.000					
260	260.000	30.0	60.0	-57.82	12.760	-7.322
261	261.000					
262	262.000	30.0	70.0	-94.87	11.284	-9.438
263	263.000					
264	264.000	30.0	80.0	-107.62	9.632	-11.119
265	265.000					
266	266.000	30.0	90.0	-96.05	7.985	-12.355
267	267.000					
268	268.000	30.0	100.0	-50.18	6.462	-13.216
269	269.000					
270	270.000	30.0	110.0	.00	5.115	-13.793

C-44

RCF2H 12/28/72 9:30

271 -	271.000	:				
272 -	272.000	:				
273 -	273.000	:				
274 -	274.000	:				
275 -	275.000	:	1 WHEN THE LOAD P 22.500 IS 35.0 FT FROM LT. SUPT.			
276 -	276.000	:				
277 -	277.000	:				
278 -	278.000	:	*****			
279 -	279.000	:	THE HORIZONTAL REACTION H1=H2= 14.850 KIPS			
280 -	280.000	:				
281 -	281.000	:				
282 -	282.000	:	THE SHEAR AT THE LEFT SUPPORT V1= 15.341 KIPS			
283 -	283.000	:				
284 -	284.000	:				
285 -	285.000	:	THE SHEAR AT THE RIGHT SUPPORT V2= 7.159 KIPS			
286 -	286.000	:				
287 -	287.000	:				
288 -	288.000	:	SM	X	M	N
289 -	289.000	:				Q
290 -	290.000	:				
291 -	291.000	:	35.0	0.0	0.00	21.348
292 -	292.000	:				0.347
293 -	293.000	:	35.0	10.0	18.41	21.208
294 -	294.000	:				2.469
295 -	295.000	:	35.0	20.0	63.81	20.765
296 -	296.000	:				4.970
297 -	297.000	:	35.0	30.0	136.22	19.867
298 -	298.000	:				7.821
299 -	299.000	:	35.0	40.0	123.13	12.443
300 -	300.000	:				-10.814
301 -	301.000	:	35.0	50.0	24.54	14.141
302 -	302.000	:				-8.474
303 -	303.000	:	35.0	60.0	-47.05	14.141
304 -	304.000	:				-8.474
305 -	305.000	:	35.0	70.0	-91.64	12.443
306 -	306.000	:				-10.814
307 -	307.000	:	35.0	80.0	-109.23	10.557
308 -	308.000	:				-12.662
309 -	309.000	:	35.0	90.0	-99.82	8.685
310 -	310.000	:				-14.013
311 -	311.000	:	35.0	100.0	-63.41	6.960
312 -	312.000	:				-14.945
313 -	313.000	:	35.0	110.0	0.00	5.439
314 -	314.000	:				-15.563
315 -	315.000	:				
316 -	316.000	:				
317 -	317.000	:				
318 -	318.000	:	1 WHEN THE LOAD P 22.500 IS 40.0 FT FROM LT. SUPT.			
319 -	319.000	:				
320 -	320.000	:				
321 -	321.000	:	*****			
322 -	322.000	:	THE HORIZONTAL REACTION H1=H2= 16.029 KIPS			
323 -	323.000	:				
324 -	324.000	:				

FLR2H 12/28/72 9:30

325 -	325.000	: THE SHEAR AT THE LEFT SUPPORT V1= 14.318KIPS				
326 -	326.000					
327 -	327.000					
328 -	328.000	: THE SHEAR AT THE RIGHT SUPPORT V2= 8.182KIPS				
329 -	329.000					
330 -	330.000					
331 -	331.000	SH	X	M	N	Q
332 -	332.000					
333 -	333.000					
334 -	334.000	40.0	0.0	0.00	21.458	-1.209
335 -	335.000					
336 -	336.000	40.0	10.0	-2.53	21.472	.932
337 -	337.000					
338 -	338.000	40.0	20.0	24.08	21.210	3.474
339 -	339.000					
340 -	340.000	40.0	30.0	79.83	20.517	6.402
341 -	341.000					
342 -	342.000	40.0	40.0	164.73	19.231	9.596
343 -	343.000					
344 -	344.000	40.0	50.0	53.77	15.222	-9.599
345 -	345.000					
346 -	346.000	40.0	60.0	-28.05	15.222	-9.599
347 -	347.000					
348 -	348.000	40.0	70.0	-80.73	13.311	-12.111
349 -	349.000					
350 -	350.000	40.0	80.0	-104.26	11.206	-14.081
351 -	351.000					
352 -	352.000	40.0	90.0	-98.65	9.130	-15.528
353 -	353.000					
354 -	354.000	40.0	100.0	-63.90	7.224	-16.432
355 -	355.000					
356 -	356.000	40.0	110.0	0.00	5.549	-17.119
357 -	357.000					
358 -	358.000					
359 -	359.000					
360 -	360.000					
361 -	361.000	: WHEN THE LOAD P 22.500IS 45.0FT FROM LT. SUPT.				
362 -	362.000					
363 -	363.000					
364 -	364.000	*****				
365 -	365.000	: THE HORIZONTAL REACTION H1=H2= 16.885KIPS				
366 -	366.000					
367 -	367.000					
368 -	368.000	: THE SHEAR AT THE LEFT SUPPORT V1= 13.295KIPS				
369 -	369.000					
370 -	370.000					
371 -	371.000	: THE SHEAR AT THE RIGHT SUPPORT V2= 9.205KIPS				
372 -	372.000					
373 -	373.000					
374 -	374.000	SH	X	M	N	Q
375 -	375.000					
376 -	376.000					
377 -	377.000	45.0	0.0	0.00	21.341	-2.538
378 -	378.000					

RCF2H 12/28/72 9:30

379	-	379.000	:	45.0	10.0	-20.54	21.487	-4.402
380	-	380.000	:					
381	-	381.000	:	45.0	20.0	-10.38	21.383	2.152
382	-	382.000	:					
383	-	383.000	:	45.0	30.0	10.47	20.873	5.117
384	-	384.000	:					
385	-	385.000	:	45.0	40.0	102.03	19.788	8.384
386	-	386.000	:					
387	-	387.000	:	45.0	50.0	91.78	15.982	-10.695
388	-	388.000	:					
389	-	389.000	:	45.0	60.0	-0.26	15.982	-10.695
390	-	390.000	:					
391	-	391.000	:	45.0	70.0	-61.61	13.868	-13.323
392	-	392.000	:					
393	-	393.000	:	45.0	80.0	-92.26	11.562	-15.366
394	-	394.000	:					
395	-	395.000	:	45.0	90.0	-32.20	9.303	-16.830
396	-	396.000	:					
397	-	397.000	:	45.0	100.0	-61.45	7.239	-17.816
398	-	398.000	:					
399	-	399.000	:	45.0	110.0	-0.00	5.431	-18.448
400	-	400.000	:					
401	-	401.000	:					
402	-	402.000	:					
403	-	403.000	:					
404	-	404.000	:	WHEN THE LOAD P 22.500 IS 50.0 FT FROM LT. SUPP.				
405	-	405.000	:					
406	-	406.000	:					
407	-	407.000	:	*****				
408	-	408.000	:	THE HORIZONTAL REACTION H1=H2= 17.404 KIPS				
409	-	409.000	:					
410	-	410.000	:					
411	-	411.000	:	THE SHEAR AT THE LEFT SUPPORT V1= 12.273 KIPS				
412	-	412.000	:					
413	-	413.000	:					
414	-	414.000	:	THE SHEAR AT THE RIGHT SUPPORT V2= 10.227 KIPS				
415	-	415.000	:					
416	-	416.000	:					
417	-	417.000	:	SM	X	M	N	O
418	-	418.000	:					
419	-	419.000	:					
420	-	420.000	:	50.0	0.0	0.00	20.985	-3.628
421	-	421.000	:					
422	-	422.000	:	50.0	10.0	-35.49	21.792	-1.522
423	-	423.000	:					
424	-	424.000	:	50.0	20.0	-39.34	21.277	1.010
425	-	425.000	:					
426	-	426.000	:	50.0	30.0	-11.54	20.923	3.971
427	-	427.000	:					
428	-	428.000	:	50.0	40.0	-47.90	20.020	7.261
429	-	429.000	:					
430	-	430.000	:	50.0	50.0	138.98	18.444	10.647
431	-	431.000	:					
432	-	432.000	:	50.0	60.0	36.71	16.407	-11.761

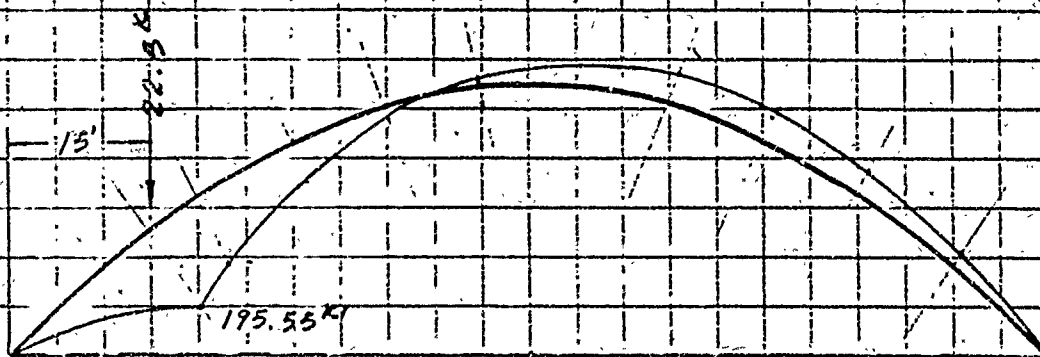
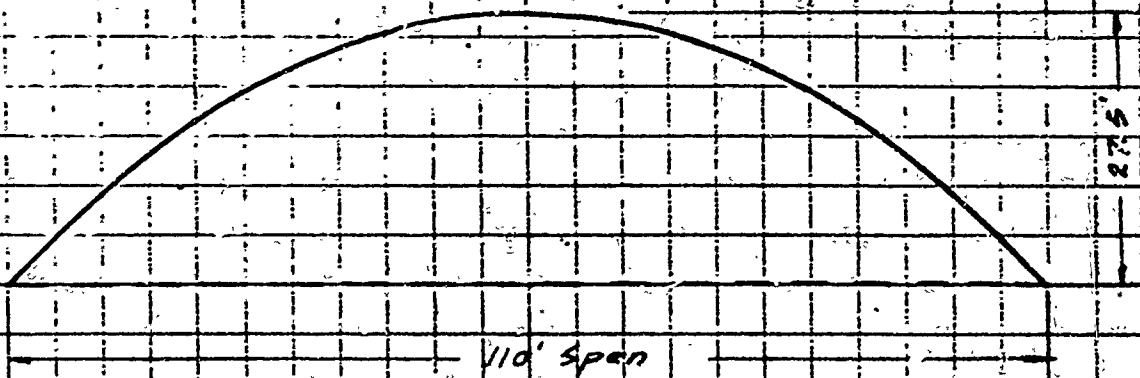
RCF-24 12/28/72 9:30

433 -	433.000	:					
434 -	434.000	:	50.0	70.0	-39.92	14.100	-14.546
435 -	435.000	:					
436 -	436.000	:	50.0	80.0	-72.91	11.612	-16.512
437 -	437.000	:					
438 -	438.000	:	50.0	90.0	-80.25	9.192	-17.972
439 -	439.000	:					
440 -	440.000	:	50.0	100.0	-55.95	6.994	-18.936
441 -	441.000	:					
442 -	442.000	:	50.0	110.0	.00	5.075	-19.538
443 -	443.000	:					
444 -	444.000	:					
445 -	445.000	:					
446 -	446.000	:					
447 -	447.000	:	: WHEN THE LOAD P 22.500 IS 55.0 FT FROM LT. SUPT.				
448 -	448.000	:					
449 -	449.000	:					
450 -	450.000	:	: *****				
451 -	451.000	:	: THE HORIZONTAL REACTION H1=H2= 17.578KIPS				
452 -	452.000	:					
453 -	453.000	:					
454 -	454.000	:	: THE SHEAR AT THE LEFT SUPPORT V1= 11.250KIPS				
455 -	455.000	:					
456 -	456.000	:					
457 -	457.000	:	: THE SHEAR AT THE RIGHT SUPPORT V2= 11.250KIPS				
458 -	458.000	:					
459 -	459.000	:					
460 -	460.000	:	SM	X	M	N	Q
461 -	461.000	:					
462 -	462.000	:					
463 -	463.000	:	55.0	.0	.00	20.385	-4.475
464 -	464.000	:					
465 -	465.000	:	55.0	10.0	-47.30	20.729	-2.424
466 -	466.000	:					
467 -	467.000	:	55.0	20.0	-62.64	20.870	.054
468 -	468.000	:					
469 -	469.000	:	55.0	30.0	-46.02	20.658	2.968
470 -	470.000	:					
471 -	471.000	:	55.0	40.0	2.56	19.919	6.228
472 -	472.000	:					
473 -	473.000	:	55.0	50.0	83.10	18.524	9.612
474 -	474.000	:					
475 -	475.000	:	55.0	60.0	83.10	16.487	-12.795
476 -	476.000	:					
477 -	477.000	:	55.0	70.0	2.56	13.999	-15.479
478 -	478.000	:					
479 -	479.000	:	55.0	80.0	-46.02	11.347	-17.515
480 -	480.000	:					
481 -	481.000	:	55.0	90.0	-62.64	8.790	-18.928
482 -	482.000	:					
483 -	483.000	:	55.0	100.0	-47.30	6.481	-19.838
484 -	484.000	:					
485 -	485.000	:	55.0	110.0	.00	4.475	-20.385
486 -	486.000	:					

C-48

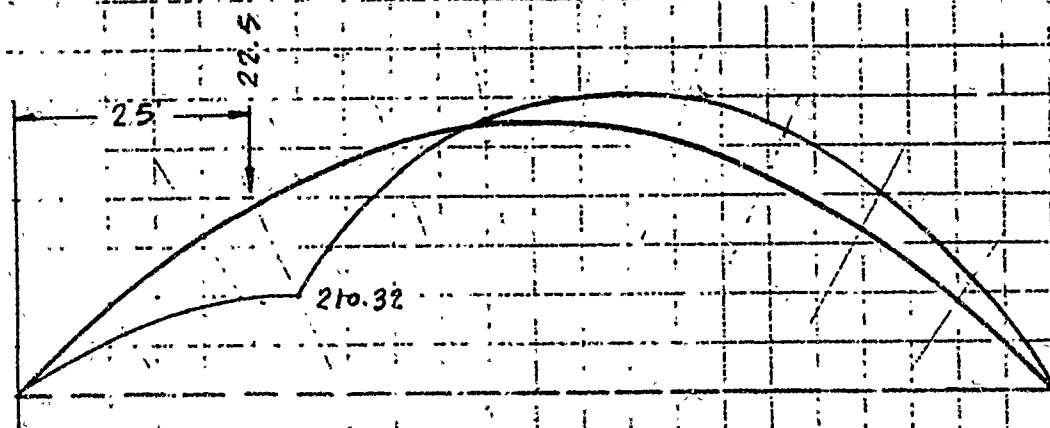
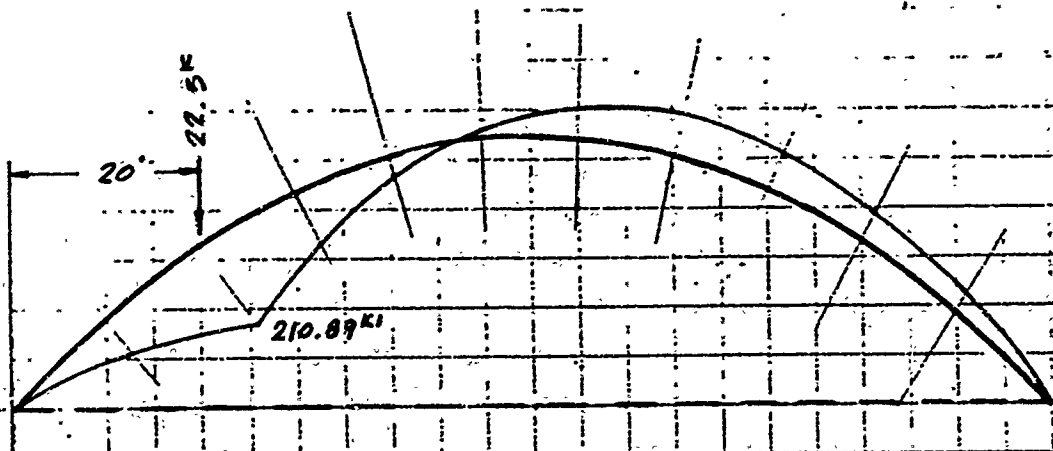
RCH2H 12/28/72 9:30

487 -	487.000	:					
488 -	488.000	:					
489 -	489.000	:					
490 -	490.000	:	: WHEN THE LOAD P 22.500 IS 60.0 FT FROM LT. SUPP.				
491 -	491.000	:					
492 -	492.000	:					
493 -	493.000	:	: *****				
494 -	494.000	:	: THE HORIZONTAL REACTION H1, H2= 17.404 KIPS				
495 -	495.000	:					
496 -	496.000	:					
497 -	497.000	:	: THE SHEAR AT THE LEFT SUPPORT V1= 10.227 KIPS				
498 -	498.000	:					
499 -	499.000	:					
500 -	500.000	:	: THE SHEAR AT THE RIGHT SUPPORT V2= 12.273 KIPS				
501 -	501.000	:					
502 -	502.000	:					
503 -	503.000	:	SM	X	M	N	Q
504 -	504.000	:					
505 -	505.000	:					
506 -	506.000	:	60.0	0	0.00	19.538	5.075
507 -	507.000	:					
508 -	508.000	:	60.0	10.0	-55.95	19.946	3.105
509 -	509.000	:					
510 -	510.000	:	60.0	20.0	-80.25	20.174	0.715
511 -	511.000	:					
512 -	512.000	:	60.0	30.0	-72.91	20.076	2.109
513 -	513.000	:					
514 -	514.000	:	60.0	40.0	-33.92	19.482	5.288
515 -	515.000	:					
516 -	516.000	:	60.0	50.0	36.71	18.258	8.610
517 -	517.000	:					
518 -	518.000	:	60.0	60.0	138.98	18.258	8.610
519 -	519.000	:					
520 -	520.000	:	60.0	70.0	47.90	13.562	-16.420
521 -	521.000	:					
522 -	522.000	:	60.0	80.0	-11.54	10.766	-18.374
523 -	523.000	:					
524 -	524.000	:	60.0	90.0	-39.34	8.094	-19.698
525 -	525.000	:					
526 -	526.000	:	60.0	100.0	-35.49	5.698	-20.519
527 -	527.000	:					
528 -	528.000	:	60.0	110.0	0.00	3.628	-20.985
529 -	529.000	:					



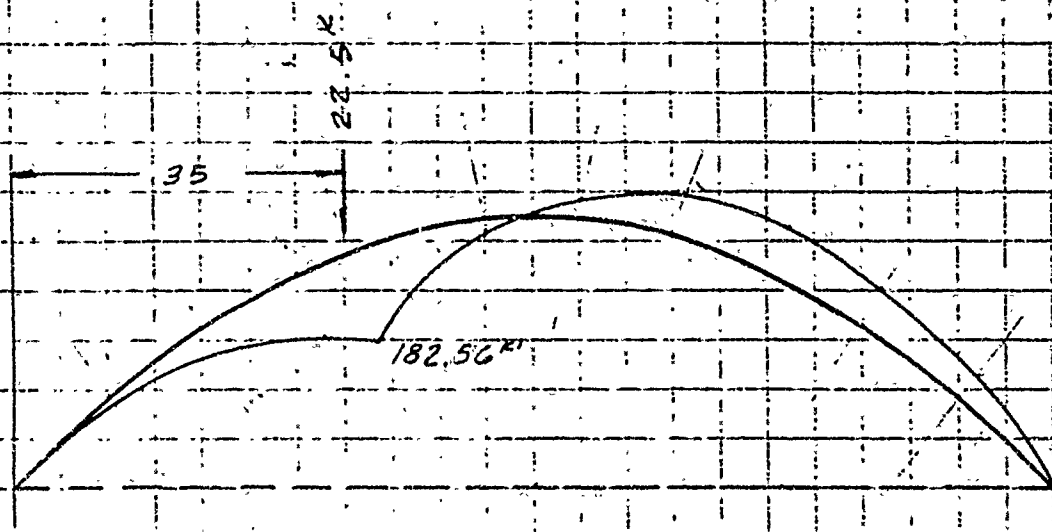
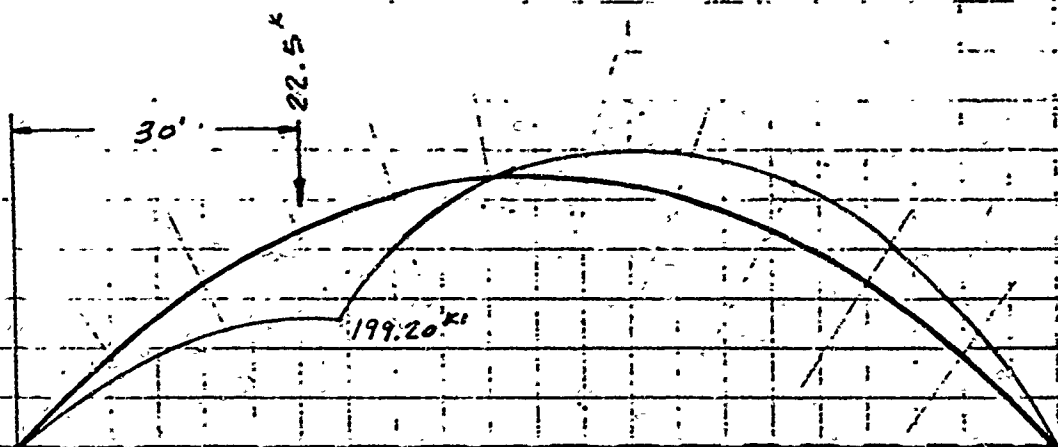
Compute M @ Load $M = \frac{(22.5)(95)(15)}{110} - (7.405)(12.955) = 195.55 \text{ k}$

$y = (4)(27.5)\left(1 - \frac{15}{110}\right)\left(\frac{15}{110}\right) = 12.955$



Compute M @ Load $M = \frac{(22.5)(85)(25)}{110} - (11.613)(19.3182) = 210.32 \text{ k'}$

$y = 4(27.5)\left(1 - \frac{25}{110}\right)\frac{25}{110} = 19.3182$



Compute M @ Load $M = \frac{(22.5)(15)(35)}{110} - (14.850)(23.864) = 182.557 \text{ K'}$

$y = 4(22.5)\left(1 - \frac{35}{110}\right)\left(\frac{35}{110}\right) = 23.864$

SUMMATION OF MOMENTS FOR CRITICAL LOADING:

$$\begin{aligned} x=10 \\ m=20 \quad M=97.70 \\ m=25 \quad M=62.29 \\ m=30 \quad M=42.09 \\ \hline 208.08 \end{aligned}$$

$$\begin{aligned} x=20 \\ M=210.89 \\ M=157.69 \\ M=108.49 \\ \hline 477.07 \end{aligned}$$

$$\begin{aligned} x=30 \\ M=117.54 \\ M=155.71 \\ M=199.20 \\ \hline 472.45 \end{aligned}$$

$$\begin{aligned} x=40 \\ m=20 \quad M=41.68 \\ m=25 \quad M=62.34 \\ m=30 \quad M=89.22 \\ \hline 193.24 \end{aligned}$$

$$\begin{aligned} x=50 \\ M=-16.71 \\ M=-9.91 \\ M=3.55 \\ \hline -23.07 \end{aligned}$$

$$\begin{aligned} x=60 \\ M=-57.62 \\ M=-61.05 \\ M=-57.82 \\ \hline -176.49 \end{aligned}$$

$$\begin{aligned} x=70 \\ m=20 \quad M=-81.05 \\ m=30 \quad M=-91.07 \\ m=40 \quad M=-94.87 \\ \hline -266.99 \end{aligned}$$

$$\begin{aligned} x=80 \\ M=-87.00 \\ M=-99.98 \\ M=-107.62 \\ \hline -294.60 \text{ MAX(-)} \end{aligned}$$

$$\begin{aligned} x=90 \\ M=-75.48 \\ M=-87.77 \\ M=-96.05 \\ \hline -259.60 \end{aligned}$$

$$\begin{aligned} x=100 \\ m=20 \quad M=-46.48 \\ m=25 \quad M=-54.46 \\ m=30 \quad M=-60.18 \\ \hline -161.10 \end{aligned}$$

$$\begin{aligned} x=25 \\ M=162.02 \\ M=210.32 \\ M=150.81 \\ \hline 523.15 \text{ MAX(+)} \end{aligned}$$

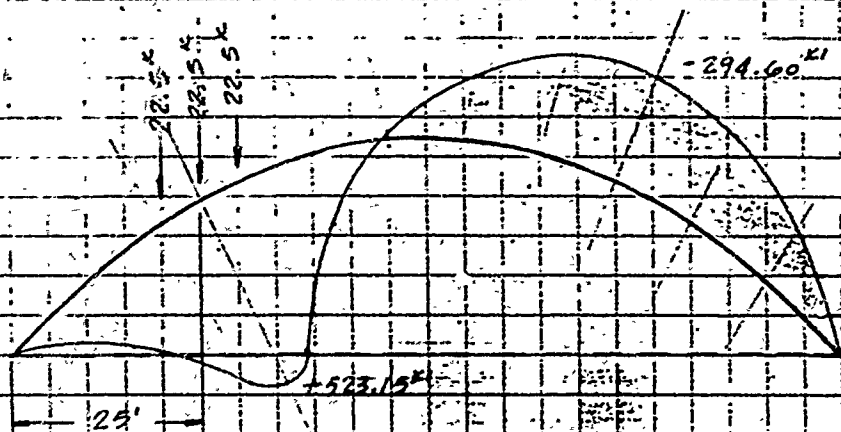
$$M_{25} = (22.5)(20)\left(1 - \frac{25}{110}\right) - (9.613)(19.3182) = 162.02$$

(m=20)

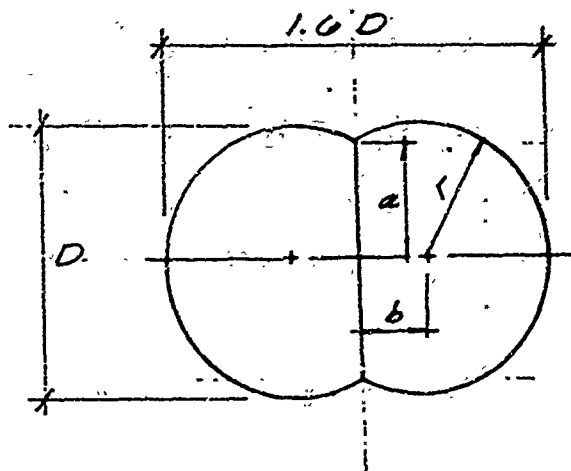
$$M_{25} = \frac{(22.5)(80)(25)}{110} - (13.370)(19.3182) = 150.807$$

(m=30)

Tank Loading Spans Over 15' : Stressing 3 Cables / Arch
(Max. Moments Occure @ 20, 25, 30 m intervals)



INVESTIGATE INFLATION PRESSURES & FABRIC STRESSES:



MAX. BENDING MOMENT IS
523.15 KIP-FT. = 6.278×10^6
IN.-LBS.

IF $a = .8r$
 $b = .6r$

FABRIC STRESS DUE TO BENDING (S_B):

$$S_B = \frac{M}{2N(ab + r^2 \sin^{-1}(b/r))}$$

N = No. OF CELLS

M = MOMENT

(ASSUME WEB CARRIES NO LOAD)

$$S_B = \frac{M}{2N(.48r^2 + r^2 \sin^{-1}(.6))}$$

$$S_B = \frac{M}{2.247 Nr^2}$$

TO PREVENT COMPRESSION FAILURE $S_T = S_B$

FABRIC STRESS DUE TO INFLATION (S_T)

$$S_T = \frac{P(r^2 \sin^{-1}(b/r) + ab)}{2r \sin^{-1}(b/r)} \quad (\text{WEB CARRIES NO LOAD})$$

OR

$$P = \frac{S_T 2r \sin^{-1}(b/r)}{r^2 \sin^{-1}(b/r) + ab} \quad \text{FOR } S_T = S_B$$

$$P = \frac{(S_B)(2r)(\sin^{-1}(.6))}{r^2 \sin^{-1}(.6) + .48r^2} = 1.146 S_B / r$$

$$P = \frac{1.146}{r} \left(\frac{M}{2.247 Nr^2} \right) = .51 M / Nr^3$$

FOR $N=2$

$M = 6.278 \times 10^6$ IN.-LBS.

$$P = 1.600 \times 10^6 / r^3 \quad (\text{LBS./IN}^2)$$

MAX. LONGITUDINAL FABRIC STRESS: (S_L)

$$S_{LMAX.} = S_B + S_T \quad \text{SINCE } S_B = S_T$$

$$S_{LMAX.} = 2S_B = (2) \left(\frac{M}{2.247 N r^2} \right)$$

FOR $N=2$

$$M = 6.278 \times 10^6 \text{ IN-LBS.}$$

$$S_L = 2.794 \times 10^6 / r^2 \text{ (LBS./IN.)}$$

MAX. TRANSVERSE FABRIC STRESS: (S_T)

$$S_T = PR$$

10 FOR D=1 TO 15 STEP 1

>20 F

20 3AD FORMAT

>20 R=S*D

>30 P=1605.77C/(R*R*R)

>40 S1=2794000/(R*R)

>50 S2=P/R

>60 PRINT D,P,S1,S2

>70 NEXT D

>80 END

>RUN

14:57 12/27

1 DIA.

2 (FT.)

3

4

5

6

7

8

9

10

11

12

13

14

15

PRESS (LBS./IN²)

7407.41

925.926

274.348

115.741

59.2593

34.2936

21.5959

14.4676

10.1611

7.40741

5.56529

4.28669

3.37160

2.65949

2.18479

LONG.

FABRIC

STRESS

(LBS./IN.)

77611.1

19408.8

8623.46

4850.69

3104.44

2155.86

1583.90

1212.67

958.162

776.111

641.414

538.966

459.237

395.975

344.938

TRANS.

FABRIC

STRESS

(LBS./IN.)

44444.4

11111.1

4938.27

2777.78

1777.78

1234.57

907.029

694.444

548.697

444.444

367.309

308.642

262.985

226.757

197.531

80 HALT

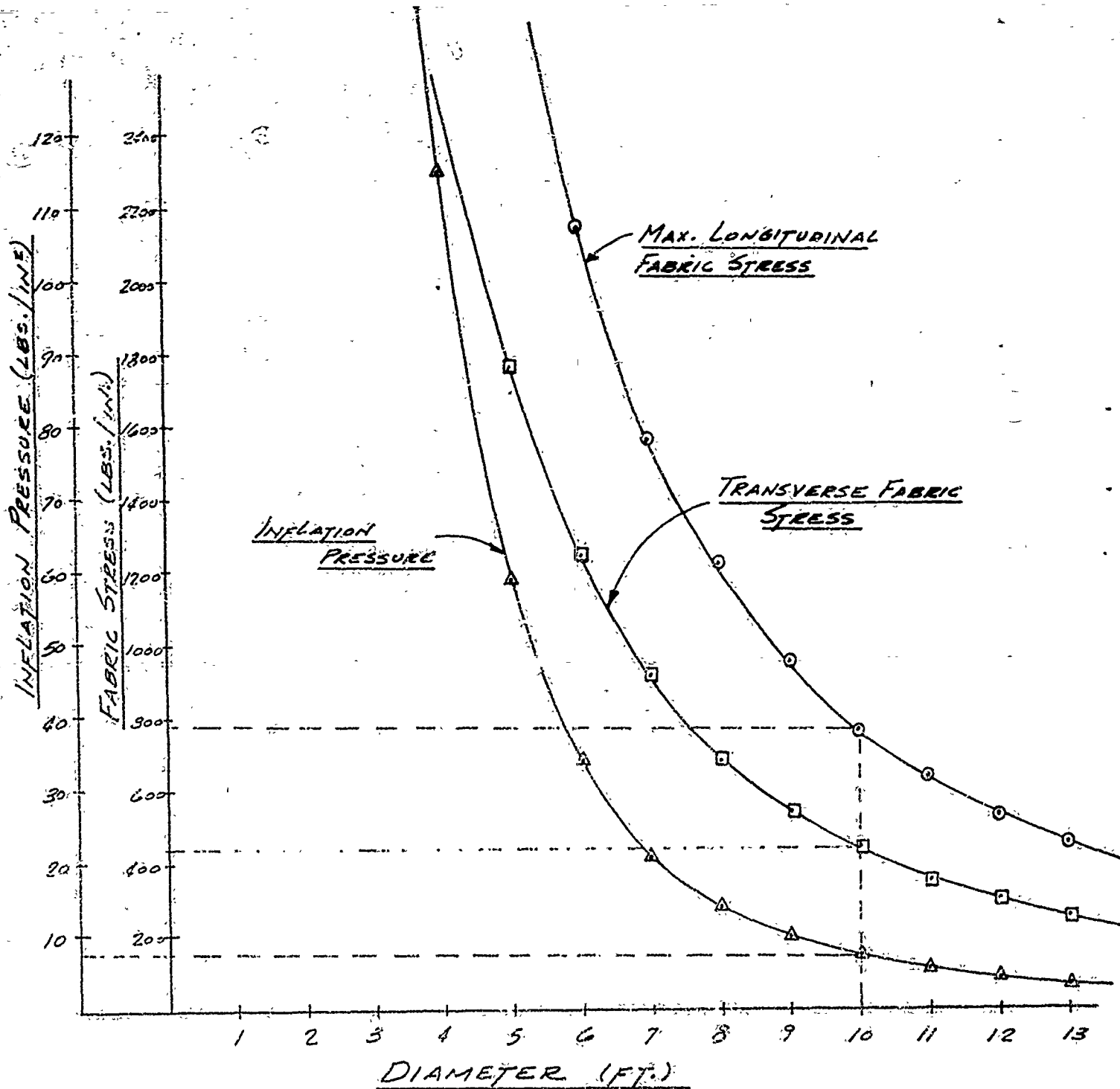
>SYS

!BYE

12/27/ 72 14:58

CLT 7

CCU 0.020

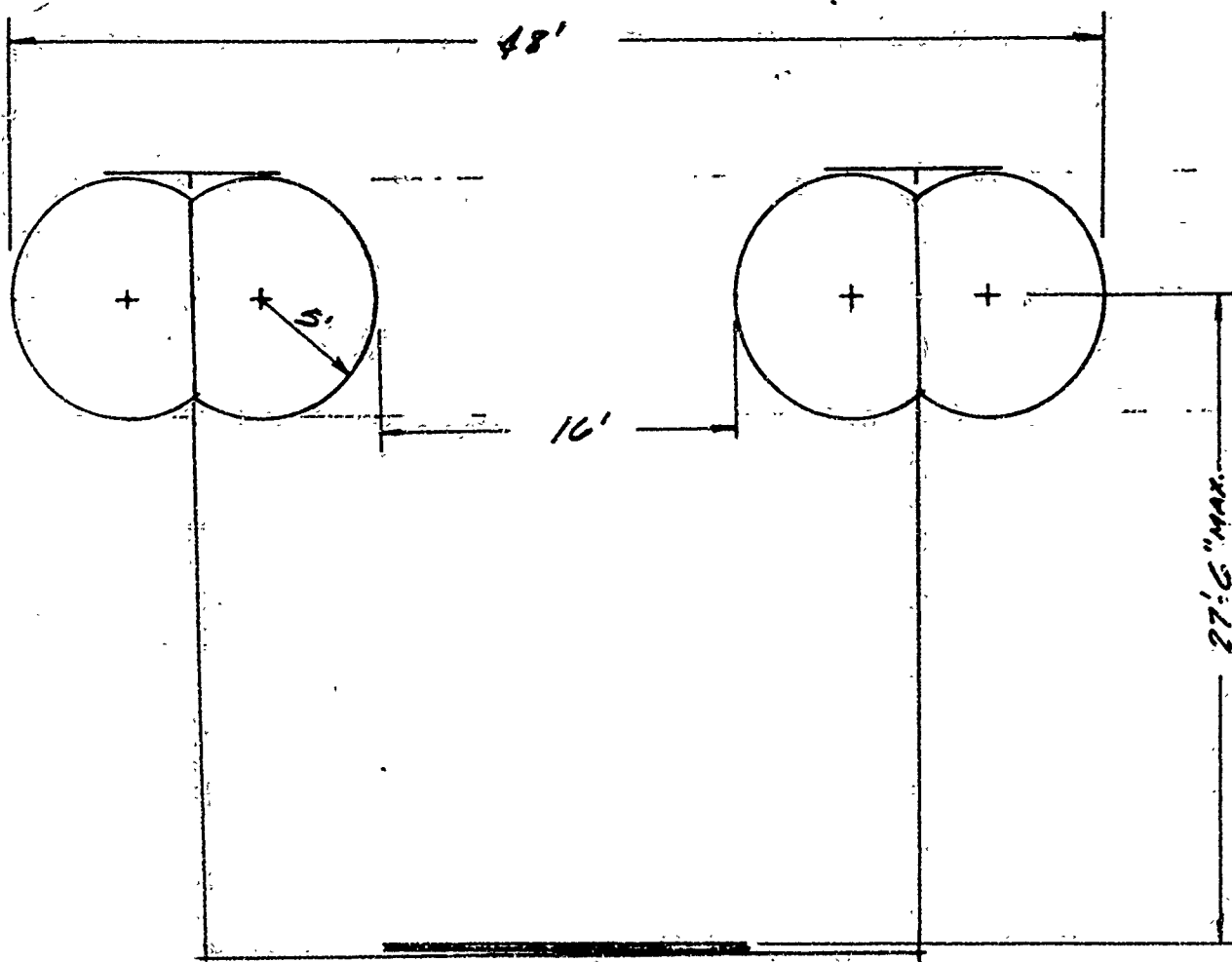


FOR 10 FT. DIAMETER ARCH

MAX. LONG. FABRIC STRESS = 776 LBS./IN.

TRANS. FABRIC STRESS = 444 LBS./IN.

INFLATION PRESSURE = 7.4 LBS./IN²



OVERALL DIMENSIONS - 48 FT. W X 32'-6" H

FABRIC STRESS - 776 LBS./IN.

INFLATION PRESSURE - 7.4 LBS./IN²

$$VOLUME = (2) \left[(2)(\pi)(10)^2/4 - (9.27)(5) - (8)(5-2) \right] \times 126 = 21,856 \text{ FT}^3$$

$$SURFACE AREA = (2) \left[2(\pi)(10) - (2)(9.27) \right] 126 = 11,162 \text{ FT}^2$$

CONCEPT Nº 6

INVERSE SUSPENSION

BRIDGE

C-59a

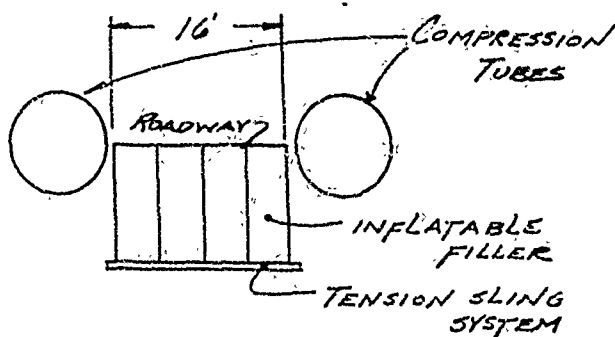
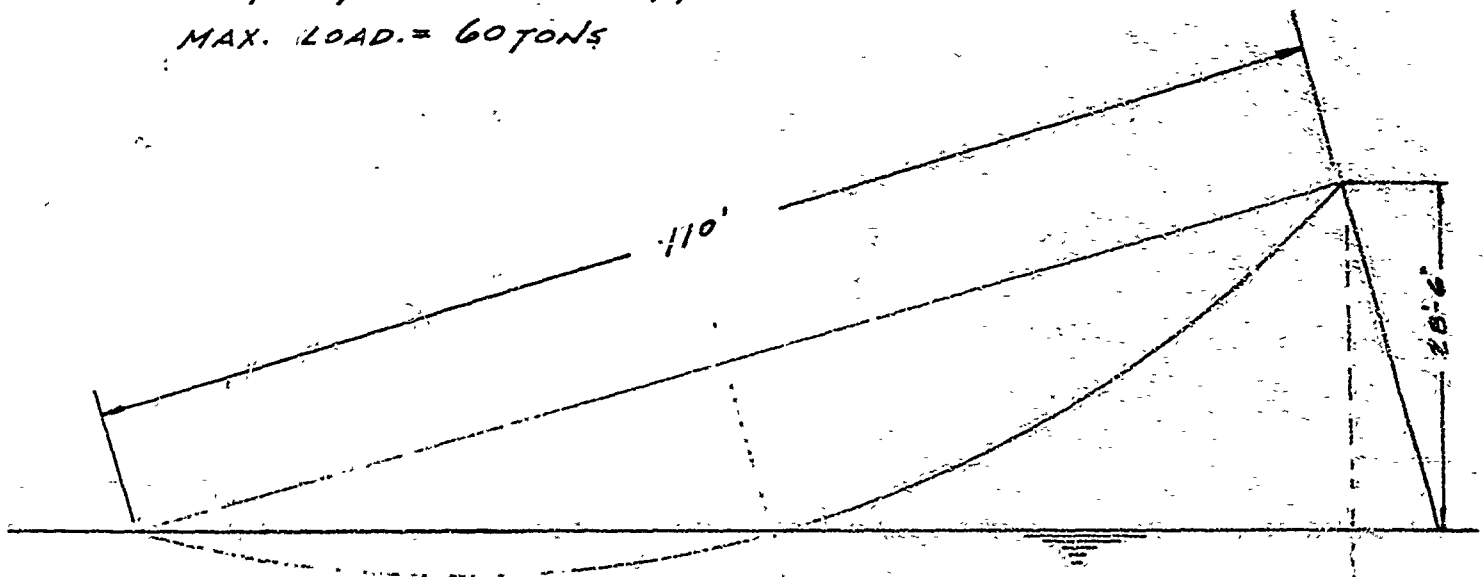
INVERSE SUSPENSION BRIDGE CONCEPT:

DESIGN DATA:

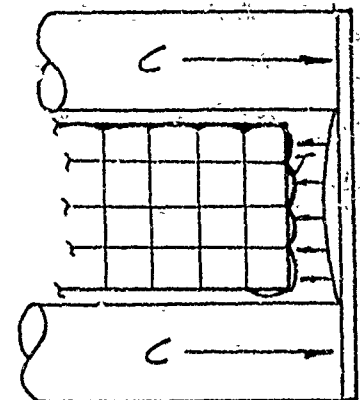
LENGTH = 110 FT.

WIDTH OF ROADWAY = 16 FT.

MAX. LOAD = 60 TONS



SECTION



PLAN VIEW

FILLER SYSTEM:

$$P = \frac{\text{LOAD}}{\text{AREA}} = \frac{120,000^{\#}}{(16)(15)} = 4 \text{ LBS/IN}^2$$

$$S_s = (P)(r) = (4)(48) = 192 \text{ LBS./IN.}$$

S=XISEARCH

12/18/ '72 11:53

LOGIN: 15078RD,C,

ID= D

!BASIC

>10 FOR B=1 TO 15

>20 LET R=((4*B*B)+(110*110))/(B*B))

>30 LET A=ATN(55/(R-B))

>40 LET T=120000/SIN(A)

>50 LET C=T*COS(A)

>60 PRINT B,R,A,T,C

>70 NEXT B

>80 END

>RUN

11:56	12/18	R (FT.)	ANGLE (RAD.)	TENSION	COMPRESSION
1	B	1513	3.63596E-02	3.30109E+06	3.29891E+06
2		757.250	7.26952E-02	1.65218E+06	1.64782E+06
3		505.667	.108983	1.10327E+06	1.09673E+06
4		380.125	.145199	829364.	820636.
5		305	.181320	665455.	654545.
6		255.083	.217322	556545.	543455.
7		219.571	.253184	479065.	463792.
8		193.063	.288883	421227.	403773.
9		172.556	.324398	376485.	356848.
10		156.250	.359707	340909.	319091.
11		143	.394791	312000.	288000.
12		132.042	.429631	288091.	261909.
13		122.846	.464208	268028.	239664.
14		115.036	.498504	250987.	220442.
15		108.333	.532504	236364.	203636.

80 HALT

>SYS

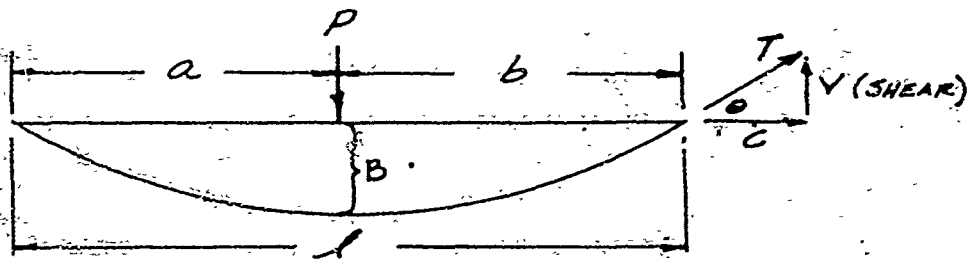
!BYE

12/18/ '72 11:58

CLT 5

CCU 0.012

INVESTIGATE SUSPENSION CONCEPTS:

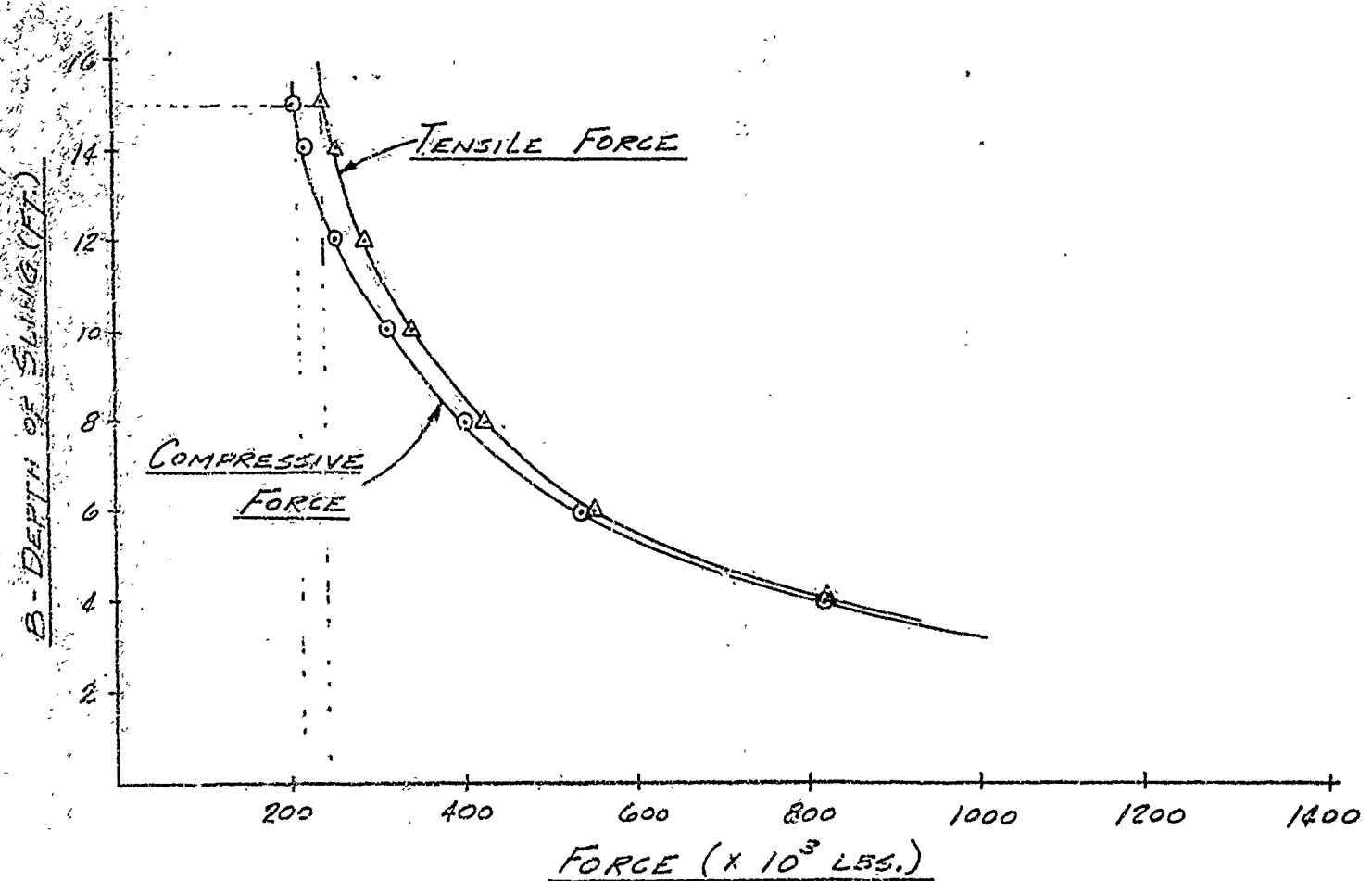


V (MAX.) OCCURS WHEN P IS AT SUPPORT

$$T = V / \sin \theta$$

$$C = T \cos \theta$$

FOR $P = 120,000$ LBS.
 $l = a = 110$ FT



AX:50JERSEARCH

12/18/ '72 14:30

!LOGIN: 1507BRD,C,

ID= A

!BASIC

>10 LET C=101818

>20 FOR P=10 TO 25

>30 LET D=SQR((4*C)/(P*3.14))

>40 LET S=P*(D/2)

>50 PRINT P,D,S

>60 NEXT P

>70 END

>RUN

14:33	12/18	DIA.	FABRIC STRESS
10	P	113.888	569.439
11		108.588	597.233
12		103.965	623.790
13		99.8863	649.261
14		96.2528	673.770
15		92.9891	697.418
16		90.0363	720.290
17		87.3480	742.458
18		84.8870	763.983
19		82.6229	784.918
20		80.5309	805.309
21		78.5901	825.196
22		76.7832	844.615
23		75.0954	863.597
24		73.5143	882.172
25		72.0290	900.363

70 HALT

>SYS

!BYE

12/18/ '72 14:34

CLT 3

CCU 0.010

FOR $B = 15 \text{ FT.}$

$$T = 236,364 \text{ LBS.}$$

$$C = 203,636 \text{ LBS.}$$

$$t \text{ (PER INCH OF WIDTH)} = \frac{236,364 \text{ LBS.}}{(16 \text{ FT.})(12 \text{ IN./FT.})}$$

$$t = 1231 \text{ LBS./IN.}$$

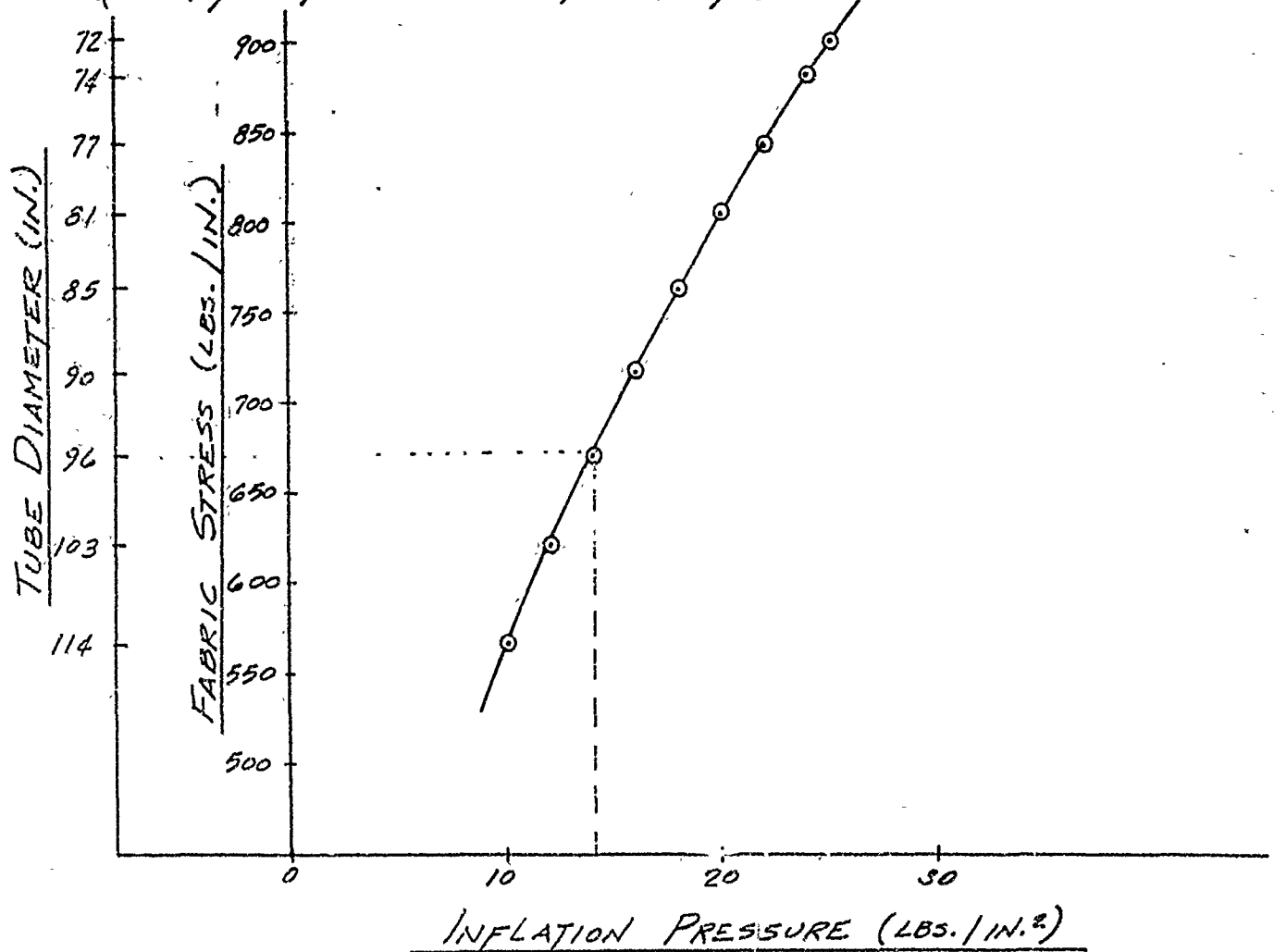
$$C/2 = 101,818 \text{ LBS. PER TUBE} = C'$$

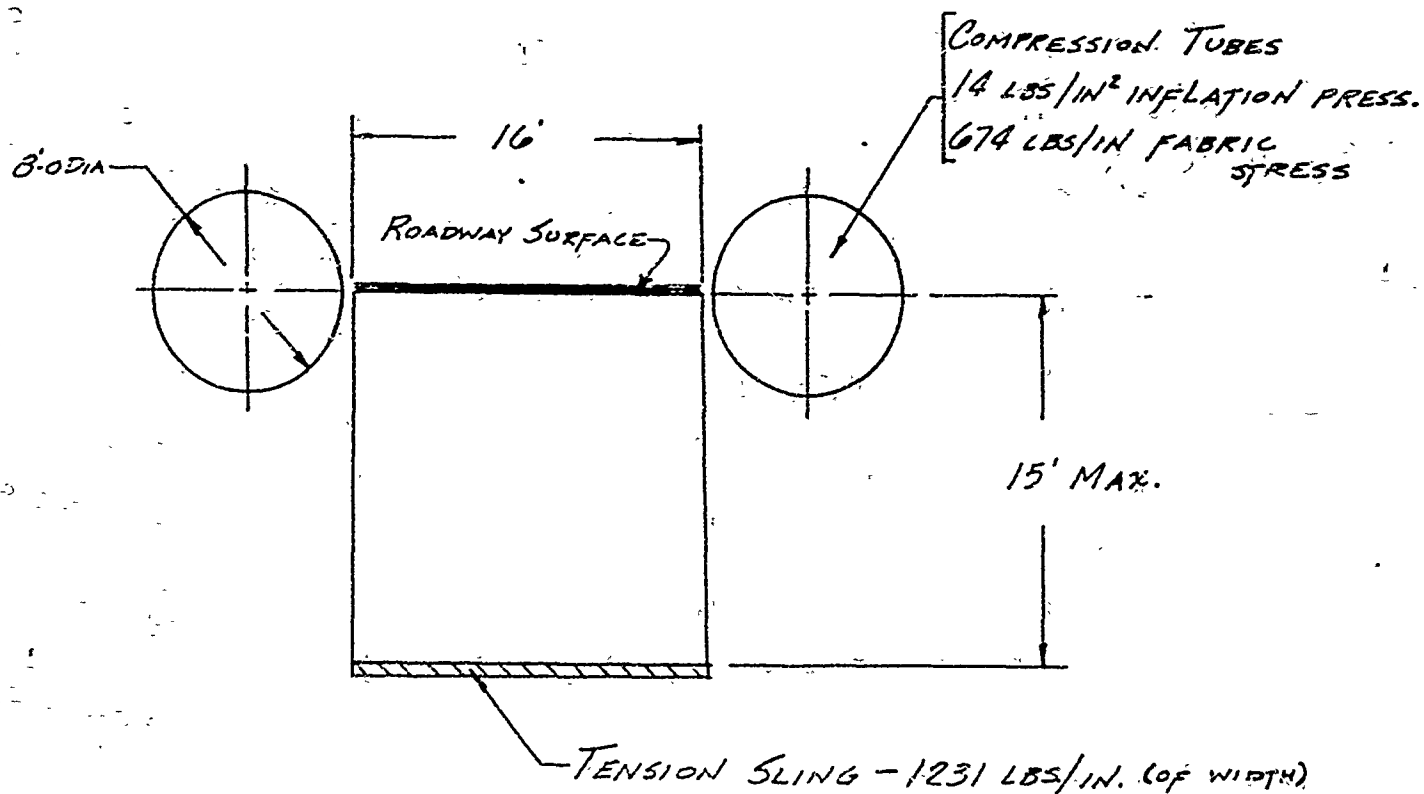
$$A = \frac{C/2}{P} = \frac{C'}{P} \quad P = \text{INFLATION PRESSURE}$$

$$A = \pi d^2/4$$

$$d = (4C'/P\pi)^{1/2}$$

$$S(\text{FABRIC}) = Pr$$





OVERALL DIMENSIONS - 32 FT. W X 19' H

FABRIC STRESS - 674 LBS./IN.

INFLATION PRESSURE - 14 LBS/IN²

VOLUME - TUBES - $(\pi)(8)^2/4 \times 110 \times 2 = 11,058 \text{ FT.}^3$

FILLER - $(2/3)(110)(15)(16) = 17,600 \text{ FT.}^3$

SURFACE AREA - TUBES - $(\pi)(8)(110)(2) = 5529 \text{ FT.}^2$

FILLER - $(2/3)(110)(15)(2) + (110)(16) + (115)(16) = 5800 \text{ FT.}^2$

CONCEPT № 7

TUBES

WITH

SUPPORT

C-65a

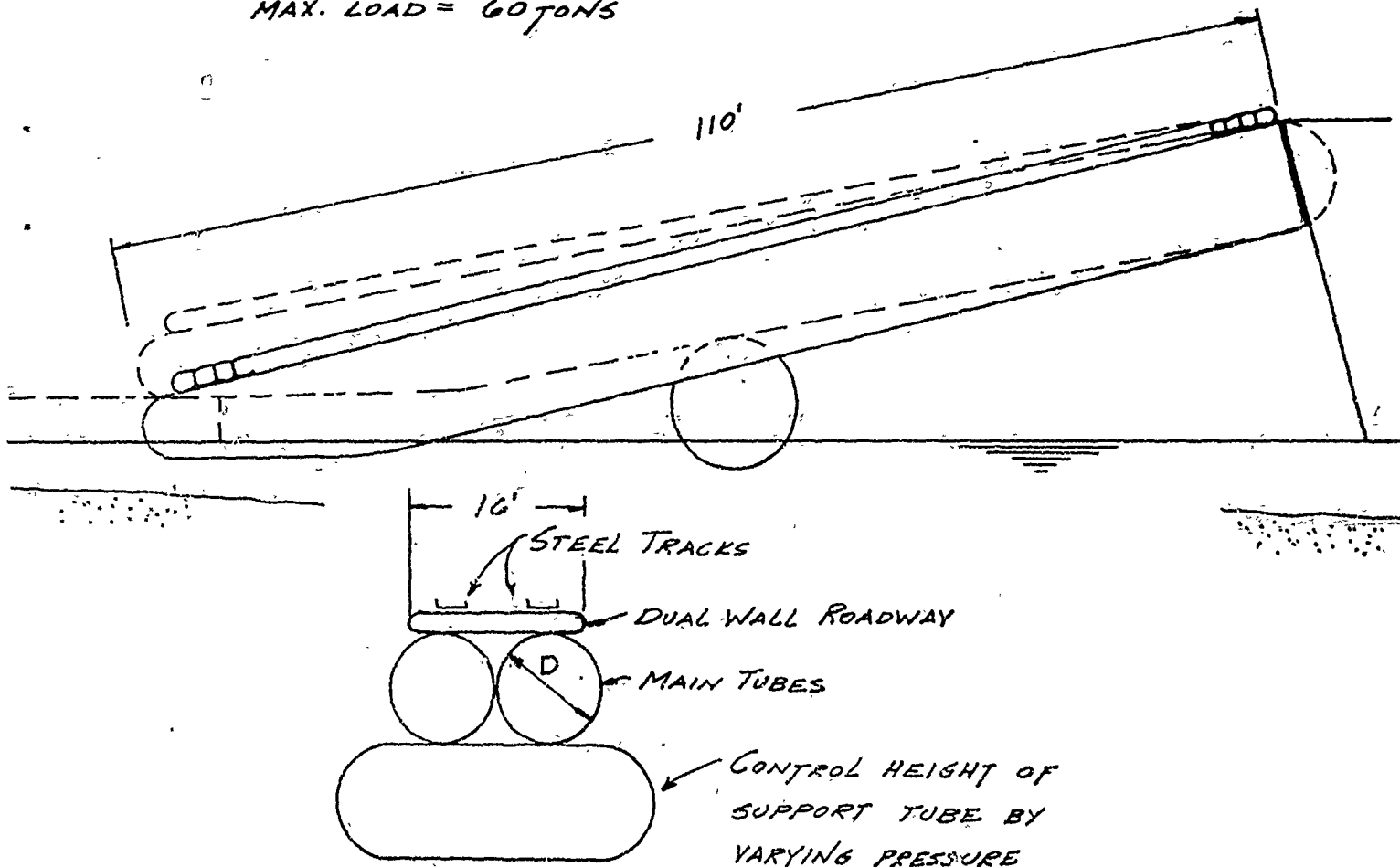
CIRCULAR TUBES WITH SUPPORT CONCEPT:

DESIGN DATA:

LENGTH = 110 FT.

WIDTH OF ROADWAY = 16 FT.

MAX. LOAD = 60 TONS



SECTION

(TRANSITION PIECE REQD. AT BEACH OR CAUSEWAY END OF RAMP)

LONGITUDINAL STRESS (INFLATION) $S_I = \frac{pd}{4}$

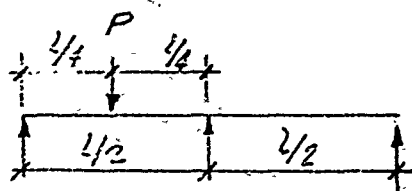
$$S_I = S_B$$

LONGITUDINAL STRESS (MOMENT) $S_B = \frac{M}{\text{AREA}} = \frac{4M}{\pi d^2}$

INFLATION PRESSURE TO RESIST BENDING $p = \frac{4}{d} \left(\frac{4M}{\pi d^2} \right) = \frac{16M}{\pi d^3}$

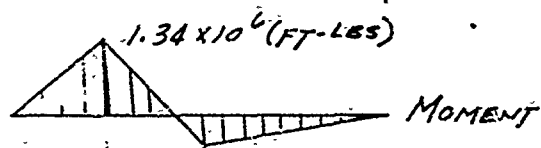
MAX. FABRIC STRESS = $\left(\frac{pd}{4} \right) (2) = \frac{pd}{2}$

INVESTIGATE VARIOUS BENDING MOMENT CONDITIONS:



$$P = 120,000 \text{ LBS.}$$

$$L = 110 \text{ FT.}$$

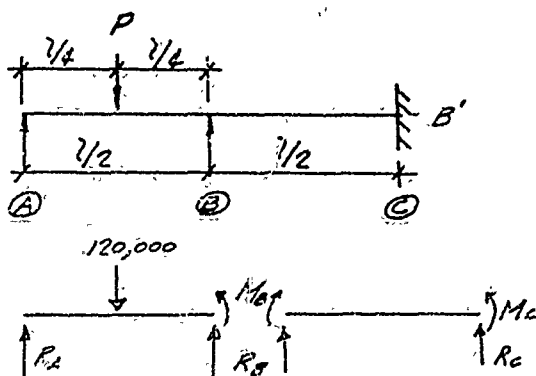


$$M(\text{MAX}) = \frac{13}{64} (P) (L/2) \text{ (FROM HANDBOOK)}$$

$$M(\text{MAX.}) = \frac{13}{64} (120,000) (55)$$

$$\underline{M(\text{MAX}) = 1,340,625 \text{ FT-LBS.}}$$

$$= 16.088 \times 10^6 \text{ IN-LBS.}$$



(SOLVE BY THREE MOMENT EQUATION)

$$M_A(55) + (2)(M_B)(110) + M_C(55) =$$

$$- (120,000)(27.5)(27.5)(1 + 1/2)$$

$$4M_B + M_C = -2,475,000 \text{ (FT-LBS.)}$$

$$\sum \epsilon M_A = 0$$

$$(120,000)(27.5) - (-707,143) = 55R_B$$

$$R_B = 72,875 \text{ LBS.}$$

$$M_B(55) + 2M_C(55+0) + M_{B'}(0)$$

$$M_B = -2M_C$$

$$\sum \epsilon F_V = 0 \therefore R_A = 47,143 \text{ LBS.}$$

$$-8M_C + M_C = -2,475,000$$

$$M_C = 353,571 \text{ FT-LBS.}$$

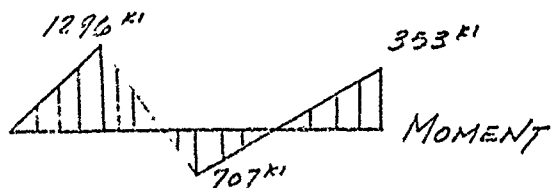
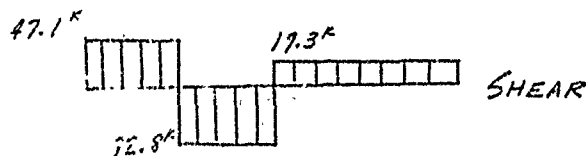
$$M_B = -707,143 \text{ FT-LBS.}$$

$$\sum \epsilon M_C = 0$$

$$-353,571 + (-707,143) + 55R_B = 0$$

$$R_B = 19,286 \text{ LBS.}$$

$$\sum \epsilon F_V = 0 \quad R_C = -19,286 \text{ LBS (ACTING DOWN)}$$



$$\underline{M(\text{MAX}) = 1,296,000 \text{ FT-LBS.}}$$

$$= 15.552 \times 10^6 \text{ IN-LBS.}$$

XOC
RSEARCH

01/03/ '73 12:54

!LOGIN: 157FFF

?
!LOGIN: 1507BRD,C,

ID= B

!BASIC

>10 FOR D=60 TO 120 STEP 6

>20 M=8044000 (EA. TUBE)

>30 P=(16*M)/(3.14*D*D*D)

>40 S=(P*D)/2

>50 PRINT D,P,S

>60 NEXT D

>70 END

>RUN (LBS./IN²) (LBS./IN.)

12:56	01/03	PRESS.	STRESS
60	DIA.	189.762	5692.85
66	(IN.)	142.571	4704.84
72		109.816	3953.37
78		86.3731	3368.55
84		69.1552	2904.52
90		56.2257	2530.16
96		46.3285	2223.77
102		38.6244	1969.85
108		32.5380	1757.05
114		27.6661	1576.97
120		23.7202	1423.21

70 HALT

>10 FOR D=60 TO 120 STEP 6

>20 M=7776000 (EA. TUBE - FIXED END)

>30 P=(16*M)/(3.14*D*D*D)

>40 S=(P*D)/2

>50 PRINT D,P,S

>60 NEXT D

>70 END

>RUN

12:59	01/03		
60		183.439	5503.18
66		137.821	4548.09
72		106.157	3821.66
78		83.4954	3256.32
84		66.8511	2807.75
90		54.3524	2445.86
96		44.7850	2149.68
102		37.3376	1904.22
108		31.4540	1698.51
114		26.7443	1524.43
120		22.9299	1375.80

70 HALT

>SYS

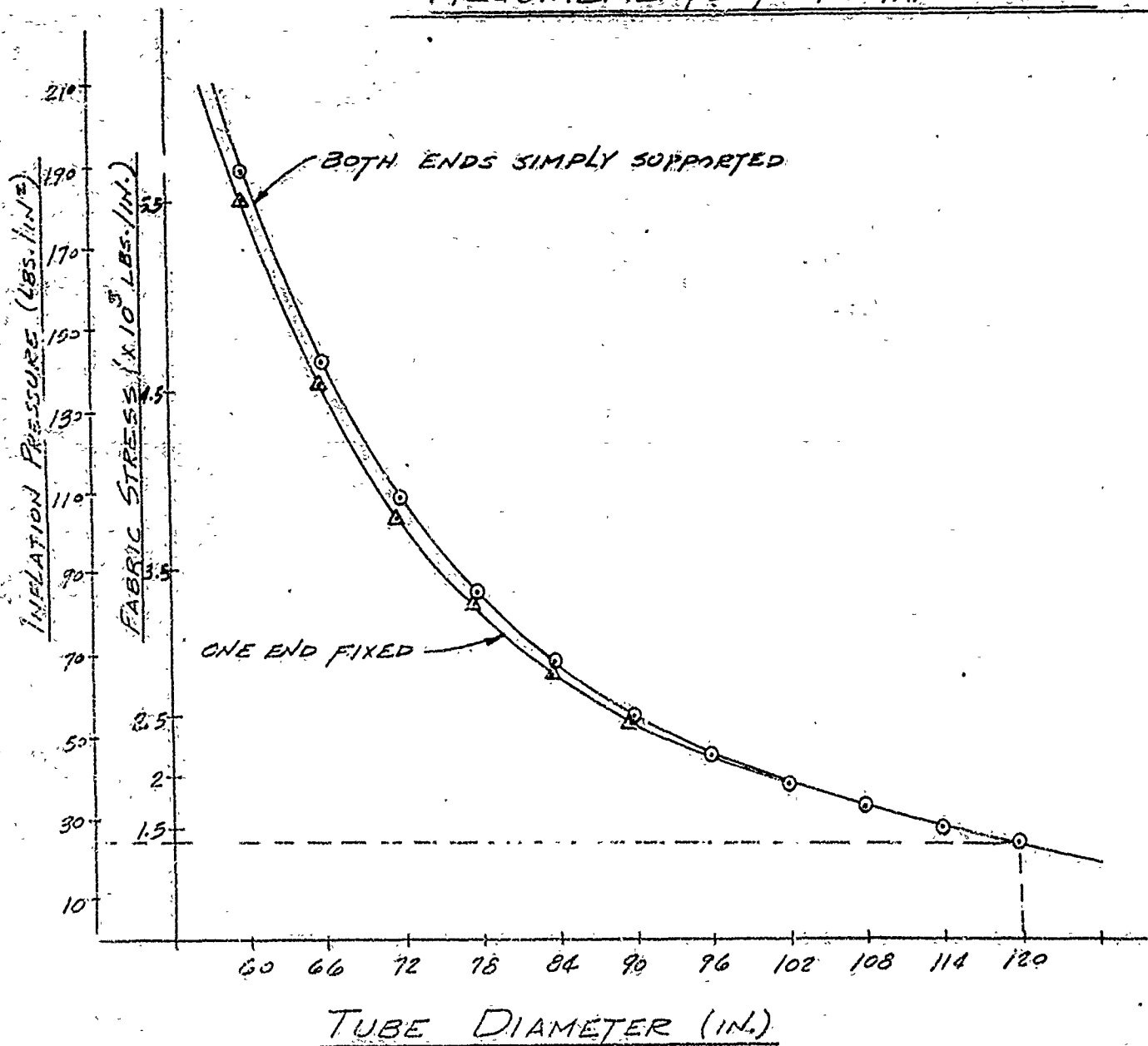
!BYE

01/03/ '73 12:59

CLT 4

CCU 0.020

REQUIREMENTS FOR MAIN TUBES



50.0 DIA. = 120 IN. = 10 FT.

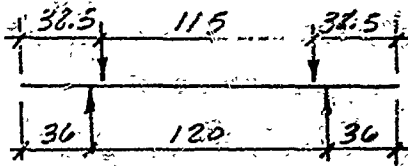
BOTH ENDS SIMPLY SUPPORTED:

$$P = 23.7 \text{ LBS./IN.}^2 \quad S = 1423 \text{ LBS./IN.}$$

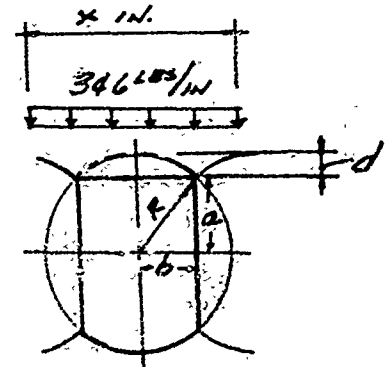
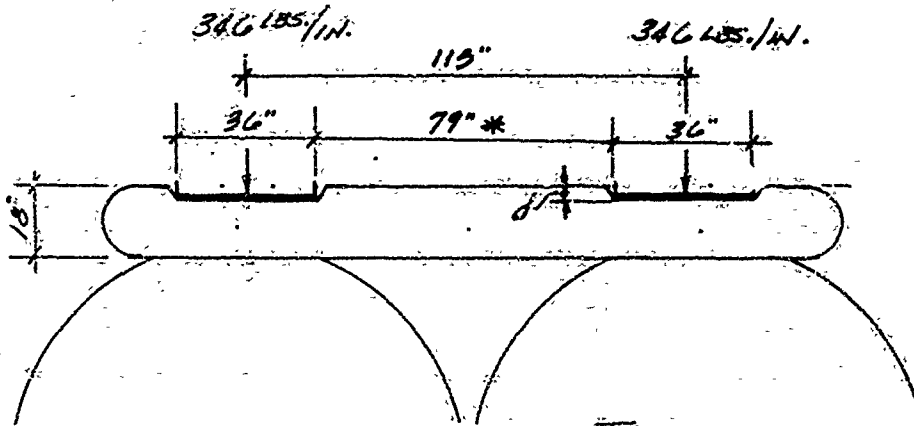
ONE END FIXED:

$$P = 22.9 \text{ LBS./IN.}^2 \quad S = 1376 \text{ LBS./IN.}$$

DUAL WALL ROADWAY:



TRACK SPACING ON 60 TON TANK = 115 IN.
TRACK WIDTH = 27" USE 36" SUPPORT TRACK



TANK LOADING PER INCH = $\frac{60,000 \text{ LBS.}}{173 \text{ IN.}} = 346 \text{ LBS./IN. (PER TRACK)}$

+ (1/4 SCALE)

FOR PRELIMINARY DESIGN, CONSIDER TANK LOADING CRITICAL.
BENDING'S MOMENT IN DUAL WALL ≈ 0 . HIGH INFLATION REQD. TO
KEEP LOCAL DEFLECTION TO A MINIMUM.

DUAL WALL DESIGN - $\frac{a}{b} \geq 1.3$ LET $a = 1.3b$

$$d = R - a$$

$$R = (a^2 + b^2)^{1/2} = ((1.3b)^2 + b^2)^{1/2} = (2.69b^2)^{1/2} = 1.64b$$

$$d = 1.64b - 1.3b = .34b$$

IF ALLOWED TO DEFLECT TO WEB LINE, THEN:

$$\text{AREA OF CONTACT} = (2b)(\text{WIDTH OF TRACK}) = 72b \text{ (IN}^2\text{) (for } d = .34b\text{)}$$

$$\text{LOAD} = (346 \text{ LBS./IN.})(2b) = 692b \text{ (LBS.)}$$

$$\text{INFLATION PRESSURE} = \frac{\text{LOAD}}{\text{AREA}} = \frac{692b}{72b} = 9.6 \text{ LBS./IN}^2$$

$$\text{FOR } R = 9 \text{ IN. } b = \frac{9}{1.64} = 5.48 \text{ IN } d = (5.48)(.34) = 1.86 \text{ IN.}$$

$$S = pR = (9.6)(9) = 86.5 \text{ LBS./IN.}$$

* 79" DIMENSION WILL HAVE TO BE REDUCED FOR OTHER VEHICLES
UNDER THE P-25 ALLOWANCE. BENDING MOMENT WILL
EFFECT THE DUAL WALL BEAM FABRIC STRESSES.

OVERALL DIMENSIONS - 20 FT. W X 12 FT D

FABRIC STRESS - 1423 LBS./IN.

INFLATION PRESSURE - 23.7 LBS./IN.²

VOLUME - TUBES - $2 \times (\pi)(10)^2/4 \times 110 = 17,279 \text{ FT.}^3$

DUAL WALL - $(\pi)(1.5)^2/4 \times 18' \times 73 = 2,322 \text{ FT.}^3$

SURFACE AREA - TUBES - $(\pi)(10)(2)(110) = 6911 \text{ FT.}^2$

DUAL WALL - $(18)(1.5)(110) = 2970 \text{ FT.}^2$

TUBE TUNNEL CONCEPT

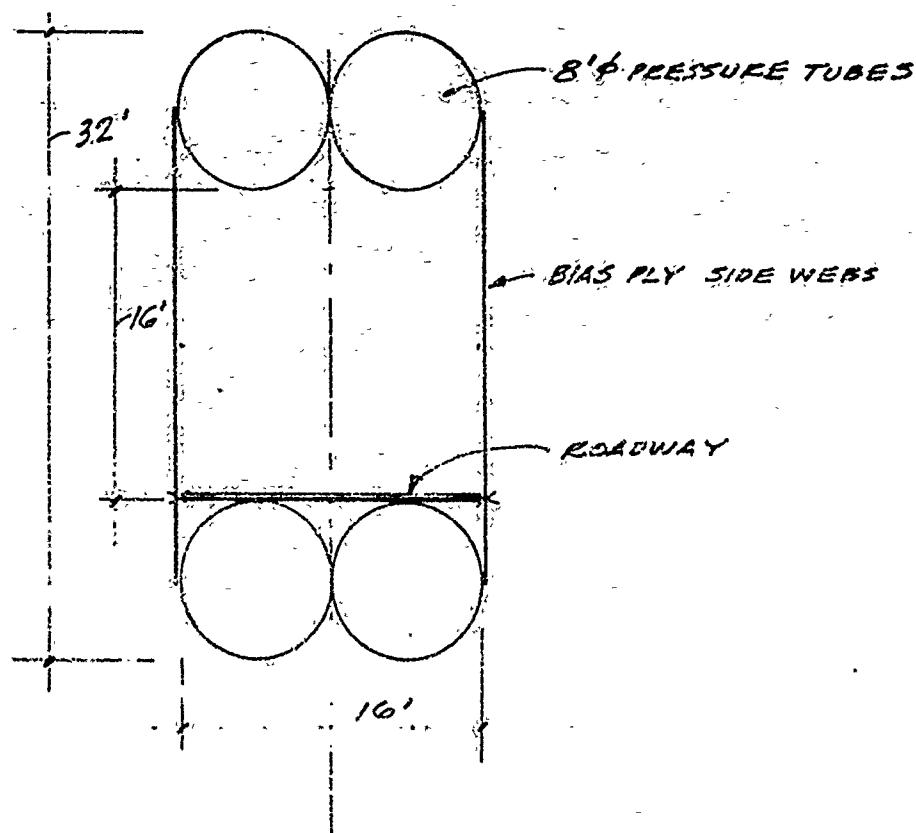
DESIGN DATA :

INSIDE WIDTH - 16 FT.
INSIDE HEIGHT - 16 FT.
LENGTH - 110 FT.
LOAD - 60 TONS

THE MAXIMUM BENDING MOMENT WITH A TANK AT MID SPAN

$$IS \quad M = \frac{PL}{4} = \frac{120,000(110)}{4} = 3,300,000 \text{ FT. LBS.}$$

RAMP CROSS SECTION IS -



IF SIDE WEBS CARRY NO SHEAR THEN MOMENT PER
TUBE IS

$$M_T = \frac{M}{4} = \frac{3,300,000}{4} = 825,000 \text{ LBS.}$$

THE BENDING STRESS IS

$$S_B = \frac{4M}{\pi d^2} = \frac{4(825,000)}{\pi (8)^2} = 16413 \text{ PSI}$$
$$= 1368 \text{ PSI}$$

THE PRESSURE REQ'D. IS

$$P = \frac{4S_d}{L} = \frac{4(1368)}{96} = 57 \text{ psi.}$$

MAX. STRESS IS

$$S_m = \frac{PL}{2} = \frac{57(96)}{2} = 2736 \text{ #/in.}$$

IF SIDE WEBS CARRY FULL SHEAR THEN THE FOUR TUBES ACT AS ONE BEAM, TAKING MOMENTS ABOUT THE CENTROID OF THE LOWER TUBES

$$PA_y - M = 0$$

$$\text{WHERE } A = 2\pi r^2 \\ y = 16 + d$$

$$P(2\pi r^2)(16+d) - M = 0$$

$$P = \frac{M}{(2\pi r^2)(16+d)} = \frac{3,300,000}{(2\pi 4^2)(16+8)} = 1368 \text{ PSF.} \\ = 9.5 \text{ PSI.}$$

MAX. STRESS IS

$$S_m = \frac{PL}{2} = \frac{9.5(96)}{2} = 456 \text{ #/in.}$$

OVERALL DIMENSIONS - 16 FT. W X 32 FT. H

FABRIC STRESS - 2736 LBS./IN - NO WEB CONTRIBUTION

456 LBS./IN - W/ WEB CONTRIBUTION

INFLATION - 57 LBS./IN² - NO WEB CONTRIBUTION

10 LBS./IN² - W/ WEB CONTRIBUTION

$$\text{VOLUME} = 4 \times \frac{(\pi)(8)^2}{4} \times 110' = 22,117 \text{ FT}^3$$

$$\text{SURFACE AREA} = 4 \times (\pi)(8) \times 110' = 11,058 \text{ FT}^2$$

CONCEPT No 9

HYBRID

TRUSS AND INFLATED

BLADDER

HYBRID STRUCTURE -

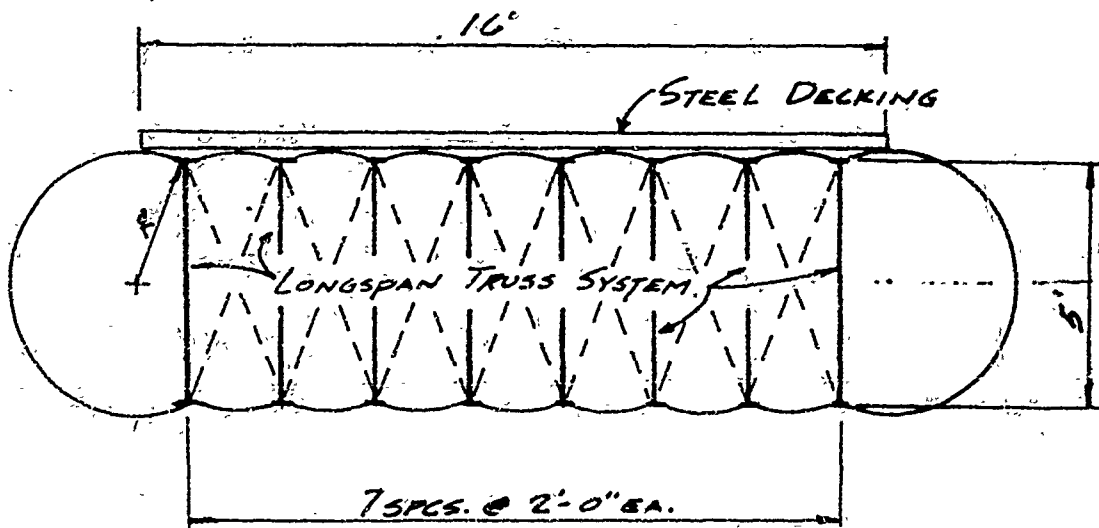
STEEL JOIST WITH INFLATABLE BLADDER

DESIGN CRITERIA:

LENGTH = 110 FT.

MIN. WIDTH = 16 FT.

MAX. LOAD = 60 TONS



LOADING - 60 TON TANK AT MIDSPAN:

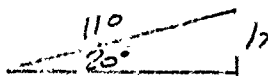
$$M = \frac{PL}{4} = \frac{(120,000 \text{ LBS.})(110 \text{ FT.})}{4} = 3.30 \times 10^6 \text{ FT.-LBS.}$$

EQUIVALENT UNIFORM LOADING - $M = \frac{WL^2}{8}$

$$W = \frac{8}{(L^2)}(M) = \frac{8}{(110)^2}(3.30 \times 10^6) = 2181 \text{ LBS./FT.}$$

DISTRIBUTED OVER 8 JOISTS = 272 LBS./FT. LIVE LOAD PER JOIST

LOAD DISTRIBUTION AT MAX. INCLINATION OF 20°



$$h = (110)(\sin 20^\circ) = 37.62'$$

$$\text{SLOPE} = \frac{\text{RISE}}{\text{RUN}} = \frac{37.62}{110} = .342 \text{ FT./FT.} = 4 \text{ IN./FT.}$$

$$P = 120,000 \text{ LBS.}$$

$$F_v = (120,000)(\cos 20^\circ) = 112,763 \text{ LBS.}$$

$$F_H = (120,000)(\sin 20^\circ) = 41,042 \text{ LBS.}$$

LOAD DISTRIBUTION AT MAX. INCLINATION (CONT.)

$$M = \frac{F_v L}{4} = (112,763)(110)/4 = 3.10 \times 10^6 \text{ FT.-LBS.}$$

$$\text{EQUIVALENT UNIFORM LOADING} = M = \frac{WL^2}{8}$$

$$W = \frac{8}{(110)^2} (3.10 \times 10^6) = 2000 \text{ LBS./FT.}$$

DISTRIBUTED OVER 8 JOISTS = 256 LBS./FT. LIVE LOAD PER JOIST

$$F_H = 41,012 \text{ LBS.} / 8 = 5130 \text{ LBS. TENSION / JOIST}$$

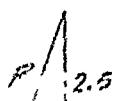
GENERAL REMARKS CONCERNING TRUSS SYSTEM:

1. FROM STANDARD SPECIFICATIONS AND LOAD TABLES FOR DEEP LONGSPAN STEEL JOISTS, THE FOLLOWING CRITERIA MUST BE FOLLOWED.
 - a) TOP COMPRESSION FLANGE Laterally supported every 36 in. - CAN BE ACCOMPLISHED WITH DECK.
 - b) MAX. SLOPE IN ORDER TO USE LOAD TABLES IS $\frac{1}{2}$ in./ft. - SLOPE TO STEEP. - TABLES VOID!
2. NECESSARY TO DESIGN A TRUSS SYSTEM - APPROX. 60 in. DEEP TO CARRY HORIZONTAL AND VERTICAL FORCES.

PRESSURIZATION AND FABRIC STRESS:

PRESSURIZATION OF BLADDER REQD. TO SEPARATE JOISTS AND TENSION DIAGONAL CABLE BRIDGING.

$$\text{ASSUME INFLATION PRESSURE} = 5 \text{ LBS./IN}^2$$



$$R = [(2.5)^2 + (1)^2]^{1/2} = 2.69 \text{ FT.}$$



$$\text{TRANSVERSE FABRIC STRESS} = PR = \text{MAX. STRESS}$$

$$S_T = (5 \text{ LBS./IN}^2)(2.69)(12) = 161 \text{ LBS./IN.}$$

STANDARD LOAD TABLE FOR

BASED ON

This table was developed using 30,000 psi allowable tensile stress. Steels with allowable tensile stresses from 22,000 psi to 30,000 psi may be used to meet this load table. The following table gives the TOTAL safe uniformly distributed load-carrying capacities in pounds per linear foot of span.

All loads shown are for roof construction only. The weight of DEAD loads, including weight of joists, must in all cases be deducted to determine the LIVE load-carrying capacity of the joists. Approximate weights per linear foot of joist include accessories.

The figures shown in red are the LIVE loads per linear foot of joist which will produce an approximate deflection of 1/360 of the span. Loads which will produce an approximate deflection of 1/240 of the span may be obtained by multiplying the red figures by 1.5. (NOTE: The tabulated loads corresponding to these deflection limitations have been computed on the basis of 30,000 psi allowable stress provisions. For joists designed to a lower

working stress, these loads may be increased in the ratio of 30,000 psi to the design stress used, in order to meet the same deflection limitations.) For roofs, LIVE load deflection is limited to 1/360 of the span where a plaster ceiling is attached or suspended; 1/240 of the span for all other cases. In no case shall the TOTAL capacity of the joists be exceeded.*

When holes are required in the top or bottom chords, the carrying capacities must be reduced in proportion to reduction of chord areas.

The top chords are considered as being stayed laterally by the roof deck.

The load table applies to joists with either parallel chords or standard pitched chords. When top chords are pitched, the carrying capacities are determined by the nominal depth of the joist at the center of the span. Standard top chord pitch is 1/4" per foot. If pitch exceeds this standard, the load table does not apply.

The load table may be used for parallel chord joists installed to a maximum slope of 1/4" per foot.

Joist Designation	Approx. Wt. in Lbs. per Linear Ft.	Depth in Inches	SAFE LOAD** in Lbs. Between	CLEAR OPENING OR NET SPAN IN FEET															
				28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43
52DLH10	27	52	26700	288	291	285	279	273	267	261	255	249	243	237	231	225	219	213	207
52DLH11	29	52	29300	327	320	313	306	299	293	287	281	275	270	264	259	254	249	244	240
52DLH12	31	52	32700	365	357	349	342	334	327	320	314	307	301	295	289	284	278	273	268
52DLH13	36	52	39700	443	433	424	414	406	397	389	381	373	366	358	351	344	338	331	325
52DLH14	40	52	45400	507	497	486	476	468	457	447	438	430	421	413	405	397	390	382	375
52DLH15	45	52	51000	589	577	565	553	542	531	520	509	498	487	476	465	454	443	432	421
52DLH16	50	52	55000	614	601	588	575	563	551	540	528	518	507	497	487	476	465	454	443
52DLH17	55	52	63300	708	691	676	661	647	634	620	608	595	583	572	560	549	539	528	518
56DLH11	29	56	28100	288	283	277	272	267	262	257	253	248	244	239	235	231	227	223	218
56DLH12	31	56	32300	331	324	318	312	306	300	295	289	284	278	273	268	263	259	254	249
56DLH13	36	56	39100	401	394	386	379	372	365	358	351	344	338	331	325	319	314	308	303
56DLH14	40	56	44200	453	444	435	427	419	411	403	396	388	381	375	368	361	355	349	343
56DLH15	45	56	50500	518	508	498	488	478	469	460	451	443	434	425	419	411	403	396	389
56DLH16	50	56	54500	559	548	537	526	516	506	496	487	478	469	460	452	444	436	426	417
56DLH17	55	56	62800	643	630	619	605	594	582	571	560	549	539	529	520	510	501	492	482



DEEP LONGSPAN STEEL JOISTS/DLH SERIES

MAXIMUM ALLOWABLE TENSILE STRESS OF 30,000 PSI

Joist Designation	Approx. Wt. in Lbs. per Linear Ft.	Depth in Inches	SAFE LOAD** in Lbs. Between	CLEAR OPENING OR NET SPAN IN FEET																	
				12	14	16	18	20	22	24	26	28	30	32	34	36	38	40	42	44	46
60DLH12	31	60	31100	795	792	789	786	783	780	777	774	771	768	765	762	759	756	753	750	747	744
60DLH13	36	60	37800	958	954	950	946	942	938	934	930	926	922	918	914	910	906	902	898	894	890
60DLH14	39	60	42000	1088	1083	1078	1073	1068	1063	1058	1053	1048	1043	1038	1033	1028	1023	1018	1013	1008	1003
60DLH15	45	60	49300	1288	1282	1276	1270	1264	1258	1252	1246	1240	1234	1228	1222	1216	1210	1204	1198	1192	1186
60DLH16	50	60	54200	1438	1431	1424	1417	1410	1403	1396	1389	1382	1375	1368	1361	1354	1347	1340	1333	1326	1319
60DLH17	55	60	62300	1618	1610	1602	1594	1586	1578	1570	1562	1554	1546	1538	1530	1522	1514	1506	1498	1490	1482
60DLH18	62	60	71900	1888	1879	1870	1861	1852	1843	1834	1825	1816	1807	1798	1789	1780	1771	1762	1753	1744	1735
64DLH12	31	64	30000	264	262	259	257	254	252	249	247	244	242	239	237	234	232	229	227	224	222
64DLH13	36	64	36400	321	318	315	312	309	306	303	300	297	294	291	288	285	282	279	276	273	270
64DLH14	39	64	41700	367	363	359	356	352	349	346	343	339	336	332	328	325	321	318	314	311	307
64DLH15	45	64	47800	421	416	412	408	404	400	396	392	388	384	380	376	372	368	364	360	356	352
64DLH16	50	64	53800	474	468	463	458	453	448	443	438	433	428	423	418	413	408	403	398	393	388
64DLH17	55	64	62000	546	539	533	527	521	515	509	503	497	491	485	479	473	467	461	455	449	443
64DLH18	62	64	71600	630	622	615	608	601	594	587	580	573	566	559	552	545	538	531	524	517	510
68DLH13	36	68	35000	288	284	279	275	271	267	263	259	255	252	248	244	240	237	233	229	225	221
68DLH14	39	68	40300	332	327	322	317	312	308	303	299	294	290	286	281	277	273	269	265	261	257
68DLH15	43	68	45200	372	365	360	354	348	343	337	332	327	322	317	312	308	303	299	295	291	287
68DLH16	50	68	53600	441	433	427	420	413	407	400	394	388	382	376	371	365	360	354	349	343	338
68DLH17	55	68	60400	497	489	481	474	467	460	453	446	439	433	427	420	414	408	403	397	391	385
68DLH18	62	68	69900	575	566	557	549	540	532	524	516	508	501	493	486	479	472	465	458	451	444
68DLH19	70	68	80500	662	651	641	631	621	611	601	592	583	574	565	555	546	537	527	518	508	499
72DLH14	39	72	39200	303	298	294	290	285	281	277	274	270	266	262	259	255	252	248	244	240	236
72DLH15	43	72	44900	347	342	335	331	326	322	317	312	308	303	299	295	291	286	282	277	273	269
72DLH16	50	72	51900	401	395	390	384	378	373	368	363	358	353	348	343	338	333	328	323	318	313
72DLH17	55	72	58400	451	445	438	432	426	420	414	408	402	397	391	386	381	376	371	366	361	356
72DLH18	62	72	68400	528	520	512	505	497	490	483	477	470	463	457	450	444	438	432	426	420	414
72DLH19	70	72	80200	619	609	600	591	582	573	565	557	549	541	533	525	518	511	504	497	490	483

*Section 204.10 of the Standard Specifications for Deep Longspan Steel Joists, DLJ and DLH Series limits the design LIVE load deflection as follows:
1/240 of span where a plaster ceiling is attached or suspended; 1/240 of span for all other cases.

**For extrapolation for safe uniform load between spans shown, divide the Safe Load in pounds by net span in feet plus 67 feet (The added .67 feet, eight inches, is necessary to obtain the proper span for which the load tables were developed)



PRESSURE STABILIZED LIGHTWEIGHT TRUSSES

DESIGN DATA:

LENGTH 110 FT.
LOAD 60 TONS

MAXIMUM BENDING MOMENT WITH LOAD AT MID SPAN IS

$$M = \frac{PL}{4} = \frac{120000(110)}{4} = 3,300,000 \text{ FT. LBS.}$$

ASSUMING LOAD MUST BE CARRIED BY TWO TRUSSES, THE
MOMENT PER TRUSS IS

$$M/T = 1,650,000 \text{ FT. LBS.}$$

$$= 19,800,000 \text{ IN. LBS.}$$

FOR 6061-T6 ALUM. FABRICATION

$$\sigma_{ALL} = 15 \text{ KSI.}$$

ASSUME DEPTH OF SECTION = 72 IN.

$$I_{REQ'D.} = \frac{Mc}{\sigma} = \frac{19,800,000(36)}{15,000}$$

$$= 47520 \text{ IN.}^4$$

$$I/\text{UNIT AREA FOR PAIR AT 72" SPC.} = 2592 \text{ IN.}^4$$

AREA REQ'D TOP & BOTTOM AT 72" SPC.

$$= \frac{47520}{2592} = 18.333 \text{ IN.}^2$$

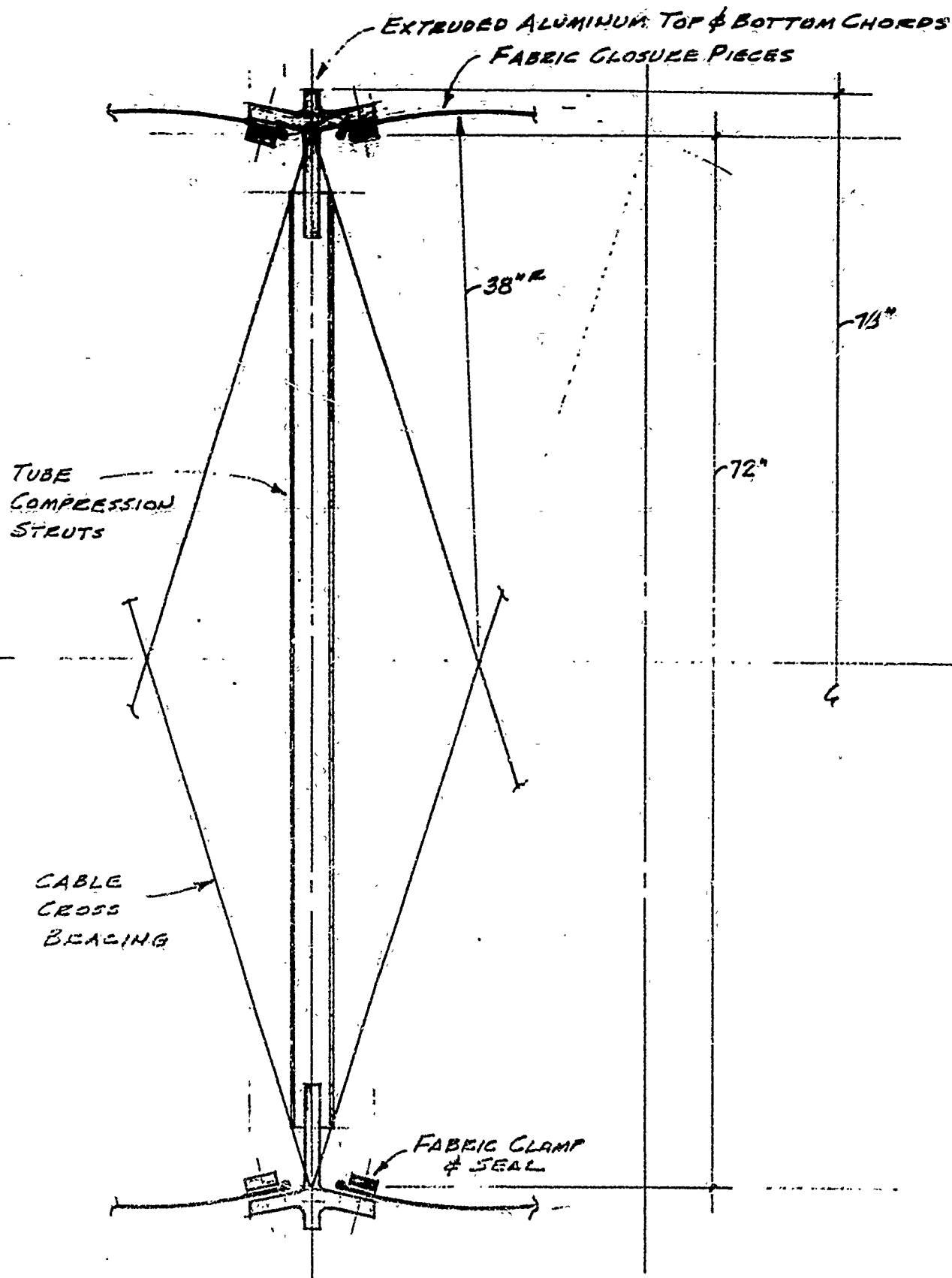
MAXIMUM FABRIC STRESS

$$S = pr = 5(38) = 190 \text{ #/IN.}$$

$$\text{FOR } f.s. = 3$$

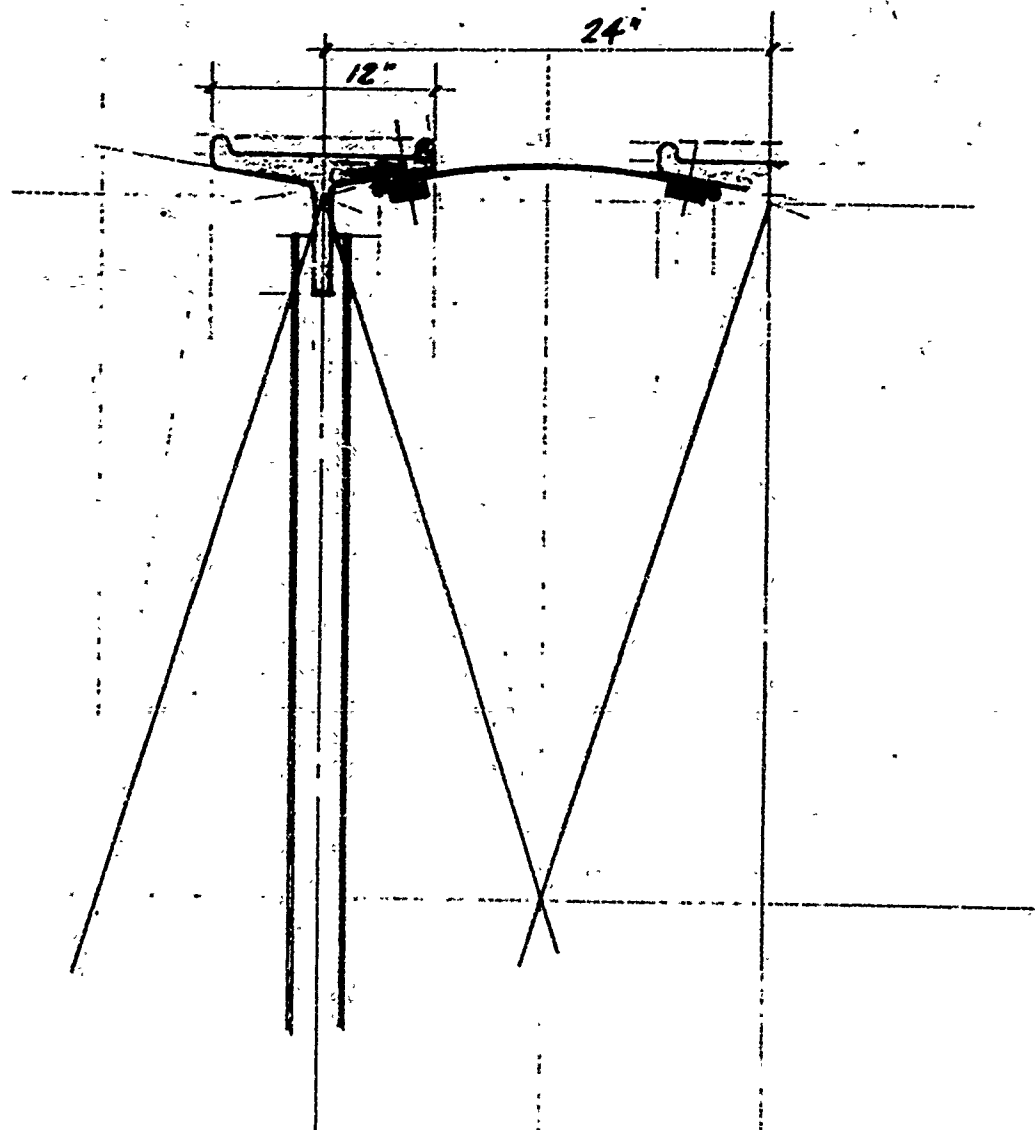
$$\text{MIN. BREAKING STRENGTH} = 3(190) = 570 \text{ #/IN.}$$

2 PLY 1002. POLYESTER IS O.K.

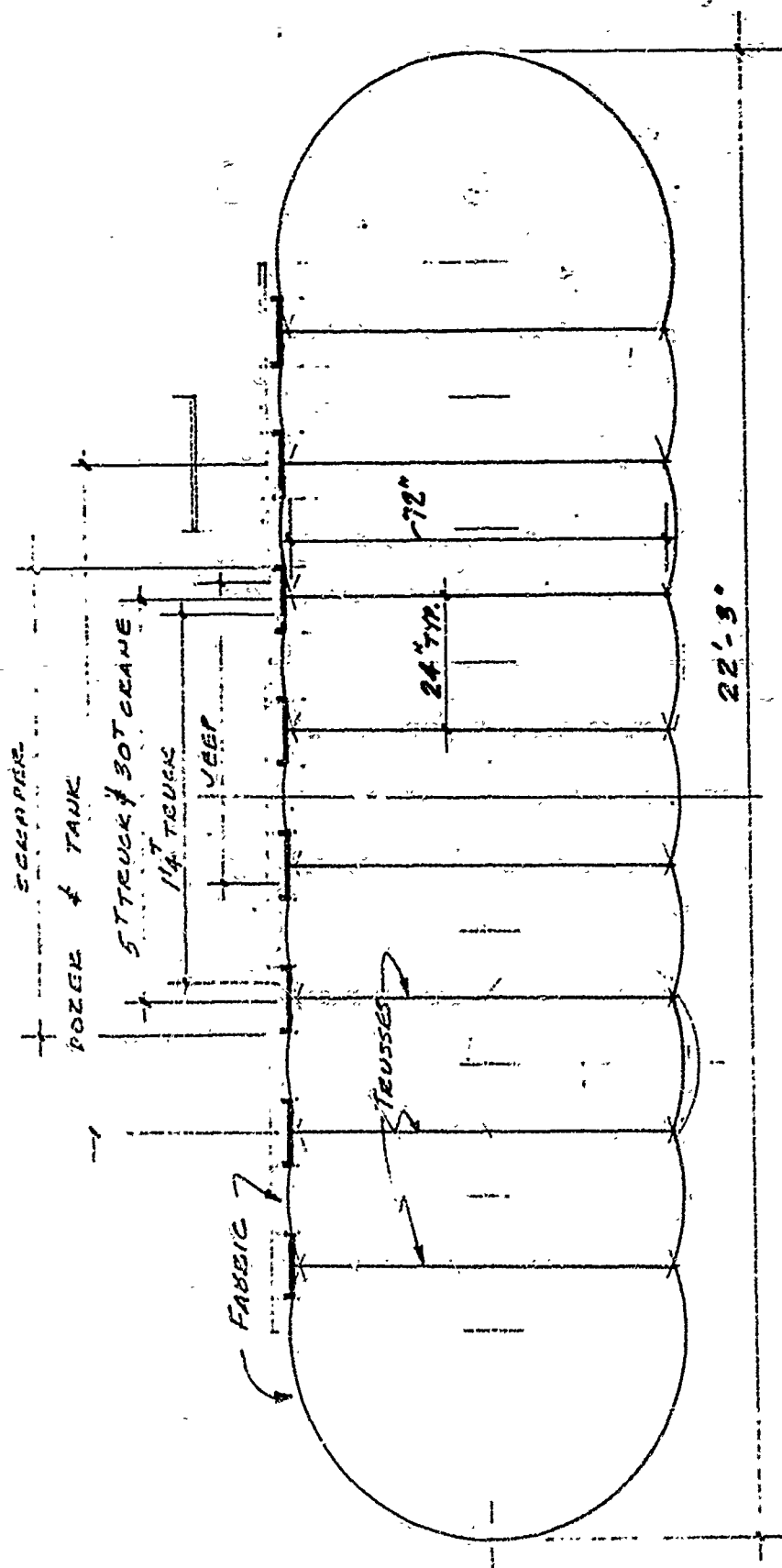


CELLWISE CROSS SECTION

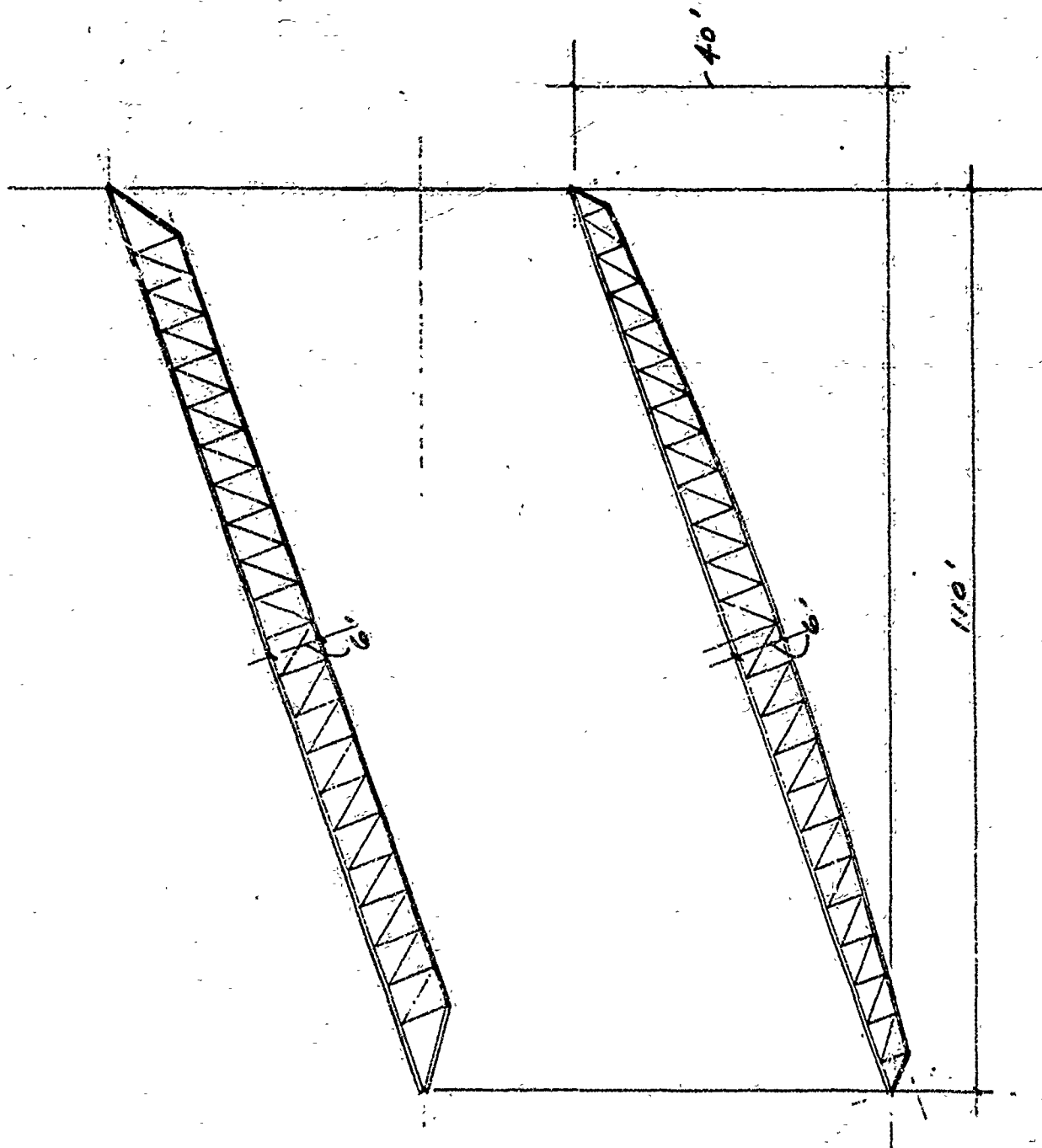
C-79



ALTERNATE TOP CHORD EXTRUSION



RAMP CROSS SECTION



OVERALL DIMENSIONS: 22 FT. W X 5 FT. D

FABRIC STRESS - 161 LBS./IN.

INFLATION PRESSURE - 5 LBS./IN²

VOLUME - $[16 \times 5 + (\pi \times 5)^2 / 4] 110 = 10,960 \text{ FT}^3$

SURFACE AREA (FABRIC) = $[32 + (\pi)(5)] 110 = 5,248 \text{ FT}^2$

APPROX. WT. OF JOISTS = $8 \times 50 \times 110 = 44,000 \text{ LBS.}$

CONCEPT № 10

HYBRID

COMPRESSION DECK

WITH

BLADDER

C-83a

HYBRID STRUCTURE -

ALUMINUM DECK WITH CABLE BELLY AND BLADDER

DESIGN CRITERIA:

LENGTH = 110 FT.

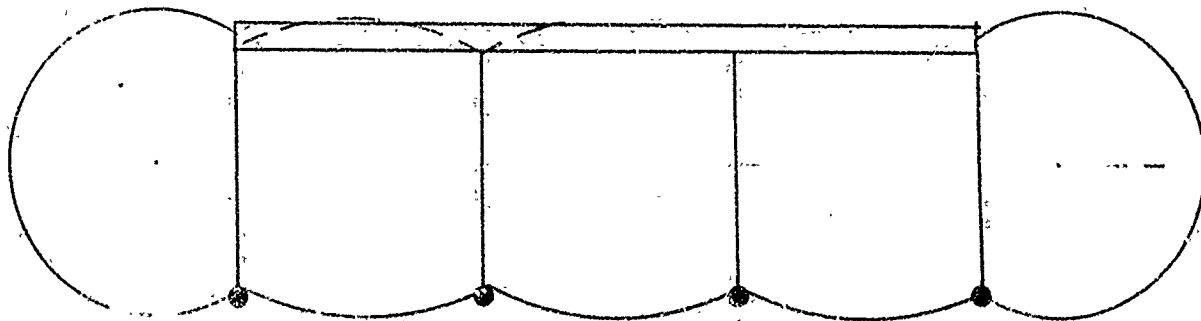
MIN. WIDTH = 16 FT.

MAX. LOAD = 60 TONS

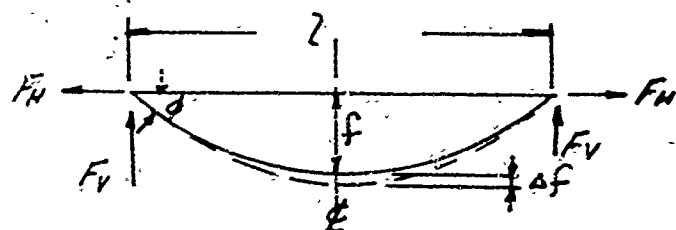
DECK TO TAKE
COMPRESSION

CABLE SLING

INFLATABLE BLADDER



SUSPENSION FORCES -



[FOR STATIC BEHAVIOR IN
CABLES, REF. BETHLEHEM
BOOKLET 2318-A pg. 15]

FOR CONCENTRATED LOAD OF 60 TONS @ MIDSPAN
MOMENT = 3.30×10^6 FT. LBS.

EQUIVALENT UNIFORM LOADING TO PRODUCE THIS MOMENT IS:

$$M = WL^2/8$$

$$W = \frac{8}{(110)^2} (3.30 \times 10^6) = 2181 \text{ LBS./FT.}$$

$$L (\text{CABLE LENGTH}) = \ell \left[1 + \left(\frac{8}{3} \right) \left(\frac{f}{\ell} \right)^2 \right] \quad \text{LET } f = 5 \text{ FT.}$$

$$L = 110 \left[1 + \left(\frac{8}{3} \right) \left(\frac{5}{110} \right)^2 \right] = 110.6 \text{ FT.}$$

$$T (\text{TENSION}) = \frac{WL^2}{8f} \left(1 + 16 \left(\frac{f}{\ell} \right)^2 \right)$$

$$T = \frac{(2181)(110)^2}{(8)(5)} \left[1 + 16 \left(\frac{5}{110} \right)^2 \right] = 681,562 \text{ LBS.}$$

4 CABLES = 170,390 LBS. /CABLE
(CABLE FACTOR OF SAFETY = 2)
BREAKING STRENGTH = 170 TONS

1 11/16" CLASS A - BRIDGE STRAND
(PRESTRETCHED - $E = 29 \times 10^6$ LBS./IN.²)

AREA EA. CABLE = 1.71 IN.²

WT. EA. CABLE = 5.98 LBS./FT.

$$\Delta L = TL/EA$$

$$\Delta L = \frac{(681,562 \text{ LBS.})(110.6 \text{ FT.})(12 \text{ IN./FT.})}{(29 \times 10^6 \text{ LBS./IN.}^2)(1.71 \text{ IN.}^2)(4)}$$

$$\Delta L = 5.51 \text{ IN.}$$

$$\Delta f = \frac{\Delta L}{16/15 (f/\lambda) [5 - 24 (f/\lambda)^2]}$$

$$\Delta f = \frac{3.5 \text{ IN.}}{(16/15) (5/110) [5 - 24 (5/110)^2]}$$

$$\Delta f = 22.96 \text{ IN.} = 1.91 \text{ FT.}$$

$$\tan \phi = \frac{4(f + \Delta f)}{7}$$

$$\tan \phi = \frac{(4)(5 + 1.91)}{110}$$

$$\phi = 14.10^\circ$$

$$F_V = T \sin \phi = (681,562) = \underline{166,095 \text{ LBS.}}$$

$$F_H = T \cos \phi = (681,562) = \underline{661,014 \text{ LBS.}}$$

INFLATION PRESSURE REQD.

$$p = \text{FORCE} / \text{AREA}$$

$$\text{FORCE} = 120,000 \text{ LBS.}$$

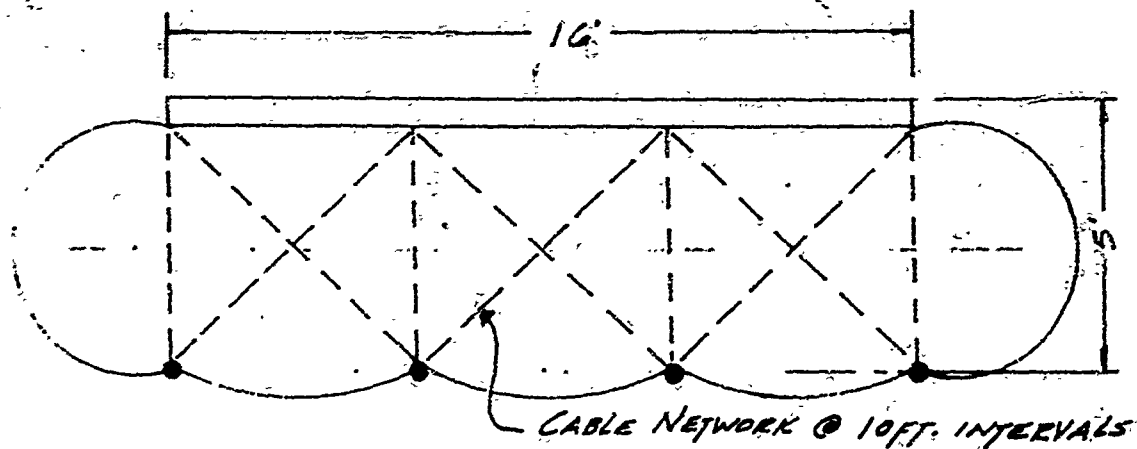
$$\text{AREA} = 16 \text{ FT.} \times 14.5 \text{ FT.} = 232 \text{ FT}^2$$

$$p = \frac{120,000}{(232)(144)} = \underline{3.6 \text{ LBS./IN}^2} \text{ MIN. INFLATION REQD.}$$

$$\text{FABRIC STRESS} = pR \text{ (DUE TO INFLATION)}$$

$$S = (3.6)(2.5')(12 \text{ IN./FT.}) = \underline{108 \text{ LBS./IN.}}$$

INVESTIGATE STRUCTURAL REQUIREMENTS:



$$\text{STRESS}_{(\text{SYSTEM})} = \frac{P}{A} + \frac{MC}{I} \quad \text{COMBINED AXIAL \& BENDING}$$

STRESS DUE TO BUCKLING WILL GOVERN OVER BENDING STRESS.

COMPRESSION MEMBER (DECK) TO BE CONSTRUCTED OF ALUMINUM. (6061-T6) WT. = 174 LBS./FT³

$$P(\text{AXIAL COMPRESSIVE FORCE}) = F_H(\text{CABLE}) = 661,014 \text{ LBS.}$$

$$\text{BENDING MOMENT} = 3.30 \times 10^6 \text{ FT.-LBS. (TANK LOADING AT MIDSPAN)}$$

TRANSFORMED SECTION REQD. TO CALC. INERTIA:

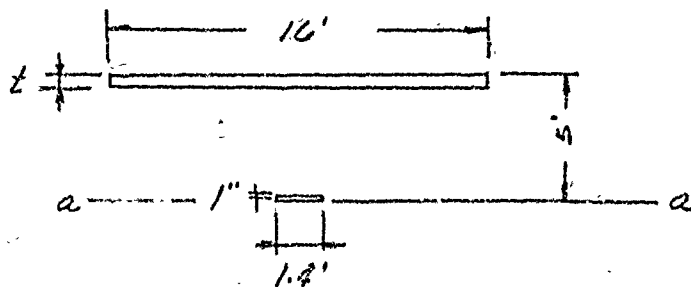
$$E_{\text{CABLE}} = 24 \times 10^6 \text{ LBS./IN}^2$$

$$E_{\text{AL.}} = 10 \times 10^6 \text{ LBS./IN}^2$$

$$\text{TRANSFORM TO ALUMINUM: } \frac{E_C}{E_A} = \frac{24}{10} = 2.4$$

$$\text{AREA CABLES} = (4)(1.71) = 6.84 \text{ IN}^2$$

$$\text{EQUIV. AREA OF ALUM.} = (2.4)(6.84) = 16.4 \text{ IN}^2 \quad \Phi 1 \times 16.4"$$



COMPUTE CENTROID IN TERMS OF t

$$\bar{y} = \frac{\sum Ay}{\sum A} \quad (\text{TAKE MOMENTS ABOUT a-a})$$

$A (in^2)$	$y (in)$	$Ay (in^3)$
16.4	.5	8.2
$192t$	$60 - .5t$	$11,520t - 96t^2$

$$\bar{y} = \frac{-96t^2 + 11,520t + 8.2}{192t + 16.4}$$

LET $t = 1 in$

$$\bar{y} = \frac{(-96)(1) + (11,520)(1) + 8.2}{(192)(1) + 16.4} = 54.86 in.$$

$$I_{TRANSFORMED} = \frac{bh^3}{12} + Ad^2$$

$$\frac{(192)(1)^3}{12} = 16$$

$$+ \frac{4133}{(192)(1)(4.64)^2} = 4149$$

$$\frac{(16.4)(1)^3}{12} = 1.3$$

$$+ (16.4)(1)(54.86)^2 = 48,463$$

$$I_T = 55,612 in^4$$

$$r = \sqrt{I/A}$$

$$A = 192$$

$$+ 16.4$$

$$208.4 in^2$$

$$r = (55,612 / 208.4)^{1/2} = 15.89 in \text{ (ENTIRE SYSTEM)}$$

$$L/r = 200 \text{ OR LESS COMPRESSION MBR.}$$

$$r_{COMP.} = (4149 / 192)^{1/2} = 4.65 in.$$

@ 10' FT. LATERAL SUPPORT

$$r_{REQD.} = \frac{(10)(12)}{200} = .60 in. < 4.65 \text{ OK}$$

$$\begin{aligned}
 \text{COMBINED STRESS} &= \frac{P}{A} + \frac{MC}{I} \\
 &= \frac{661,014}{192} + \frac{(3.30 \times 10^6)(12)(5.14)}{55,612} \\
 &= 3442 + 3660 \\
 &= 7102 \text{ LBS./IN}^2
 \end{aligned}$$

ALLOW. COMBINED STRESS = STRESS DUE TO COMPRESSION
FOR 6061-T6 ALUMINUM.

FROM TEXT - "STATICS & STRENGTH OF MATERIALS" BY
JENSEN & CHENOWETH PG. 304

$$L/r = \frac{K=1}{120/4.65} = 25.8$$

$$\text{ALLOW. STRESS} = 13,000 \text{ LBS./IN}^2 > 7102 \text{ LBS./IN}^2 \text{ OK}$$

OVERALL DIMENSIONS - 22 FT. W X 5 FT. DEEP

FABRIC STRESS - 108 LBS./IN.

INFLATION PRESSURE - 3.6 LBS./IN²

$$\text{VOLUME} = \left[(16 \times 5) + (\pi)(5)^2/4 \right] 110 \left]^{2/3} = 7306 \text{ FT}^3$$

$$\text{FABRIC SURFACE AREA} = (22)(\pi)(5)(22)^{2/3} = 5068 \text{ FT}^2$$

$$\text{WT. OF CABLES} = 4 \times 110.6 \times 5.98 = 2646 \text{ LBS.}$$

APPENDIX - D

REFINED

DESIGN

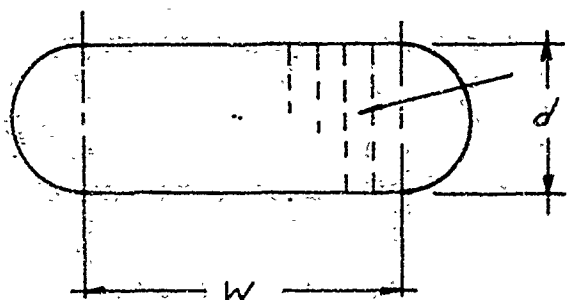
CALCULATIONS

REFINED DESIGN FOR CONCEPT NO. 2

DESIGN DATA:

1. LENGTH = 110 FT.
 2. MIN. WIDTH = 16 FT.
 3. WT. OF ALUM. DECK = 11.34 TONS
 4. APPROX. WT. OF FABRIC = 11 TONS
 5. CONSIDER 1 OR 2 INTERMEDIATE SUPPORTS
 6. REF. BIRDAIR DWG. 7258-3-1 UNDER CONCEPT NO. 2 FOR CONFIGURATION.
- } REF. PRELIM. INVESTIGATION

SUMMARY OF STRESS EQUATIONS (FROM PRELIM. DUAL-WALL BEAM INVESTIGATION)



WEBS CARRY SHEAR
NEGLECT FOR BENDING

$$S_L = \frac{F}{C} = \frac{pA}{C}$$

$$S_L = \frac{p(Wd + \pi d^2/4)}{2W + \pi d}$$

$$S_T = \frac{pd}{2}$$

TERMS:

S_L = FABRIC STRESS DUE TO INFLATION (LONGITUDINAL DIRECTION)

F = FORCE = pA

p = INFLATION PRESSURE

A = CROSS-SECTIONAL AREA

C = CIRCUMFERENCE

S_T = FABRIC STRESS DUE TO INFLATION (TRANSVERSE DIRECTION)

$$f_s = \frac{M}{A} = \frac{M}{(Wd + \pi d^2/4)}$$

TERMS:

f_s = FABRIC STRESS DUE TO BENDING MOMENT

M = BENDING MOMENT

A = CROSS-SECTIONAL AREA

TO PREVENT WRINKLING-

$$f_s = s_i$$

$$\frac{(Wd + \pi d^2/4) \cdot p}{2W + \pi d} = \frac{M}{(Wd + \pi d^2/4)}$$

FOR $W = 16 \text{ FT.} = 192 \text{ IN.}$

$$M = \frac{(192d + \pi d^2/4)^2 \cdot p}{384 + \pi d}$$

EQ. 1

MAX. LONGITUDINAL FABRIC STRESS = $2 s_i$

BENDING MOMENT FOR VARIOUS CONDITIONS-

LOAD

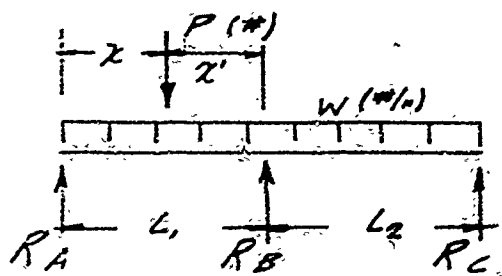
LIVE LOAD = 60 TON MOVING CONCENTRATED LOAD.

DEAD LOAD = 11.34 TONS DECK

APPROX 11.0 TONS FABRIC

$$22.34 \text{ TONS} = 44,680 \text{ LBS} \div 1320 \text{ IN.}$$

$$\underline{\text{DEAD LOAD}} = 33.8 \text{ LBS./IN.}$$



TWO SPAN - CONTINUOUS

(ASSUME R_B IS A RIGID SUPPORT)

SOLVE BY THREE-MOMENT EQUATION:

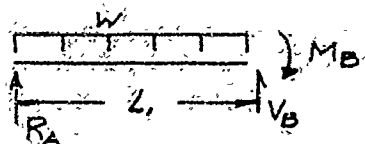
BENDING MOMENT CREATED BY DEAD LOAD

$$2M_B(L_1 + L_2) = -\frac{1}{4}(WL_1^3 + WL_2^3)$$

$$\text{FOR } L = 660 \text{ IN } W = 33.8 \text{ LBS./IN.}$$

SOLVE FOR M_B

$$M_B = -1,840,410 \text{ IN.-LBS.}$$



$$\uparrow \Sigma M_B = 0 = R_A(L_1) + M_B - (W)(L_1/2)$$

$$\text{SOLVE FOR } R_A \text{ WITH } L_1 = 660 \text{ IN } M_B = 1,840,410$$

$$R_A = 8365.5 \text{ LBS.}$$

$$\uparrow \Sigma F_V = 0 = R_A + V_B - WL_1 \quad V_B = 13,942.5 \text{ LBS.}$$

BECAUSE OF SYMMETRY -

$$R_A = R_C = 8365.5 \text{ LBS.}$$

$$R_B = 2V_B = 27,885 \text{ LBS.}$$

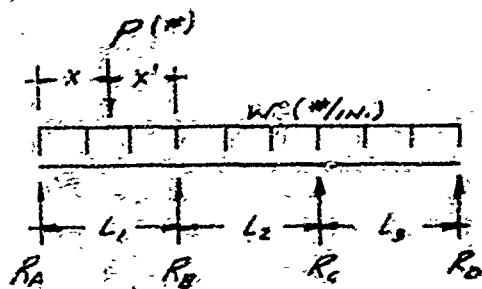
$$\left[\begin{array}{l} \text{MOMENT (DEAD LOAD)} = (R_A)(x) - (W)(x^2/2) \\ \text{FOR ANY POINT } x \leq 660 \text{ IN.} \end{array} \right]$$

BENDING MOMENT CREATED BY MOVING LIVE LOAD

REF. A.I.S.C. STEEL MANUAL

$$M_{\text{MAX. (AT POINT OF LOAD)}} = \frac{P(x)(x')}{4(L_1)^3} (4L_1^2 - x(L_1 + x))$$

$$M_1 \text{ (AT SUPPORT } R_B) = -\frac{P(x)(x')}{4(L_1)^2} (L_1 + x)$$



3 SPAN CONTINUOUS

(ASSUME R_B AND R_C ARE RIGID SUPPORTS)

BENDING MOMENT FOR DEAD LOAD

REF. AISC STEEL MANUAL -

$$R_A = R_D = .400 WL$$

$$R_B = R_C = 1.10 WL$$

$$\text{MOM. (DEAD LOAD)} = (R_A)(x) - (w)(x^2/2)$$

FOR ANY POINT $x \leq 440$ IN

$$\text{MOM. (DEAD LOAD)} = (.5 WL)(x) - .1 WL^2 - (w)(x^2/2)$$

FOR ANY POINT x WHERE $440 < x \leq 660$

BENDING MOMENT FOR MOVING LIVE LOAD -

SOLVE BY THREE MOMENT EQUATION:

$$2M_B(L_1 + L_2) + M_C L_2^2 = P(x)(x')(1 + \frac{x}{L_1})$$

$$M_B(L_2) + 2M_C(L_2 + L_3) = 0$$

$$\text{FOR } L_1 = L_2 = L_3 = 440 \text{ IN AND } x \leq 440 \text{ IN}$$

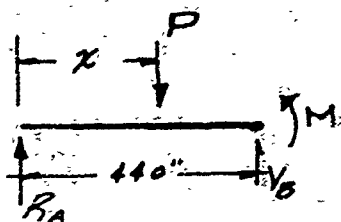
$$M_B = -4M_C$$

$$-3M_C(880) + M_C(440) = -P(x)(440-x)(1 + \frac{x}{440})$$

$$M_C = \frac{1}{6600} \left[P(x)(440-x)(1 + \frac{x}{440}) \right]$$

$$M_B = -\frac{4}{6600} \left[P(x)(440-x)(1 + \frac{x}{440}) \right]$$

NOTE: ONLY FOR $x \leq 440$ IN.



$$\sum M_B = 0 = R_A(440) - P(440 - x) + M_B = 0$$

$$R_A = \frac{1}{440} \left[P(440 - x) - \frac{4}{6600} (P(x)(440 - x)(1 + \frac{x}{440})) \right]$$

$$\text{MOM. MAX. (AT POINT OF LOAD)} = R_A(x)$$

FOR $x \leq 440$ IN.

$$\text{MOM. (AT SUPPORT } R_B) = R_A(440) - P(440 - x)$$

NOTE: LOADING OF CONCENTRATED LIVE LOAD IN SPAN NO. 1 CREATES THE MAXIMUM BENDING MOMENTS ON THE BEAM.

Z5=ZJARCH

02/23/ '73 09:15

!LOGIN: 1507BRD,C.

ID= F

!BASIC

>LOAD TWO

>LIST

10 PRINT"THIS IS A PRINT OUT FOR BENDING MOMENT ON A TWO SPAN"

12 PRINT"CONTINUOUS BEAM WITH A CONCENTRATED LIVE LOAD MOVING"

13 PRINT"ACROSS THE BEAM."

15 PRINT

20 PRINT"THE CONCENTRATED LIVE LOAD (LBS)="

30 INPUT P

40 PRINT"THE DEAD LOAD OF THE RAMP(LBS/IN)="

50 INPUT W

60 PRINT

70 PRINT"DISTANCE

TOTAL

TOTAL"

80 PRINT"ALONG

MOMENT

MOMENT"

90 PRINT"THE RAMP

AT LOAD

AT SUPPORT"

100 PRINT" (IN)

(IN-LBS)

(IN-LBS)"

101 PRINT

105 FOR X=60 TO 660 STEP 30

110 M1=(8365.5*X)-((W*(X+2))/2)

120 M2=(8365.5*660)-((W*(660+2))/2)

130 M3=((P*X*(660-X))/(4*(660+3)))*((4*(660+2))-(X*(660+X)))

140 M4=((P*X*(660-X))/(4*(660+2)))*(660+X)*-1

150 M5=M1+M3

160 M6=M2+M4

170 PRINT X,M5,M6

180 NEXT X

190 END

>SYS

!BYE

02/23/ '73 09:17

CLT 2

CCU 0.018

PROGRAM LISTING

*
!BASIC
>LOAD TWO
>RUN

14:52 02/22

THIS IS A PRINT OUT FOR BENDING MOMENT ON A TWO SPAN
CONTINUOUS BEAM WITH A CONCENTRATED LIVE LOAD MOVING
ACROSS THE BEAM.

THE CONCENTRATED LIVE LOAD (LBS)=

?120000

THE DEAD LOAD OF THE RAMP (LBS/IN)=

?33.8

DISTANCE ALONG THE RAMP (IN)	TOTAL MOMENT AT LOAD (IN-LBS)	TOTAL MOMENT AT SUPPORT (IN-LBS)
60	6.82426E+06	-3.62553E+06
90	9.58194E+06	-4.49020E+06
120	1.19094E+07	-5.32140E+06
150	1.38138E+07	-6.10797E+06
180	1.53041E+07	-6.83876E+06
210	1.63917E+07	-7.50260E+06
240	1.70896E+07	-8.08834E+06
270	1.74130E+07	-8.58483E+06
300	1.73793E+07	-8.98091E+06
330	1.70077E+07	-9265410
360	1.63195E+07	-9.42719E+06
390	1.53379E+07	-9.45508E+06
420	1.40885E+07	-9.33793E+06
450	1.25985E+07	-9.06458E+06
480	1.08973E+07	-8.62388E+06
510	9.01652E+06	-8.00467E+06
540	6.98948E+06	-7.19578E+06
570	4.85173E+06	-6.18607E+06
600	2.64078E+06	-4.96438E+06
630	396211.	-3.51954E+06
660	-1840410	-1840410

190 HALT
>SYS

COMPUTERSEARCH

02/23/ '73 08:53

!LOGIN: 1507BRD,C,

ID= D

!BASIC

>LOAD CONY

CONY

UNABLE TO OPEN

>LOAD CONT

>LIST

PROGRAM LISTING

10 PRINT"THIS IS A PRINT OUT FOR BENDING MOMENTS ON A THREE"

12 PRINT"SPAN CONTINUOUS BEAM WITH A CONCENTRATED LIVE LOAD"

13 PRINT"MOVING ACROSS THE BEAM."

15 PRINT

20 PRINT"THE CONCENTRATED LIVE LOAD (LBS)="

30 INPUT P

40 PRINT"THE DEAD LOAD OF THE RAMP (LBS/IN)="

50 INPUT W

60 PRINT

65 PRINT"DISTANCE

TOTAL

TOTAL"

70 PRINT" ALONG

MOMENT

MOMENT"

80 PRINT"THE RAMP

AT LOAD

AT 1ST. SUPPORT"

90 PRINT" (IN)

(IN-LBS)

(IN-LBS)"

100 PRINT

110 FOR X=40 TO 440 STEP 20

120 M1=(.4*W*440*X)-(W*((X+2)/2))

130 M2=-.1*W*(440+2)

140 Z=(4/6600)*(P*X*(440-X)*(1+(X/440)))

150 K=(1/440)*((P*(440-X)-Z))

160 M3=K*X

170 M4=(K*440)-(P*(440-X))

180 M5=M1+M3

190 M6=M2+M4

200 PRINT X,M5,M6

210 NEXT X

220 END

>SYS

!BYE

02/23/ '73 08:55

CLT 2

CCU 0.023

IBASIC

>LOAD CONT

>RUN

14:55 02/22

THIS IS A PRINT OUT FOR BENDING MOMENTS ON A THREE
SPAN CONTINUOUS BEAM WITH A CONCENTRATED LIVE LOAD
MOVING ACROSS THE BEAM.

THE CONCENTRATED LIVE LOAD (LBS)=

2120000

THE DEAD LOAD OF THE RAMP (LBS/IN)=

233.8

DISTANCE ALONG THE RAMP (IN)	TOTAL MOMENT AT LOAD (IN-LBS)	TOTAL MOMENT AT 1ST. SUPPORT (IN-LBS)
40	4.45915E+06	-1.92379E+06
60	6.25732E+06	-2.53867E+06
80	7.77222E+06	-3.12974E+06
100	9.00890E+06	-3.68908E+06
120	9.97385E+06	-4.20875E+06
140	1.06750E+07	-4.68081E+06
160	1.11217E+07	-5.09734E+06
180	1.13248E+07	-5.45040E+06
200	1.12966E+07	-5.73205E+06
220	1.10508E+07	-5.934768
240	1.06024E+07	-6.11941E+06
260	9.96818E+06	-6.26924E+06
280	9.16607E+06	-5.98594E+06
300	8.21556E+06	-5.79156E+06
320	7.13756E+06	-5.47817E+06
340	5.95445E+06	-5.03784E+06
360	4.69002E+06	-4.46263E+06
380	3.36952E+06	-3.74462E+06
400	2.01962E+06	-2.87586E+06
420	668470.	-1.84842E+06
440	-654368.	-654368.

220 HALT

>SYS

IBYE

02/22/ '73 14:57

CLT 15

RAD SPACE 1

DISC SPACE 1

CCU 0.152

N:5EJEF KANCH

02/03/ '73 10:35

LOGIN: 1307BRD.C.

JD= F

IBASIC

>10 PRINT"FOR A GIVEN DEPTH AND INFLATION PRESSURE THE RESULTING"

>11 PRINT"BENDING MOMENTS CAN BE SUPPORTED"

>12 PRINT

>16PRINT"THE INFLATION PRESSURE (PSI)="

>17 INPUT P

>20 PRINT" DEPTH BENDING"

>30 PRINT" OF RAMP MOMENT"

>40 PRINT" (IN) (IN-LBS)

40 BAD TEXT STRING

>40 PRINT" (IN) (IN-LBS)"

>50 FOR D=20 TO 150 STEP 10

>60 X=(192*D+.7854*D^2)+2

>70 Y=384+3.14159*D

>80 M=X*P/Y

>90 PRINT D,M

>100 NEXT D

*
 !BASIC
 >LOAD STRESS
 >RUN
 16:34 02/22

THE FOLLOWING IS A LISTING OF FABRIC STRESSES AND
 INFLATION PRESSURES REQUIRED TO RESIST MAXIMUM BENDING
 MOMENTS.

THE MAX. BENDING MOMENT (IN-LBS)=

?17413000

DEPTH OF RAMP (IN)	MAXIMUM LONG. STRESS (LBS/IN)	MAXIMUM TRANS. STRESS (LBS/IN)	INFLATION PRESSURE (PSI)
50	3011.98	1761.60	70.4640
100	1287.47	830.548	16.6110
150	749.551	517.244	6.89659
200	498.940	361.696	3.61696
250	358.800	270.082	2.16065
300	271.548	210.569	1.40379

110 HALT

>RUN

16:36 02/22

THE FOLLOWING IS A LISTING OF FABRIC STRESSES AND
 INFLATION PRESSURES REQUIRED TO RESIST MAXIMUM BENDING
 MOMENTS.

THE MAX. BENDING MOMENT (IN-LBS)=

?11324800

DEPTH OF RAMP (IN)	MAXIMUM LONG. STRESS (LBS/IN)	MAXIMUM TRANS. STRESS (LBS/IN)	INFLATION PRESSURE (PSI)
50	1958.88	1145.68	45.8273
100	837.323	540.159	10.8032
150	487.481	336.398	4.48530
200	324.493	235.234	2.35234
250	233.351	175.652	1.40521
300	176.605	136.946	.912976

110 HALT

>SYS

!BYE

02/22/ 73 16:37

CLT 13

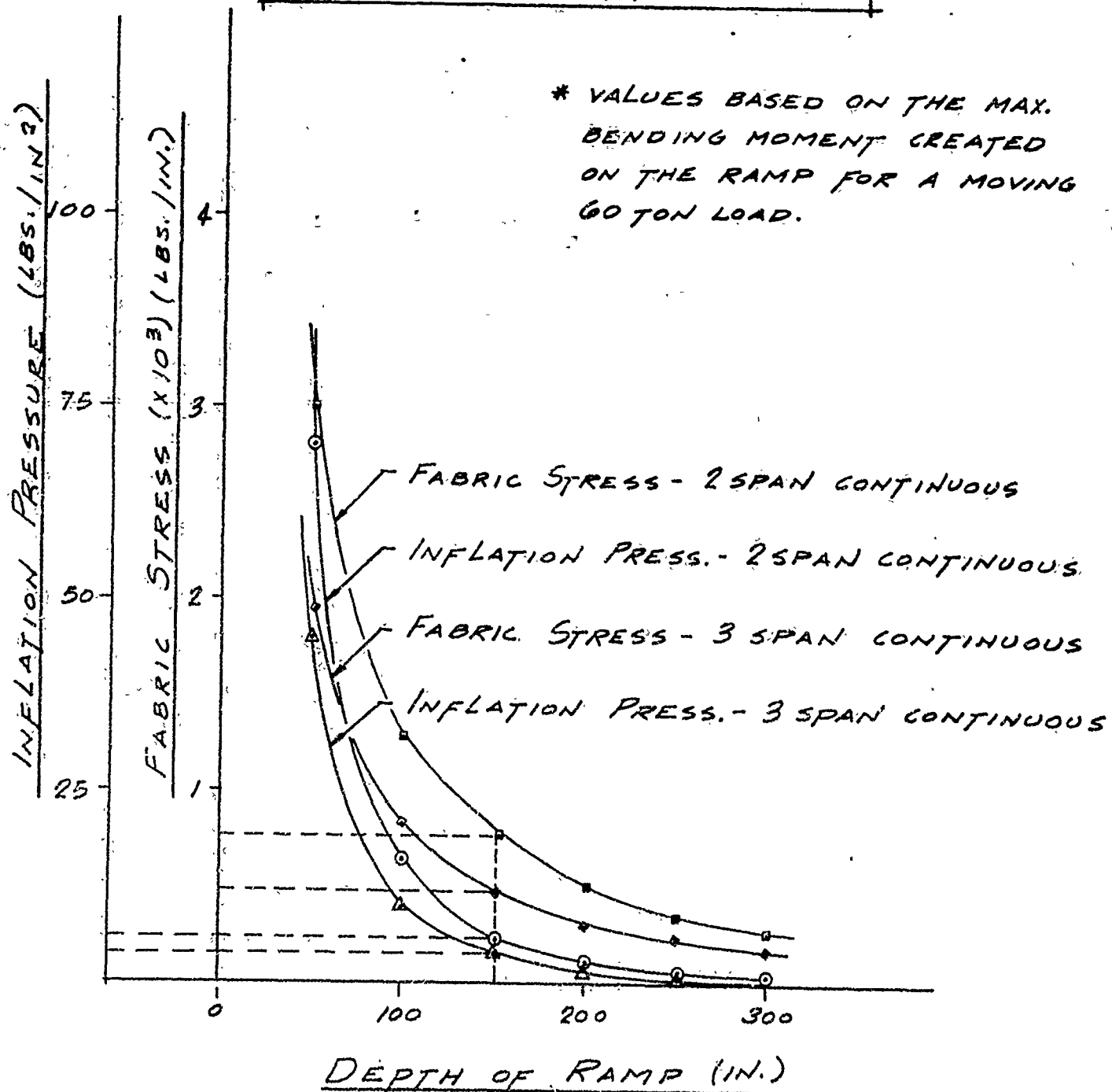
RAD SPACE 2

DISC SPACE 1

CCU 0.110

D-11

INFLATION PRESSURE AND MAX. LONGITUDINAL FABRIC STRESS VS. DEPTH *



FOR MAX. DEPTH = 150 IN.

2 SPAN CONT.

3 SPAN CONT.

MAX. LONG. FABRIC STRESS = 749.6 LBS/IN. MAX. LONG. FABRIC STRESS = 487.5 LBS/IN.
MAX. TRANS. FABRIC STRESS = 517.2 LBS/IN. MAX. TRANS FABRIC STRESS = 336.4 LBS/IN.
INFLATION PRESSURE = 6.90 LBS./IN.² INFLATION PRESSURE = 4.5 LBS/IN.²

10:40 02/23

FOR A GIVEN DEPTH AND INFLATION PRESSURE THE RESULTING
BENDING MOMENTS CAN BE SUPPORTED

THE INFLATION PRESSURE (PSI)=

26.9

DEPTH OF RAMP (IN)	BENDING MOMENT (IN-LBS)
20	266484.
30	603369.
40	1.08122E+06
50	1.70517E+06
60	2.48100E+06
70	3.41498E+06
80	4.51377E+06
90	5.78428E+06
100	7.23365E+06
110	8.86920E+06
120	1.06984E+07
130	1.27287E+07
140	1.49678E+07
150	1.74235E+07

110 HALT

>RUN

10:42 02/23

FOR A GIVEN DEPTH AND INFLATION PRESSURE THE RESULTING
BENDING MOMENTS CAN BE SUPPORTED

THE INFLATION PRESSURE (PSI)=

24.5

DEPTH OF RAMP (IN)	BENDING MOMENT (IN-LBS)
20	173794.
30	390502.
40	705143.
50	1.11206E+06
60	1.61804E+06
70	2.22714E+06
80	2.94376E+06
90	3.77236E+06
100	4.71760E+06
110	5.78426E+06
120	6.97719E+06
130	8.30132E+06
140	9.76163E+06
150	1.13631E+07

110 HALT

!BASIC

>SYS

!BYE

02/23/ '73 10:44

CLT 8

CCU 0.024

D-13

*
!BASIC
>LOAD TWO
>RUN

14:52 02722

THIS IS A PRINT OUT FOR BENDING MOMENT ON A TWO SPAN
CONTINUOUS BEAM WITH A CONCENTRATED LIVE LOAD MOVING
ACROSS THE BEAM.

THE CONCENTRATED LIVE LOAD (LBS)=

?120000

THE DEAD LOAD OF THE RAMP (LBS/IN)=

?33.8

DISTANCE ALONG THE RAMP (IN)	TOTAL MOMENT AT LOAD (IN-LBS)	TOTAL MOMENT AT SUPPORT (IN-LBS)	REQD. DEPTH P = 6.9 PSI
60	6.82426E+06	-3.62553E+06	97
90	9.58194E+06	-4.49020E+06	114
120	1.19094E+07	-5.32140E+06	126
150	1.38138E+07	-6.10797E+06	135
180	1.53041E+07	-6.83876E+06	140
210	1.63917E+07	-7.50260E+06	146
240	1.70896E+07	-8.08834E+06	148
270	1.74130E+07	-8.58483E+06	150
300	1.73793E+07	-8.98091E+06	148
330	1.70077E+07	-9.265410	146
360	1.63195E+07	-9.42719E+06	145
390	1.53379E+07	-9.45508E+06 *	140
420	1.40885E+07	-9.33793E+06	136
450	1.25955E+07	-9.06458E+06	128
480	1.08273E+07	-8.62388E+06	122
510	9.01652E+06	-8.00467E+06	114 *
540	6.98948E+06	-7.19578E+06	↑ ↓
570	4.85173E+06	-6.18607E+06	
600	2.64078E+06	-4.96438E+06	
630	396211	-3.51954E+06	
660	-1840410	-1840410	114

190 HALT

>SYS

* GOVERNS FOR MIN. DEPTH
AT SUPPORT

!BASIC
 >LOAD CONT
 >RUN

14:55 02/22

THIS IS A PRINT OUT FOR BENDING MOMENTS ON A THREE
 SPAN CONTINUOUS BEAM WITH A CONCENTRATED LIVE LOAD
 MOVING ACROSS THE BEAM.

THE CONCENTRATED LIVE LOAD (LBS)=
 ?120000
 THE DEAD LOAD OF THE RAMP (LBS/IN)=
 ?33.8

DISTANCE ALONG THE RAMP (IN)	TOTAL MOMENT AT LOAD (IN-LBS)	TOTAL MOMENT AT 1ST. SUPPORT (IN-LBS)	REQD. DEPTH P=4.5 PSI
40	4.45915E+06	-1.92379E+06	97
60	6.25732E+06	-2.53867E+06	114
80	7.77222E+06	-3.12974E+06	120
100	9.00890E+06	-3.68908E+06	135
120	9.97385E+06	-4.20875E+06	140
140	1.06750E+07	-4.68081E+06	146
160	1.11217E+07	-5.09734E+06	148
180	1.13248E+07	-5.45040E+06	150
200	1.12966E+07	-5.73205E+06	148
220	1.10508E+07	-5934368	146
240	1.06024E+07	-6.04941E+06	145
260	9.96818E+06	-6.06924E+06 *	140
280	9.16607E+06	-5.98594E+06	136
300	8.21556E+06	-5.79156E+06	128
320	7.13756E+06	-5.47817E+06	122
340	5.95445E+06	-5.03784E+06	114 *
360	4.69002E+06	-4.46263E+06	↑
380	3.36952E+06	-3.74462E+06	
400	2.01962E+06	-2.87586E+06	
420	668470.	-1.84842E+06	
440	-654368.	-654368.	

220 HALT
 >SYS

* GOVERNS FOR MIN. DEPTH
 AT SUPPORT

!BYE
 02/22/ '73 14:57
 CLT 15
 RAD SPACE 1
 DISC SPACE 1
 CCU 0.152

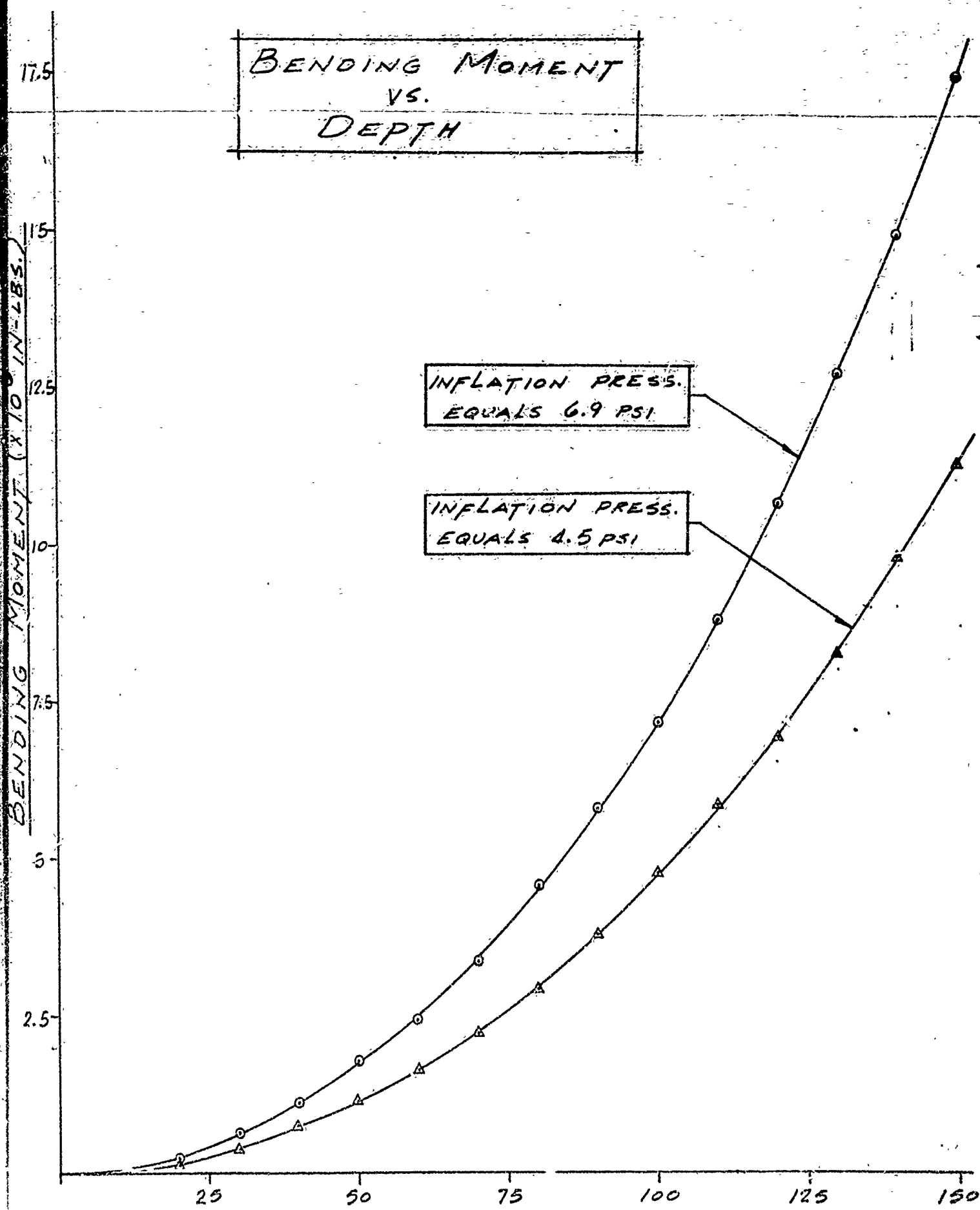
BENDING MOMENT
VS.
DEPTH

BENDING MOMENT ($\times 10^3$ IN-LBS.)

INFLATION PRESS.
EQUALS 6.9 PSI

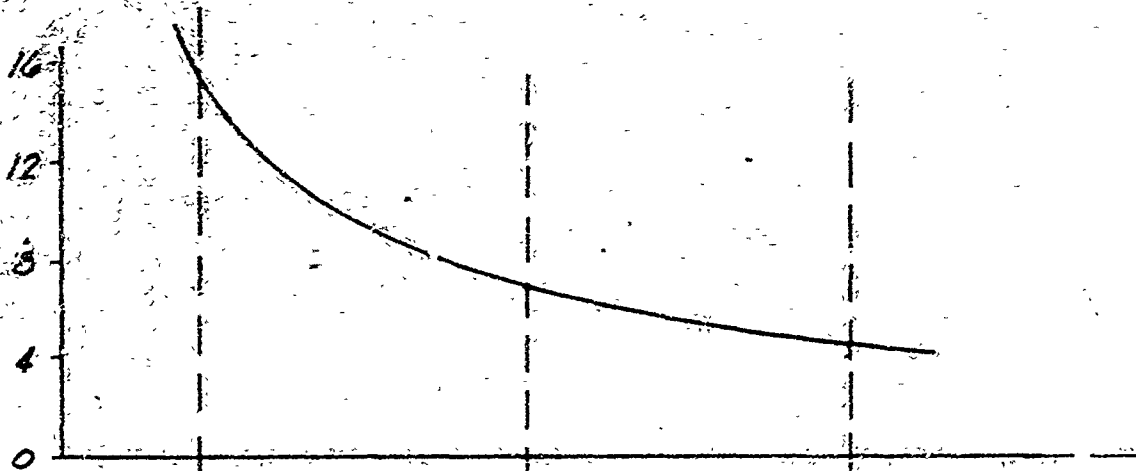
INFLATION PRESS.
EQUALS 4.5 PSI

DEPTH (IN.)

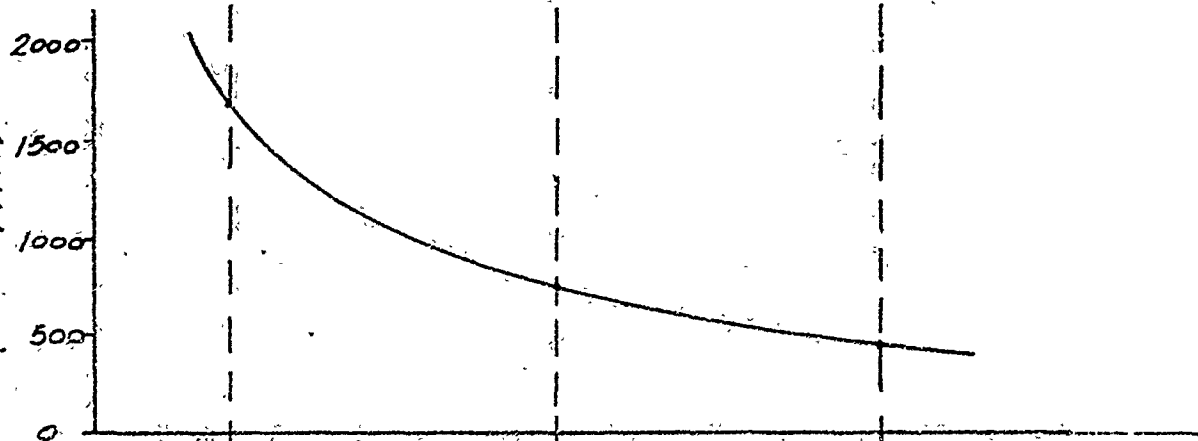


EFFECT OF INTERMEDIATE SUPPORTS

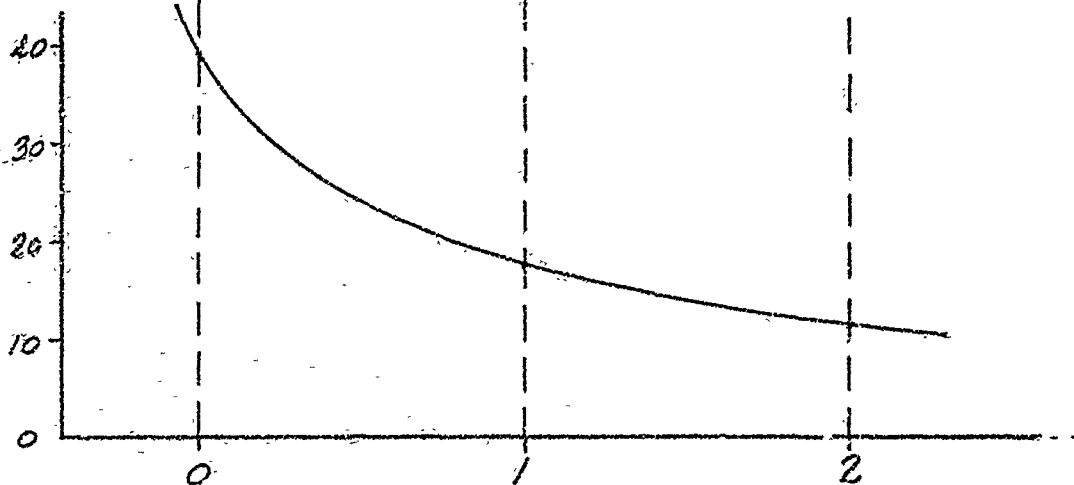
INFLATION PRESSURE
(LBS./IN.^2)



FABRIC STRESS
(LBS./IN.)



BINDING MOMENT
($\times 10^6 \text{ IN.-LBS.}$)



NO. OF INTERIOR SUPPORTS

DEFLECTION OF RAMP UNDER MOVING LOAD

GENERAL DEFLECTION EQUATION:

$$\delta = \frac{(V)(x)}{pA}$$

WHERE:

δ = DEFLECTION (DUE TO SHEAR, NOT FLEXURE)

V = SHEAR AT POINT IN QUESTION

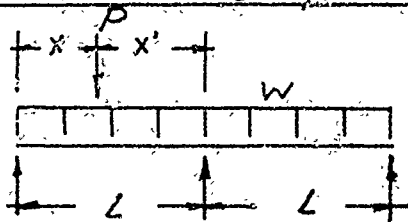
x = DISTANCE FROM POINT IN QUESTION TO SUPPORT.

p = INFLATION PRESSURE

A = CROSS-SECTIONAL AREA AT POINT IN QUESTION.

DETERMINE SHEAR (V) AT ANY POINT ALONG RAMP:

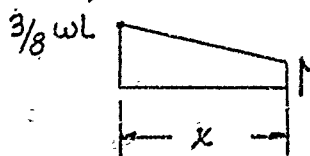
TWO SPAN CONTINUOUS:



FOR LIVE LOAD

$$V_{L.L.} = \frac{Px'}{4L^3} (4L^2 - x(L+x)) \quad \text{REF. AISC STEEL MANUAL}$$

FOR DEAD LOAD



$$V_{D.L.} = \frac{3}{8} w - wx$$

TOTAL SHEAR (V) = $V_{L.L.} + V_{D.L.}$
(AT ANY POINT x)

09:00 02/26

THIS PRINT OUT IS A LISTING OF THE SHEAR VALUE (V) AS
A CONCENTRATED LIVE LOAD MOVES ACROSS THE BEAM

THE CONCENTRATED LIVE LOAD (LBS)=

?120000

THE DEAD LOAD OF THE RAMP (LBS/IN)=

?33.8

THE SPAN (IN)=

?660

DISTANCE ALONG RAMP (IN)	SHEAR (V) (LBS)	CONSTANT (V*X)/PRESS. (CU-IN)	DEPTH (IN) *	DEFLECTION (IN)
60	112724.	980206.	97	22.7
90	104945.	1.36885E+06	114	42.6
120	97217.1	1.69073E+06	126	46.1
150	89556.8	1.94689E+06	135	48.4
180	81981.0	2.13863E+06	140	50.6
210	74506.6	2.26759E+06	146	50.6
240	67150.6	2.33567E+06	148	51.2
270	61450.8	2.40460E+06	150	51.7
300	56410.1	2.45261E+06	148	53.8
330	51538.5	2.46488E+06	146	55.1
360	46852.8	2.44450E+06	145	55.1
390	42370.0	2.39483E+06	140	56.7
420	38107.0	2.31956E+06	136	57.1
450	34080.6	2.22265E+06	128	59.4
480	30307.8	2.10837E+06	122	60.0
510	26805.4	1.98127E+06	114	61.7
540	23590.5	1.84621E+06	114	57.5
570	20679.8	1.70833E+06	114	53.2
600	18090.3	1.57307E+06	114	47.0
630	15838.9	1.44616E+06	114	55.1
660	13942.5	1.33363E+06	114	

200 HALT

>SYS

!BYE

02/26/ '73 09:02

CLT 4

CCU 0.074

CROSS-SECTIONAL AREA (A) = $WD + \frac{\pi D^2}{4}$
FOR W = 192 IN.

FINAL CONFIGURATION FOR CONCEPT N^o. 2

3 SPAN CONTINUOUS BEAM MOST DESIRABLE

INFLATION PRESS. REQD. = 4.5 LBS./IN.²

MAX. FABRIC STRESS = 487.5 LBS/IN (OUTER SKIN)

FOR FACTOR OF SAFETY = 3

FABRIC STRENGTH REQUIRED = (487.5)(3) = 1463 LBS./IN.
(FOR OUTER SKIN)

BEARING LENGTH REQD. EA. END:

DECK DISTRIBUTES LOAD OVER FULL WIDTH = 192"

$$L_{REQD} = 120,000 \text{ LBS} / (4.5 \text{ */IN}^2)(192 \text{ IN.}) = 139 \text{ IN.}$$

SHEAR FORCE ON WEBS:

MAX. SHEAR OCCURS AT 1ST. INTERIOR SUPPORT

DEPTH AT SUPPORT - 114 IN

SHEAR VALUE WITH LOAD AT SUPPORT

$$L.L. = 120,000 \text{ LBS}$$

$$D.L. = 1.10 WL = (1.10)(33.8)(440) = 16,359 \text{ LBS}$$

(CONSERVATIVE SINCE THE BEARING
ON EACH END REDUCES THE D.L.
SHEAR VALUE)

$$\text{TOTAL SHEAR} = 136,359 \text{ LBS.}$$

SHEAR FORCE ON WEBS:

FOR WEB SPACING = 12 IN.

NO. OF WEBS = $16/1 = 16 + 1 = 17$ WEBS REQD.

SHEAR FORCE PER WEB = $136,359/17 = 8021$ LBS.

STRESS PER WEB (BIAS PLY) = $8021/(114)(1.414) = 50$ LBS./IN

STRESS PER WEB (ST. PLY) = $(12)(4.5) = 54$ LBS./IN.

FACTOR OF SAFETY = 3

FABRIC STRENGTH REQD. (BIAS PLY) = 150 LBS./IN

FABRIC STRENGTH REQD. (ST. PLY) = 162 LBS./IN

INTERIOR SUPPORT MECHANISM -

NOTE: FOR CONSERVATIVE DESIGN APPROACH, CONSIDER THE SPAN EQUAL TO 440 IN. DO NOT CONSIDER THE EFFECTS OF THE 130 IN. BEARING LENGTH ON THE ENDS.

TO CONTROL DEFLECTION OF THE SUPPORT DUE TO BUOYANCY, AND STILL BE FLEXIBLE ENOUGH TO ACCOMMODATE VARYING RAMP ANGLES, A CIRCULAR HORIZONTAL TUBE SEEMS MOST PRACTICAL.

MAX. LOAD AT SUPPORT

L.L. = 120,000 LBS.

D.L. = $(1.10)(33.8)(440) = 16,359$ LBS

TOTAL LOAD = 136,359 LBS.

INTERIOR SUPPORT MECHANISM

FOR BUOYANCY

$$F = \gamma V$$

V = VOLUME DISPLACED

$$\gamma = 62.4 \text{ LBS./FT}^3$$

$$F = \text{LOAD}$$

$$V = F/\gamma = 136,359/62.4 = 2185 \text{ FT}^3$$

IF WHOLE TUBE SUBMERGED

$$D_{(\text{MIN.})} = \sqrt{V/4\pi} = \sqrt{2185/4\pi} = 13.2 \text{ FT}$$

\therefore FOR $1/4$ OF TUBE SUBMERGED, 50 FT \pm DIA. REQD.

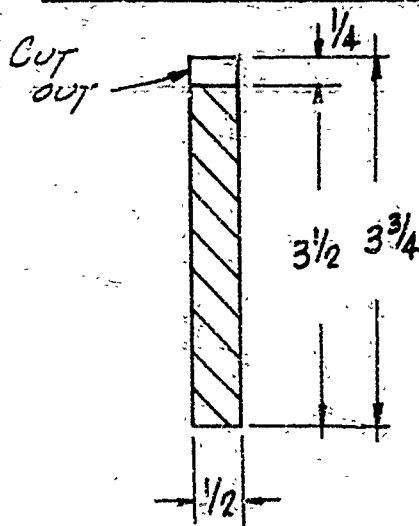
NOTE: HORIZONTAL SUPPORT TUBE INFEASIBLE

REFINED DESIGN FOR CONCEPT N^o 10

DESIGN DATA:

1. LENGTH = 110 FT. = 1320 IN.
2. MIN. WIDTH = 16 FT. = 192 IN.
3. ALUMINUM DECK TO TAKE COMPRESSION
4. CABLES TO CARRY TENSION
5. REFERENCE BIRDAIR DWG. FIGURE 3, CONCEPT N^o 10 FOR GENERAL CONFIGURATION

DESIGN PROPERTIES OF EXISTING ALUMINUM DECK (TO BE USED AS COMP. MBR.)



TYPICAL BAR

CNTR. TO CNTR. SPACING
- 6" LONG. DIR.
- 3" TRANS. DIR.

ASSUME 6061-T6 ALUMINUM
FOR FULLY SUPPORTED, ALLOW.
COMPRESSIVE STRESS = 14 KSI

FOR WIDTH = 16 FT. = 192 IN.

$$N^o \text{ OF BARS} = \frac{192}{3} = 64 + 1 = 65 \text{ BARS}$$

$$\text{TOTAL COMPRESSIVE FORCE} = (\text{STRESS})(\text{AREA})$$

$$\text{ALLOW. COMP. FORCE} = (14,000)(.5)(3.5)(65)$$

$$\text{ALLOW. COMP. FORCE} = 1.5925 \times 10^6 \text{ LBS.}$$

$$\text{SECTION MODULUS} = \frac{bd^2}{6} \text{ (PER BAR)}$$

$$S = \frac{(.5)(3.5)^2}{6} = 1.028 \text{ IN}^3 \text{ PER BAR}$$

DESIGN PROPERTIES OF EXISTING ALUMINUM DECK

WEIGHT PER SQ. FT. =

$$6 \text{ BARS} \times 12" \text{ LONG} \times .5 \times 3.75 = 135 \text{ IN.}^3$$

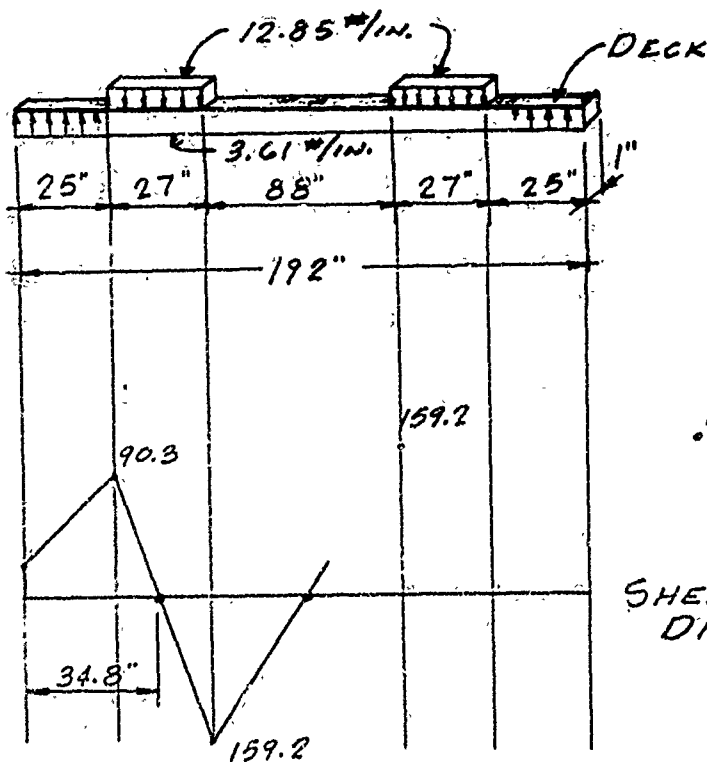
$$\text{ALUM.} = 165 \text{ LBS./C.F.} = .0955 \text{ LBS./IN.}^3$$

$$\text{WT. PER. SQ. FT.} = (135)(.0955) = \underline{12.89 \text{ LBS./S.F.}}$$

$$\text{TOTAL WT. OF DECK} = (16)(110)(12.89)/2000 = \underline{11.34 \text{ TONS}}$$

CHECK CAPACITY OF DECK TO DISTRIBUTE VARIOUS LOADS:

1. TANK LOADING (TRANS. DIRECTION)



60 TON TANK = 12.85 PSI
TRACK PRESS.

FOR 1" WIDE STRIP
LOAD = 12.85 LBS./IN.

$$\Sigma F_v = 0$$

$$\therefore (W)(192) = (2)(12.85)(27)$$

$$W = 3.61 \text{ LBS./IN.}$$

SHEAR
DIAGRAM

$$\frac{249.5}{27} = \frac{90.3}{x}$$

$$x = 9.8 \text{ IN.}$$

$$\begin{aligned} \text{BENDING MOM.} &= (3.61)(34.8)(34.8/2) - (12.85)(9.8)(9.8/2) \\ @ 34.8" &= 556.7 \text{ IN.-LBS} \end{aligned}$$

$$\begin{aligned} \text{BENDING MOM.} &= (3.61)(96)(96/2) - (12.85)(27)(44 + 13.5) \\ @ \text{CNTR.} &= \underline{3314.8 \text{ IN.-LBS}} \quad \text{GOVERNS} \end{aligned}$$

CHECK CAPACITY OF DECK TO DISTRIBUTE VARIOUS LOADS:

TANK LOADING (CONT.)

ALLOW. BENDING STRESS (6061-T6) ALUMINUM
= 15 KSI

SECTION MODULUS REQD. PER IN. = M/S

$$\begin{aligned} S (\text{PER IN. OF LENGTH}) &= 3315 \text{ IN-LBS} / 15,000 \text{ PSI} \\ &= .2210 \text{ IN}^3 \end{aligned}$$

6" BAR SPACING IN LONG. DIR.

$$S_{\text{REQD}} = 6 \times .2210 = 1.326 \text{ IN}^3$$

$$S_{\text{ACTUAL}} = 1.028 \text{ IN}^3$$

CLOSE - PROBABLY
SATISFACTORY IF FULL
DEPTH IS USED.

2. WHEEL LOADING (TRANS. & LONG. DIR.)

14 C.Y. SCRAPER, TOTAL WT. = 63,500 LBS.

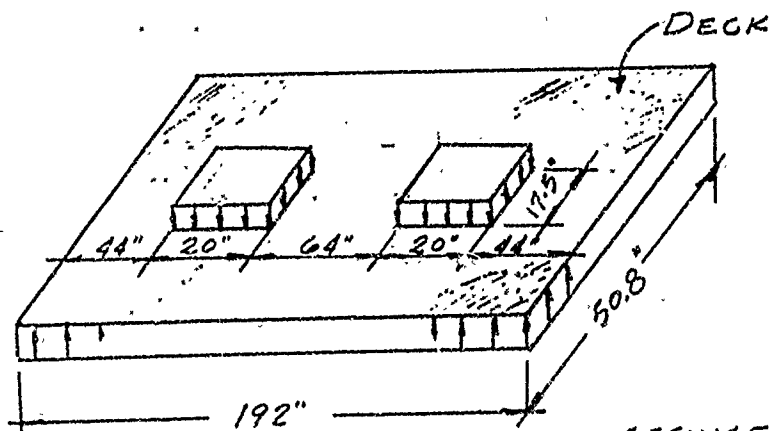
FRONT AXLE = 17,600 LBS./WHEEL

TIRE INFLATION PRESS. \approx 50 PSI

$$\text{AREA OF CONTACT PER WHEEL} = 17,600 / 50 = 350 \text{ IN}^2$$

IF WIDTH OF TIRE = 20 IN.

$$\text{LENGTH OF CONTACT} = 17.5 \text{ IN.} = 3 \text{ BARS LOADED AT ONE TIME}$$



ASSUME TANK INFLATION
PRESS. GOVERNS = 3.61 PSI

$$E F_v = 0$$

$$(2)(17,600) = (3.61)(192)(L)$$

$$L = 50.8 \text{ IN.}$$

CHECK CAPACITY OF DECK TO DISTRIBUTE VARIOUS LOADS:

CANTILEVER CONDITION
CREATES MAX. MOMENT

MAX. BENDING MOM. TRANS. DIR. (M_T) =

$$M_T = \frac{WL^2}{2} = \frac{(21.7)(4.4)^2}{2} = 21,005 \text{ IN.-LBS. } W (\text{PER BAR}) = (3.61)(6) = 21.7 \text{ LBS./IN.}$$

$$S_{\text{REQD.}} = \frac{M}{\sigma} = \frac{21,005}{15,000} = 1.40 \text{ IN.}^3$$

$$S_{\text{ACTUAL}} = 1.028 \text{ IN.}^3$$

SINCE THE BARS ARE
A LITTLE OVERSTRESSED,
THE AREA OF CONTACT
ADJUSTS ITSELF

∴ FULL WIDTH OF DECK
IS NOT STRESSED
WHILE LENGTH OF
CONTACT INCREASES.

CONCLUSION: EXISTING DECK MATERIAL SEEMS STRONG
ENOUGH TO DISTRIBUTE LOCAL LOADS.

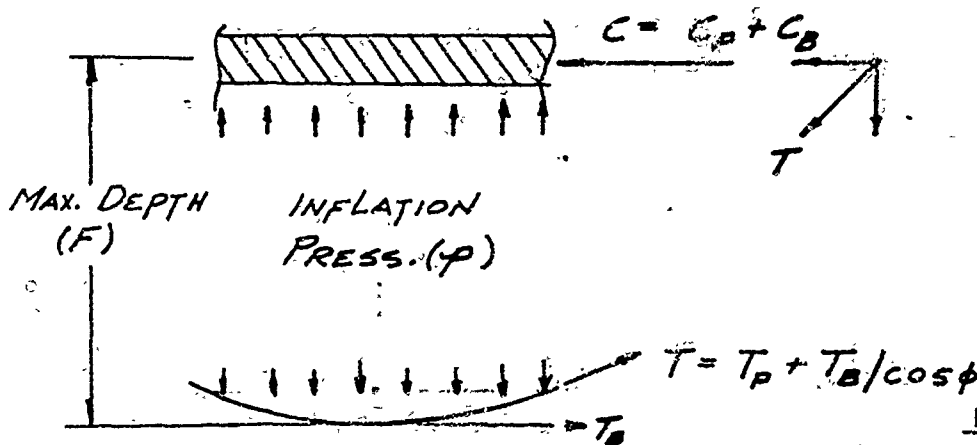
INFLATION PRESSURE TO CARRY 60 TON LOAD

THE MAXIMUM INFLATION PRESSURE EQUALS THE
PRESSURE REQUIRED TO RESIST LOCAL DEFLECTION.

$$\therefore \text{INFLATION PRESSURE} = 3.6 \text{ PSI}$$

NOTE: THIS VALUE IS CONSERVATIVE SINCE THE AREA
OF CONTACT IS 192 IN. WIDE X 174 IN. TRACK
LENGTH. THE ACTUAL LONGITUDINAL LENGTH
IS SOMETHING GREATER THAN 174 IN.

STRESS EQUATIONS:



WHERE:

T = TOTAL TENSION LOAD IN CABLE

T_p = TENSION DUE TO INFLATION PRESSURE

T_b = TENSION DUE TO BENDING MOMENT

C = TOTAL COMPRESSION LOAD IN DECK

C_p = COMPRESSION DUE TO INFLATION PRESSURE

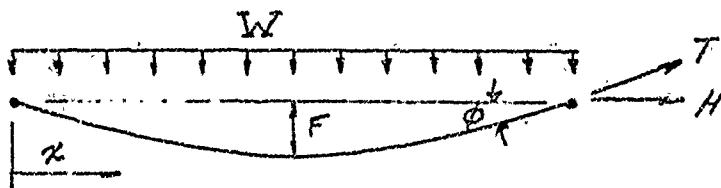
C_b = COMPRESSION DUE TO BENDING MOMENT

NOTE: 1. WEBS TO CARRY VERTICAL STRESS DUE TO INFLATION AND DIAGONAL STRESS DUE TO SHEAR.

2. SHAPE OF CABLE SLING IS TO BE PARABOLIC

STRESS DUE TO INFLATION PRESSURE

CONSIDER UNIFORM LOAD OVER PARABOLIC SHAPED CABLE



REF. TEXT "FRAMES & ARCHES"

$$H_p = \frac{WL}{8F}$$

$$T_p = H \cos \phi + W \left(\frac{1}{2} - \frac{x^2}{L^2} \right) \sin \phi$$

WHERE:

H = HORIZONTAL FORCE

T = CABLE TENSION FORCE

W = TOTAL PRESS. LOAD

L = SPAN LENGTH

F = MAX. DEPTH

x = ANY POINT ALONG SPAN.

STRESS DUE TO INFLATION PRESSURE

TO DETERMINE THE ANGLE ϕ
AT ANY POINT ALONG THE PARABOLA

$$\tan \phi = \frac{4F}{L} \left(1 - \frac{2x}{L}\right)$$

(NEGLECT EFFECT OF PRESSURE ON ENDS)

STRESS DUE TO BENDING MOMENT

$$\text{BENDING MOMENT (M)} = T_B Y = C_B Y$$

WHERE:

Y = DEPTH AT ANY POINT x

$$y = 4F \left(1 - \frac{x}{L}\right) \frac{x}{L}$$

$$\text{COMP. FORCE} = \frac{M}{Y} = C_B$$

$$\text{TENSION FORCE} = \frac{M}{Y} = T_B$$

TOTAL STRESS

$$C = C_P + C_B$$

$$C_P = H_P \text{ (REACTING FORCE)}$$

$$C = \frac{WL}{8F} + \frac{M}{Y}$$

$$T = T_P + T_B / \cos \phi$$

$$T = \frac{WL}{8F} \cos \phi + W \left(\frac{1}{2} - \frac{x}{L}\right) \sin \phi + \frac{M}{Y} \cos \phi$$

BENDING MOMENT ALONG RAMP

LOAD CONDITIONS:

LIVE LOAD - MOVING CONCENTRATED LOAD (P)

DEAD LOAD -

DECK = 11.34 TONS

FABRIC = 5 "

CABLES = 5 TONS

21.34 TONS

FOR WIDTH = 192 IN

DEAD LOAD = 32.3 LBS./IN. = W

REF. A.I.S.C. STEEL MANUAL FOR EQUATIONS:

$$\text{MOM. (D.L.)} = \frac{Wx}{2} (L-x)$$

L = SPAN (IN.)

x = ANY POINT ALONG
SPAN (IN.)

W = DEAD LOAD (LBS./IN.)

$$\text{MOM. (L.L.)} = \frac{Pab}{L} = \frac{Px(L-x)}{L}$$

(AT POINT OF LOAD)

P = CONC. LIVE LOAD (LBS.)

DETERMINE MIN. DEPTH (F) REQD.

TOTAL APPLIED COMP. FORCE = ALLOW. COMP. FORCE
DECK CAN SUPPORT

$$\text{MAX. MOM. } x = L/2$$

$$y = F$$

$$\frac{WL^2}{8F} + \frac{M_T}{F} = 1.5925 \times 10^6$$

$$\begin{aligned} W &= (P)(\text{WIDTH})(L) \\ &= (3.61)(192)(1320) \\ &= 9.149 \times 10^5 \text{ LBS.} \end{aligned}$$

$$F = \frac{WL^2 + 8M_T}{(8)(1.5925 \times 10^6)}$$

$$M_D = \frac{WL^2}{8} = \frac{(32.3)(1320)^2}{8} = 7.034 \times 10^6 \text{ IN-LBS}$$

$$= \frac{(9.149 \times 10^5)(1320)^2 + (8)(46.63 \times 10^6)}{(8)(1.5925 \times 10^6)}$$

$$M_L = \frac{PL}{4} = \frac{(120,000)(1320)}{4} = 39.6 \times 10^6 \text{ IN-LBS}$$

$$F_{\text{MIN.}} = 124 \text{ IN.}$$

$$M_T = 46.63 \times 10^6$$

```

!LOGIN: 1507BRD.C,
ID= D
!BASIC
>LOAD CONCEPT10
>LIST
10 PRINT"THIS PROGRAM COMPUTES THE COMPRESSIVE LOAD ON THE DECK"
11 PRINT"AND THE TENSILE LOAD ON THE CABLES AS A CONCENTRATED"
12 PRINT"LOAD MOVES ACROSS THE RAMP."
15 PRINT
20 PRINT"THE CONCENTRATED LIVE LOAD (LBS)="
30 INPUT P
40 PRINT"THE DEAD LOAD (LBS/IN)="
50 INPUT W
60PRINT"THE REQUIRED INFLATON PRESSURE (PSI)="
70 INPUT Z
72 PRINT"THE MAX. DEPTH AT MIDSPAN (IN)="
73 INPUT F
75 PRINT
80 PRINT"DISTANCE      BENDING      DEPTH OF      TOTAL      TOTAL"
90 PRINT" ALONG      MOMENT      RAMP      COMPRESSIVE TENSILE"
100PRINT" RAMP      (IN-LBS)      (IN)      FORCE      FORCE"
110PRINT" (IN)      (LBS)      (LBS)"
120 PRINT
130 FOR X=30 TO 660 STEP 30
140 Y=4*F*(1-(X/1320))*(X/1320)
150 A1=ATN(((4*F/1320)*(1-((2*X)/1320))))
160 M1=(W*X/2)*(1320-X)
170 M2=(P*X*(1320-X))/1320
180 M=M1+M2
190 T1=M/Y
200 T=T1/COS(A1)
210 Z1=Z*192
220 H1=(Z1*(1320+2))/(8*F)
230 H=H1*COS(A1)
240 T3=T+H*(Z1*1320*(.5-(X/1320)))
250 C=T1+H1
260 PRINT X,M,Y,C,T3
270 NEXT X
280 END
>SYS

```

```

!BYE
02/28/ '73 09:29
CLT 2
CCU 0.024

```

055201SEARCH

02/28/ '73 09:36

TELEPHONE: 15078RD, C.

10- D

1BASIC

>LOAD CONCEPTIO

>RUN

09:36 02/28

THIS PROGRAM COMPUTES THE COMPRESSIVE LOAD ON THE DECK
AND THE TENSILE LOAD ON THE CABLES AS A CONCENTRATED
LOAD MOVES ACROSS THE RAMP.

THE CONCENTRATED LIVE LOAD (LBS)=

2120000

THE DEAD LOAD (LBS/IN)=

722.3

THE REQUIRED INFLATION PRESSURE (PSI)=

23.61

THE MAX. DEPTH AT MIDSPAN (IN)=

2130

DISTANCE ALONG RAMP (IN)	BENDING MOMENT (IN-LBS)	DEPTH OF RAMP (IN)	TOTAL COMPRESSIVE FORCE (LBS)	TOTAL TENSILE FORCE (LBS)
30	4.514319E+06	11.5496	1.51997E+06	1.9068E+06
60	8.09367E+06	22.5620	1.51997E+06	1.89016E+06
90	1.18514E+07	33.0372	1.51997E+06	1.87336E+06
120	1.54165E+07	42.9752	1.51997E+06	1.85644E+06
150	1.87889E+07	52.3760	1.51997E+06	1.83939E+06
180	2.19685E+07	61.2397	1.51997E+06	1.82219E+06
210	2.49555E+07	69.5631	1.51997E+06	1.80484E+06
240	2.77497E+07	77.3554	1.51997E+06	1.78733E+06
270	3.03513E+07	84.6074	1.51997E+06	1.76964E+06
300	3.27601E+07	91.3223	1.51997E+06	1.75177E+06
330	3.4976205	97.5000	1.51997E+06	1.73370E+06
360	3.69996E+07	103.140	1.51997E+06	1.71543E+06
390	3.88303E+07	108.244	1.51997E+06	1.69695E+06
420	4.04683E+07	112.810	1.51997E+06	1.67825E+06
450	4.19136E+07	116.839	1.51997E+06	1.65932E+06
480	4.31662E+07	120.331	1.51997E+06	1.64015E+06
510	4.42261E+07	123.285	1.51997E+06	1.62075E+06
540	4.50933E+07	125.702	1.51997E+06	1.60110E+06
570	4.57670E+07	127.583	1.51997E+06	1.58120E+06
600	4.62495E+07	128.926	1.51997E+06	1.56105E+06
630	4.65386E+07	129.731	1.51997E+06	1.54064E+06
660	46634940	130	1.51997E+06	1.51997E+06

280 HALT

>SYS

1BYE

02/28/ '73 09:40

CLT 4

CCU 0.026

RESULTS FROM COMPUTER RUN:

FOR INFLATION PRESS. = 3.61 P.S.I.

FOR MAX. DEPTH (F) = 130 IN.

COMPRESSIVE FORCE IN DECK = 1.519×10^6 LBS.

ALLOW. COMP. FORCE = 1.592×10^6 LBS. OK

TENSION FORCE IN CABLES = 1.9×10^6 LBS.

SAY 2.0×10^6 AS $X \rightarrow 0$

FOR S.F. = 2

\therefore BREAKING STRENGTH REQD = 4×10^6 LBS.

FOR WEBS AND CABLES @ 12 IN. SPACING

16 CABLES REQD.

BREAKING STRENGTH PER CABLE = 125 TONS

1 7/16" CLASS A BRIDGE STRAND

AREA = 1.24 IN^2 WT. = 4.34 LBS/FT.

PRESTRETCHED E = 24,000,000 PSI

DEFLECTIONS:

ASSUMPTION: DEFLECTION CONTROLLED BY COMPRESSION OF ALUMINUM DECK AND ELONGATION OF STEEL CABLES. FABRIC DOES NOT CONTRIBUTE TO FLEXURAL STIFFNESS.

TRANSFORMED SECTION REQD.

$$E_{ALUM} = 10 \times 10^6 \text{ PSI}$$

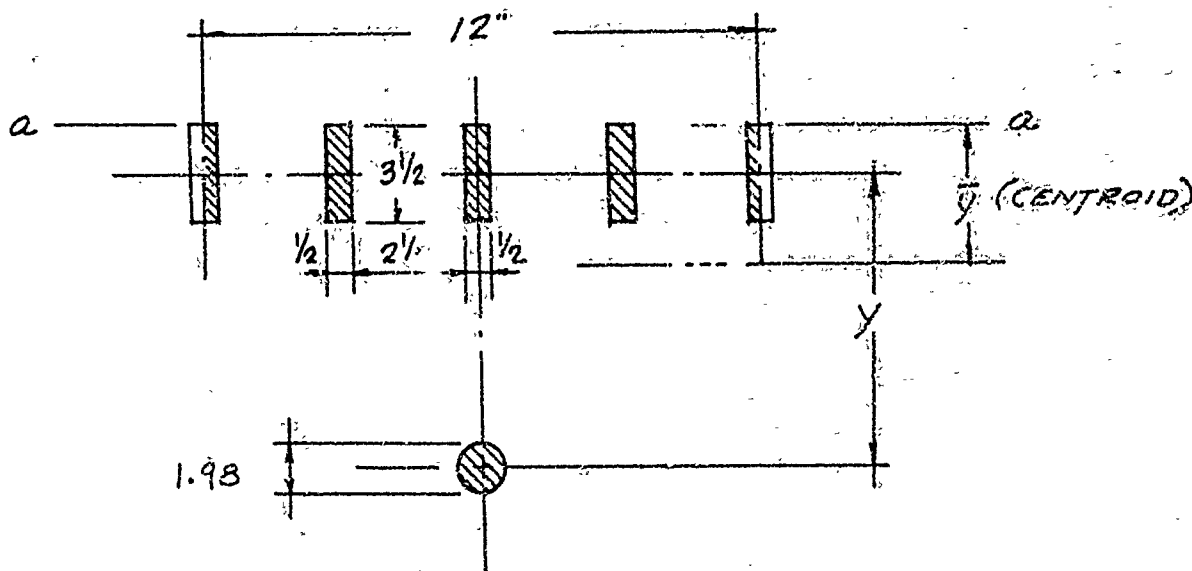
$$E_{CABLE} = 24 \times 10^6 \text{ PSI (PRESTRETCHED)}$$

$$E_c/E_A = 2.4 \text{ (TRANSFORMED TO ALUMINUM)}$$

$$\text{AREA STEEL CABLE} = 1.24 \text{ IN}^2$$

$$\text{EQUIV. AREA ALUM. CABLE} = (1.24)(2.4) = 3.07 \text{ IN}^2$$

$$DIA. = 1.98 \text{ IN.}$$



$$I_T = I_o + A d^2$$

$$I_o (\text{DECK}) = \left(\frac{b d^3}{12} \right) 4 = 4 \left[\frac{(0.5)(3.5)^3}{12} \right] = 7.146 \text{ IN}^4$$

$$I_o (\text{CABLE}) = .0491 (D)^4 = (.0491)(1.98)^4 = .755 \text{ IN}^4$$

DEFLECTIONS:

COMPUTE CENTROID ABOUT a-a

AREA

LEVER ARM

MOM.

$$(4)(.5)(3.2) = 7.00$$

$$1.75$$

$$12.25$$

$$\frac{3.07}{10.07 \text{ in}^2}$$

$$y + 1.75$$

$$\frac{5.37 + 3.07y}{17.62 + 3.07y \text{ in}^3}$$

$$\bar{y} = \frac{M}{A} = 1.75 + .305y$$

TOTAL MOMENT OF INERTIA

$$I_T = I_o + Ad^2$$

$$I_T = 7.146 + (7.00)(\bar{y} - 1.75)^2 + .755 + (3.07)(y + 1.75 - \bar{y})^2$$

DEFLECTION EQUATIONS:

REF. A.I.S.C. STEEL MANUAL

$$\Delta (\text{AT POINT } x) = \frac{w x}{24 EI} (L^3 - 2Lx^2 + x^3)$$

DEAD LOAD

$$\Delta (\text{AT POINT OF LOAD}) = \frac{Pa^2b^2}{3 EIL}$$

LIVE LOAD

$$= \frac{P(x)^2(L-x)^2}{3 EIL}$$

```

0151JERSEARCH
03/22/ '73 09:26
!LOGIN: 1507BRD.C,
ID= B
!BASIC
>LOAD DEFLECTION
>LIST
10 PRINT"THIS PRINT OUT IS A LISTING OF THE DEFLECTION AS A "
11 PRINT"CONCENTRATED LIVE LOAD MOVES ALONG THE RAMP:"
15 PRINT
20 PRINT"THE CONCENTRATED LIVE LOAD (LBS) ="
30 INPUT P
40 PRINT"THE DEAD LOAD (LBS/IN) ="
50 INPUT W
60 PRINT"THE SPAN LENGTH (IN) ="
70 INPUT L
80 PRINT"THE MAXIMUM DEPTH (F) IN INCHES ="
90 INPUT F
100 PRINT
110 PRINT"DISTANCE      MOM. OF      DEFL.      DEFL.      TOTAL
120 PRINT" ALONG      INERTIA      UNDER      UNDER      DEFL."
130 PRINT" RAMP      AT POINT      D.L.      L.L.      (IN)"
140 PRINT" (IN)      (IN4)      (IN)      (IN)"
150 PRINT
160 FOR X=30 TO 660 STEP 30
170 Y=(4*F*(1-(X/L))*(X/L))
180 Y1=1.75+(.305*Y)
190 I=7.146+(7*((Y1-1.75)+2))+.755+(3.07*((Y+1.75-Y1)+2))
195 I=I*16
200 D1=((W*X)/(24*100000000*I))*(L+3-(2*L*X/X)+X+3)
210 D2=(P*(X+2)*((L-X)+2))/(3*100000000*I*L)
220 D3=D1+D2
230 PRINT X,I,D1,D2,D3
240 NEXT X
250 END
>SYS

!BYE
03/22/ '73 09:28
CLT 1
CCU 0.026

```

COMPUTERSEARCH
03/13/ '73 10:00
LOGIN: 1507BRD,C,
ID= F

BASIC

>LOAD DEFLECTION

>195 I=I*16

>RUN

10:01 03/13

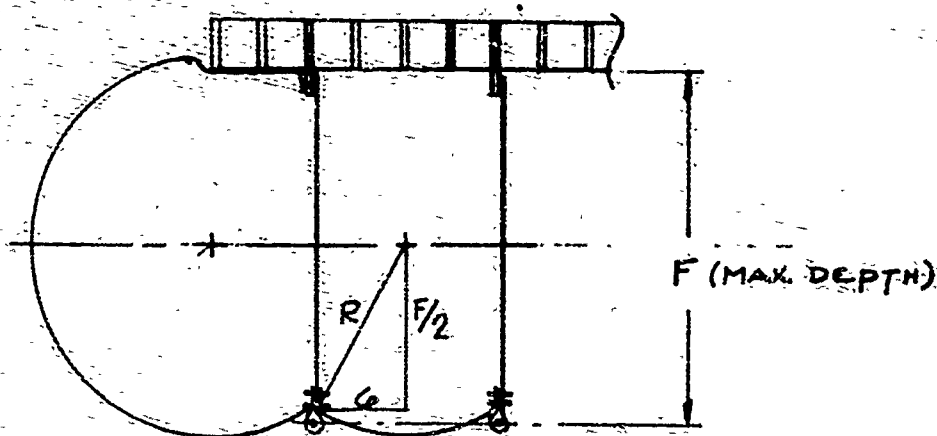
THIS PRINT OUT IS A LISTING OF THE DEFLECTION AS A
CONCENTRATED LIVE LOAD MOVES ALONG THE RAMP.

THE CONCENTRATED LIVE LOAD (LBS)=
2120000
THE DEAD LOAD (LBS/IN)=
232.3
THE SPAN LENGTH (IN)=
21320
THE MAXIMUM DEPTH (F) IN INCHES =
2130

DISTANCE ALONG RAMP (IN)	MOM. OF INERTIA AT POINT (IN4)	DEFL. UNDER D.L. (IN)	DEFL. UNDER L.L. (IN)	TOTAL DEFL. (IN)
30	4681.12	1.98171	.969524	2.95124
60	17507.7	1.05652	.989238	2.04576
90	37394.2	.738302	.993064	1.73137
120	63187.7	.578569	.994440	1.57301
150	93794.6	.482966	.995090	1.47805
180	128180.	.419611	.995450	1.41506
210	165369.	.374762	.995671	1.37043
240	204445.	.341529	.995817	1.33735
270	244551.	.316078	.9959.8	1.31200
300	284888.	.296111	.995991	1.29210
330	324717.	.280167	.996045	1.27621
360	363359.	.267275	.996086	1.26336
390	400194.	.256768	.996118	1.25289
420	434658.	.248172	.996143	1.24432
450	466250.	.241145	.996163	1.23731
480	494527.	.235435	.996178	1.23161
510	519104.	.230856	.996190	1.22705
540	539655.	.227269	.996200	1.22347
570	555916.	.224573	.996206	1.22078
600	567678.	.222696	.996211	1.21891
630	574795.	.221588	.996214	1.21780
660	577177.	.221222	.996215	1.21744

FABRIC STRESSES:

$$\left. \begin{array}{l} \text{TRANSVERSE FABRIC STRESS} = pR \\ \text{LONGITUDINAL FABRIC STRESS} = pR/2 \end{array} \right\} \text{OUTER SKIN}$$



$$\begin{aligned} \text{FOR } F &= 130 \text{ IN.} \\ F/2 &= 65 \text{ IN.} \\ R &= [36 + (65)^2]^{1/2} \end{aligned}$$

$$\begin{aligned} R &= 65.3 \text{ IN.} \\ &(\text{MAXIMUM}) \\ p &= 3.61 \text{ PSI} \end{aligned}$$

$$\text{MAX. FABRIC STRESS} = (65.3 \text{ IN.})(3.61 \text{ PSI}) = \underline{235.7 \text{ LBS./IN.}} \\ (\text{OUTER SKIN})$$

$$\text{FACTOR OF SAFETY} = 3$$

$$\text{REQUIRED FABRIC STRENGTH} = \underline{707 \text{ LBS./IN.}} \\ (2N14N58)$$

WEB STRESSES:

2 PLY WEB

- 1 STRAIGHT PLY
- 1 BIAS PLY

STRESS IN STRAIGHT PLY-
(DUE TO INFLATION PRESSURE)

$$\begin{aligned} \text{FABRIC STRESS} &= (p)(\text{WEB SPACING}) \\ &= (3.61)(12) \\ &= \underline{43.3 \text{ LBS./IN.}} \end{aligned}$$

$$\text{FACTOR OF SAFETY} = 3$$

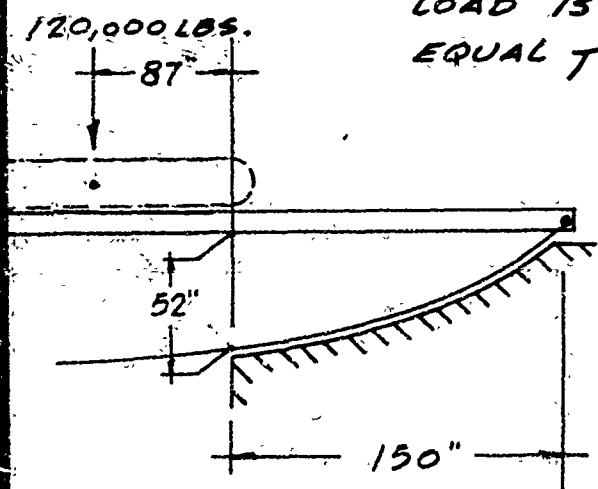
$$\text{REQUIRED FABRIC STRENGTH ST. PLY} = \underline{130 \text{ LBS./IN.}}$$

FABRIC STRESSES:

WEB STRESS - BIAS PLY

BIAS PLY CARRIES SHEAR STRESS ALONG THE RAMP.

ASSUMPTION: BECAUSE OF GEOMETRY, CONSIDER THE BEARING LENGTH ON EACH END EQUAL TO 150 IN., THEREFORE, ASSUME MIN. DEPTH OF RAMP TO CARRY SHEAR LOAD IS AT 150 IN. OR A DEPTH EQUAL TO 52 IN.



SHEAR FORCE AT SUPPORT

$$V_{D.L.} = \frac{wL'}{2} = \frac{(32.3)(1170)}{2} = 18,895 \text{ LBS.}$$

$$L' = 1320 - 300 = 1170 \text{ IN.}$$

$$V_{L.L.} = \frac{Pa'}{L''} = \frac{(120,000)(1083)}{(1170)} = 111,077 \text{ LBS.}$$

$$a' = 1170 - 87 = 1083$$

$$L'' = 1170$$

$$\text{TOTAL MAX. SHEAR FORCE} = \underline{129,972 \text{ LBS.}}$$

SHEAR FORCE ALUM. DECK WILL CARRY:

$$\text{CROSS-SECTIONAL AREA} = (65 \text{ BARS})(.5)(3.5) = 113.75 \text{ IN}^2$$

$$\text{ALLOW. SHEAR STRESS (6061-T6 ALUM.)} = 10 \text{ KSI}$$

$$\text{SHEAR LOAD} = (113.75)(10,000) = 1,137,500 \text{ LBS. } \underline{OK}$$

FABRIC STRESS

WEB STRESS

IF WEB IS TO TRANSFER SHEAR LOAD -

$$\text{FORCE PER WEB} = 129,912 / 16 = 8123 \text{ LBS. / WEB}$$

$$\text{@ } 45^\circ \text{ BIAS, LENGTH} = (1.414)(52) = 73.5 \text{ IN.}$$

$$\text{STRESS IN BIAS PLY} = 110.5 \text{ LBS. / IN.}$$

$$\text{FACTOR OF SAFETY} = 3$$

$$\text{REQUIRED FABRIC STRENGTH BIAS PLY} = 332 \text{ LBS / IN.}$$

(2N5N42)

WEIGHT CALCULATIONS:

$$\text{TOTAL WEIGHT OF ALUMINUM DECK} = 11.34 \text{ TONS}$$

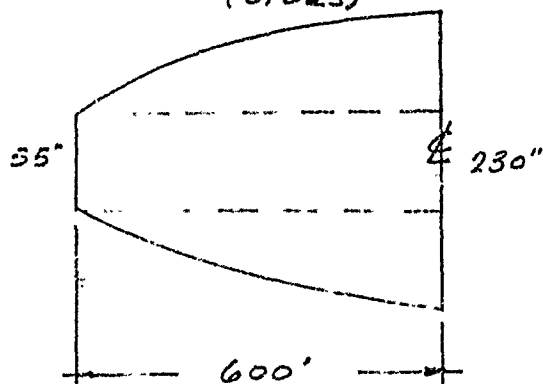
$$\text{TOTAL WEIGHT OF STAINLESS STEEL CABLES} =$$

$$16 \text{ CABLES} \times 4.34 \text{ LBS. / FT.} \times 120 \text{ FT.} = 8333 \text{ LBS.}$$

$$\begin{array}{r} \text{HARDWARE } 10\% \quad 833 \text{ LBS.} \\ \hline 9166 \text{ LBS.} \end{array}$$

FABRIC WEIGHT =

$$\text{OUTER SKIN - 2N14N58 - 58 OZ / S.Y. (SIDES)}$$



$$\text{IN}^2 = (55)(600) + (2) \left[\frac{2}{3} (87.5)(600) \right]$$

$$\text{IN}^2 = 103,000$$

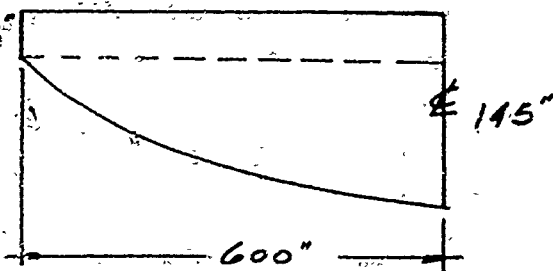
$$\text{YD}^2 = 79.5$$

$$\text{TOTAL S.Y.} = 79.5 \times 4 = 318 \text{ YD}^2$$

$$\text{WEIGHT} = (318) \left(\frac{58 \text{ OZ / YD}^2}{16 \text{ OZ / LB}} \right) = 1153 \text{ LBS.}$$

FABRIC WEIGHT CALCULATIONS CONT.

WEBS - 2NSN42 - 42 oz/YD²



$$IN^2 = (122.5)(600) + \left(\frac{2}{3}\right)(122.5)(600)$$

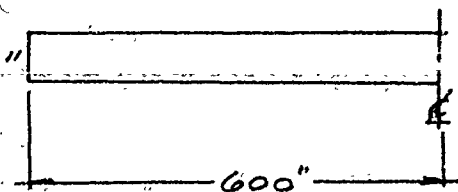
$$IN^2 = 62,500$$

$$YD^2 = 48.2$$

$$TOTAL YD^2 = 48.2 \times 2 \times 16 WEBS = 1542.4$$

$$WEIGHT = \frac{(1542.4)(42 oz/YD^2)}{16 oz/LB.} = 4048.8 \text{ LBS.}$$

BOTTOM CLOSURES



$$IN^2 = (20)(600)$$

$$IN^2 = 12,000 IN^2$$

$$YD^2 = 9.3$$

$$TOTAL YD^2 = 9.3 \times 2 \times 15 REPS. = 279$$

$$WEIGHT = (279) \left(\frac{48 oz/YD^2}{16 oz/LB.} \right) = 837 \text{ LBS.}$$

$$\begin{array}{rcl} TOTAL FABRIC WEIGHT & = & 6039 \text{ LBS} \\ 10\% \text{ FOR SEAMS} & = & 604 \\ \hline & & 6643 \text{ LBS.} \end{array}$$

ALUMINUM MEMBRANE ON DECK -

$$\frac{1}{8} \text{ IN.} \times 1320 \text{ IN.} \times 192 \text{ IN.} = 31,680 \text{ IN.}^3$$

$$@ .0955 \text{ LBS./CU. IN.} = 3025 \text{ LBS.}$$

ESTIMATED TOTAL WEIGHT OF CONCEPT NO. 10 = 20.76 TONS

```

>20 Y=4*130*(1-(X/1320))*(X/1320)
>30 V1=((192*Y)+((3.14*Y*Y)/4))*12
>40 V1=V1/1728
>50 PRINT V1
>60 NEXT X
>70 END
>RUN
08:48 04/09

```

VOLUME CALCULATIONS

36.2592
 43.1055
 49.9995
 56.9298
 63.8849
 70.8537
 77.8254
 84.7892
 91.7349
 98.6523
 105.531
 112.363
 119.137
 125.844
 132.476
 139.024
 145.479
 151.833
 158.079
 164.208
 170.213
 176.087
 181.822
 187.413
 192.852
 198.133
 203.250
 208.197
 212.970
 217.561
 221.968
 226.183
 230.204
 234.025
 237.643
 241.053
 244.252
 247.237
 250.004
 252.551
 254.875
 256.974
 258.844
 260.485
 261.895
 263.072
 264.015
 264.723
 265.196
 265.432

$$8977.13 \times 2 = \boxed{17,954.3 \text{ FT}^3}$$

```

70 HALT
>SYS

```

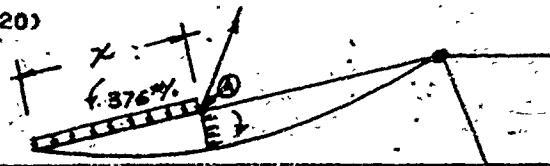
D-41

*F/LJUNON
04/09/ '73 11:02
!LOGIN: 1507BRD,C,
ID= C
!BASIC

```
>5 PRINT" X
>6 PRINT"
>7 PRINT
>15 FOR X=12 TO 660 STEP 24
>20 Y=4*130*(1-(X/1320))*(X/1320)
>30 Y1=Y/12
>40 A1=16*Y1
>50 A2=3.14*Y1*Y1/4
>60 A3=A1+A2
>70 F1=3.6*144*A3
>80 M1=F1*(Y1/2)
>90 X1=X/12
>100 M2=375*X1*(X1/2)
>110 PRINT X1,M1,M2
>120 NEXT X
>130 END
>RUN
```

MOMENT
CLOCKWISE

MOMENT"
COUNTERCLOCKWISE"



$EM_2 = 0$

MOM. (CLOCKWISE) = (PRESS.) (ARM) (LEVER)

MOM. (COUNTERCLOCKWISE) = (LOAD) (LEVER ARM)

LOAD = 20.65 TON
110' = 375 LBS/FT.

11:08 04/09

	MOMENT CLOCKWISE (DUE TO PRESS.)	MOMENT COUNTERCLOCKWISE (DUE TO WT. OF RAMP)
1	644.051	187.500
3	5789.85	1687.50
5	16012.8	4687.50
7	31153.1	9187.50
9	50969.2	15187.5
11	75148.7	22687.5
13	103318.	31687.5
15	135052.	42187.5
17	169884.	54187.5
19	207314.	67687.5
21	246816.	82687.5
23	287850.	99187.5
25	329864.	117188.
27	372305.	136688.
29	414624.	157688.
31	456283.	180188.
33	496760.	204188.
35	535556.	229688.
37	572198.	256688.
39	606245.	285188.
41	637290.	315188.
43	664967.	346688.
45	688952.	379688.
47	708965.	414188.
49	724774.	450188.
51	736198.	487688.
53	743106.	526688.
55	745417.	567188.

NOTE:

SINCE THE CLOCKWISE
MOMENT EXCEEDS THE
COUNTERCLOCKWISE MOM.
AT ALL POINTS ALONG
THE RAMP, IT IS POSSIBLE
TO HOIST THE RAMP AT
ANY POINT WITHOUT
BUCKLING THE DECK.

130 HALT
>SYS

!BYE
04/09/ '73 11:10
CLT 8
CCU 0,014

D-42

MODEL ANALYSIS

DIMENSIONAL SIMILITUDE REQD. FOR SCALE
MODEL OF CONCEPT NO. 10

BASIC ASSUMPTION: FOR $1/10$ SCALE

DEFLECTION OF MODEL = $1/10$ DEFLECTION OF ACTUAL
FULL SIZE RAMP

$$\Delta(D.L.) = \frac{W X}{24 E I} (L^3 - 2 L X^2 + X^3)$$

(AT POINT X)

$$\Delta(L.L.) = \frac{P a^2 b^2}{3 E I L}$$

(AT POINT OF
LOAD)

FROM AISC
STEEL MANUAL
REF. PG. D-34

NOTATION: SUBSCRIPT M = MODEL
SUBSCRIPT A = ACTUAL FULL SIZE RAMP

$$\Delta_M = \frac{1}{10} \Delta_A$$

$$\Delta_M(D.L.) = \frac{W_M L_M}{24 E_M I_M} \overbrace{(L_M^3 - 2 L_M^3 + L_M^3)}^{L^3} = \frac{1 W_A L_A}{(10)(24) E_A I_A} \overbrace{(L_A^3 - 2 L_A^3 + L_A^3)}^{L^3}$$

$$L_M = \frac{1}{10} L_A$$

$$I_M = \left(\frac{1}{10}\right)^4 I_A$$

$$\Delta_M = \frac{W_M \left(\frac{1}{10} L_A\right) \left(\frac{1}{10} L_A\right)^3}{24 E_M \left(\frac{1}{10}\right)^4 I_A} = \frac{W_A L_A L_A^3}{(10)(24) E_A I_A}$$

$$\underline{\underline{\frac{W_M}{E_M} = \frac{W_A}{10 E_A}}}$$

EQ. 1

$$\Delta_M = \frac{P_M L_M^2 L_M^2}{3 E_M I_M L_M} = \frac{1}{10} \left[\frac{P_A L_A^2 L_A^2}{3 E_A I_A L_A} \right]$$

$$L_M = \frac{1}{10} L_A$$

$$I_M = \left(\frac{1}{10} \right)^4 I_A$$

$$\Delta_M = \frac{P_M \left(\frac{1}{10} L_A \right)^2 \left(\frac{1}{10} L_A \right)^2}{3 E_M \left(\frac{1}{10} \right)^4 I_A \left(\frac{1}{10} \right) L_A} = \frac{P_A L_A^4}{(10)(10)(E_A)(I_A)(L_A)}$$

$$\frac{P_M}{E_M} = \frac{P_A}{100 E_A}$$

EQ. 2

FROM EQ. 1

$$E_A = \frac{W_A E_M}{10 W_M}$$

EQ. 3

FROM EQ. 2

$$E_A = \frac{E_M P_A}{100 P_M}$$

EQ. 4

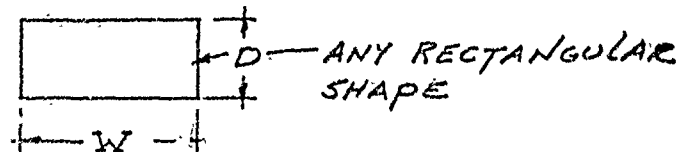
$$\frac{E_M P_A}{100 P_M} = \frac{W_A E_M}{10 W_M}$$

$$\frac{P_A}{10 P_M} = \frac{W_A}{W_M}$$

EQ. 5

$$W = f \left(\frac{L (2W + 2D) t}{\delta} \right)$$

$$W = \frac{L}{\delta} \text{ LBS./IN.} = \text{FORCE/LENGTH}$$



$$\therefore W_M = \left(\frac{1}{10} \right)^2 W_A$$

t = MTL. THICKNESS EQ. 6

$$\frac{P_A}{100 P_M} = \frac{W_A}{W_M}$$

EQ. 5

$$= \frac{W_A}{(\frac{1}{10})^2 W_A}$$

$$\therefore \underline{P_M = (\frac{1}{1000}) P_A}$$

EQ. 7

$$E_A = \frac{P_A E_M}{100 P_M}$$

EQ. 4

$$E_M = \frac{100 P_M}{P_A} E_A$$

$$P_M = \frac{P_A}{1000}$$

$$E_M = 100 \left(\frac{P_A}{1000 P_A} \right) E_A$$

$$\underline{E_M = (\frac{1}{10}) E_A}$$

EQ. 8

$$\text{INFLATION PRESS. } (P) = P / L^2$$

$$P_M = f(P_A)$$

$$P_M = \frac{P_A}{1000 (\frac{1}{10} L_A) (\frac{1}{10} L_A)} = \frac{P_A}{L_A L_A}$$

$$\underline{P_M = (\frac{1}{10}) P_A}$$

EQ. 9

FOR COMPRESSION DECK

$$S = \frac{bh^2}{6} = L^3 \quad (S = \text{SECTION MODULUS})$$

$$\underline{S_M = \left(\frac{1}{10}\right)^3 S_A}$$

EQ. 10

FOR TENSION CABLES

$$DIA. = L$$

$$\underline{DIA. M = \left(\frac{1}{10}\right) DIA. A}$$

EQ. 11

FOR FABRIC

A FUNCTION OF WEIGHT OR THICKNESS

WT. PER SQ. YD. IS A FUNCTION OF MAT. THICKNESS (t)

$$\underline{oz./yd^2 M = \left(\frac{1}{10}\right) oz./yd^2 A}$$

EQ. 12

SUMMARY OF PARAMETERS REQUIRED TO
SIMULATE CONCEPT 10 AT 1/10 SCALE:

$$\underline{LENGTH_M = \frac{1}{10} LENGTH_A = \frac{1320 \text{ IN.}}{10} = 132 \text{ IN.}}$$

$$\underline{WIDTH_M = \frac{1}{10} WIDTH_A = \frac{192 \text{ IN.}}{10} = 19.2 \text{ IN.}}$$

$$\underline{MAX. DEPTH_M = \frac{1}{10} MAX. DEPTH_A = \frac{130 \text{ IN.}}{10} = 13 \text{ IN.}}$$

$$\underline{INFLATION PRESSURE = \frac{1}{10} P_A = \left(\frac{1}{10}\right)(3.6) = .36 \text{ PSI}}$$

$$\underline{MAX. POINT LOAD = \frac{P_A}{1000} = \frac{120,000}{1000} = 120 \text{ LBS.}}$$

SUMMARY OF PARAMETERS REQD. TO SIMULATE
CONCEPT No 10 AT 1/10 SCALE: (CONT.)

COMPRESSION DECK

$$E_M = \frac{1}{10} E_A \text{ (EQ. 8)}$$

$$E_M = \left(\frac{1}{10}\right)(10,000,000) = \underline{1 \times 10^6 \text{ PSI}}$$

(6061-T6 ALUM.)

$$S_M = \left(\frac{1}{10}\right)^3 S_A \text{ (EQ. 10)}$$

$$S_M = \left(\frac{1}{10}\right)^3 (1.028)(65) = \underline{.0668 \text{ IN}^3}$$

$$S_M = \frac{bh^2}{6} \quad h^2 = \frac{6S_M}{b} \quad b = 19.2 \text{ IN.}$$

$$\underline{h = \text{THICKNESS} = .1445 \text{ IN. (9 GAGE)}}$$

TENSION CABLES

$$E_M = \frac{1}{10} E_A = \frac{1}{10} (24,000,000) = \underline{2.4 \times 10^6 \text{ PSI}}$$

$$DIA_M = \frac{1}{10} DIA_A \text{ (EQ. 11)}$$

$$\underline{DIA_M = \left(\frac{1}{10}\right)(1 \frac{7}{16}) = \frac{1.4375}{10} = \underline{.14375 \text{ IN. (1/8 IN.)}}}$$

FABRIC

$$OZ/YD^2_M = \left(\frac{1}{10}\right) OZ/YD^2_A \text{ (EQ. 12)}$$

$$\underline{OUTER SKIN - OZ/YD^2_M = \left(\frac{1}{10}\right)(2N14N48) = \underline{4.8 \text{ OZ/YD}^2 \text{ (2 PLY)}}$$

$$\underline{WEBS - OZ/YD^2_M = \left(\frac{1}{10}\right)(2N5N31) = \underline{3.1 \text{ OZ/YD}^2 \text{ (2 PLY-BIAS)}}$$

REFINED ANALYSIS FOR PRACTICAL APPROACH IN DEVELOPING 1/10 SCALE MODEL

ON PAGE E-5, NOTE THE SMALL MODULI OF ELASTICITIES THAT ARE REQD. TO SATISFY THE VARIOUS OTHER PARAMETERS.

FOR PRACTICAL PURPOSES ASSUME $E_M = E_A$

THEREFORE FROM EQ. 2

$$\frac{P_M}{E_M} = \frac{P_A}{100 E_A} \quad E_M = E_A$$

$$\underline{P_M = \frac{P_A}{100}}$$

CONVERSELY, FROM EQ. 9

$$\underline{P_M = P_A}$$

ON PAGE E-4, NOTE REQD. SECTION MODULUS FOR COMPRESSION DECK. SINCE ACTUAL MODEL DECK WILL BE CONSTRUCTED FROM SHEET ALUMINUM, ^{SINCE} AND WE REQUIRE TO STRESS THE DECK TO ITS ALLOWABLE LOAD, A SCALE DOWN OF CROSS-SECTIONAL AREA SHOULD BE THE DETERMINING FACTOR.

$$\begin{aligned} AREA_M &= \left(\frac{1}{10}\right)^2 AREA_A \\ &= \left(\frac{1}{100}\right)(65 \text{ BARS})(3.5 \text{ IN.})(.5 \text{ IN.}) = 1.14 \text{ IN}^2 \end{aligned}$$

FOR WIDTH = 19.2 IN

$$THICKNESS = \frac{1.14}{19.2} = .0592 \text{ IN.} \approx \frac{1}{16} \text{ IN.}$$

TO SATISFY SECTION MODULUS - 1/8 IN. THICKNESS REQUIRED - NEGLECT THIS SINCE IT ONLY EFFECTS DEFLECTION

ON PAGE E-4, FABRIC TYPE REQD. WAS BASED ON A WEIGHT COMPARISON. FOR THE MODEL, A MORE PRACTICAL APPROACH WILL BE TO USE THE REDUCED GEOMETRIC DIMENSIONS ALONG WITH THE REQD. INFLATION PRESSURE, AND CALCULATE FABRIC STRENGTH REQD.

BASIC GEOMETRIC REQUIREMENTS FOR 1/10 SCALE MODEL OF CONCEPT N° 10

OVERALL LENGTH = 132 IN.

DECK WIDTH = 19.2 IN.

MAX. DEPTH = 13 IN.

MAX. LOAD = 1200 LBS.

INFLATION PRESS. = 3.6 PSI

DECK - 6061-T6 ALUM. 19.2 x 132 x 1/16" TH.

CABLES - 16 REQD. 1/8" ϕ 7X16 NEOPRENE COATED
(BREAKING STRENGTH = 1900 LBS.)

APPROXIMATION OF MODEL WT.

$$\text{DECK} - (19.2)(132)(.0625)\left(\frac{165}{1728}\right) = 15.1 \text{ LBS.}$$

CABLES - 1/8" ϕ - NEOPRENE COATED
24.5 GMS./FT.

$$(16)(132)\left(\frac{1}{12}\right)(24.5)(.002) = 9.8 \text{ LBS.}$$

FABRIC - EST. 5.1 LBS.

APPROX. TOTAL WEIGHT = 30 LBS

$$W = \frac{30}{132} = \underline{\underline{.23 \text{ LBS/IN.}}}$$

<15TJERSEARCH
03/08/ '73 13:12
!LOGIN: 1507BRD,C,

?
!LOGIN: 1507BRD,C,

ID= D

!BASIC

>LOAD MODEL10

>RUN

13:13 03/08

THIS PROGRAM COMPUTES THE COMPRESSIVE LOAD ON THE DECK
AND THE TENSILE LOAD ON THE CABLES AS A CONCENTRATED
LOAD MOVES ACROSS THE RAMP.

THE CONCENTRATED LIVE LOAD (LBS)=
?1200
THE DEAD LOAD (LBS/IN)=
?.23
THE REQUIRED INFLATION PRESSURE (PSI)=
?3.6
THE MAX. DEPTH AT MIDSPAN (IN)=
?13

DISTANCE ALONG RAMP (IN)	BENDING MOMENT (IN-LBS)	DEPTH OF RAMP (IN)	TOTAL COMPRESSIVE FORCE (LBS)	TOTAL TENSILE FORCE (LBS)
3	3562.69	1.15496	14664.9	18489.4
9	10190.9	3.30372	14664.9	18161.3
15	16156.4	5.23760	14664.9	17827.9
21	21459.0	6.95661	14664.9	17488.3
27	26098.8	8.46074	14664.9	17141.5
33	30075.7	9.75000	14664.9	16786.9
39	33389.8	10.8244	14664.9	16423.5
45	36041.1	11.6839	14664.9	16050.7
51	38029.6	12.3285	14664.9	15667.9
57	39355.3	12.7583	14664.9	15274.8
63	40018.1	12.9731	14664.9	14870.9

280 HALT
>SYS

!BYE

03/08/ '73 13:16

CLT 3

CCU 0.030

FROM COMPUTER RUN:

TOTAL TENSILE LOAD = 19,000 LBS

LOAD PER CABLE = $19,000 / 16 = 1190$ LBS

SAFETY FACTOR = $1900 / 1190 = 1.6$

TOTAL COMPRESSIVE FORCE = 14,665 LBS.

ALLOW. COMPRESSIVE FORCE =

$(19.2)(.0625)(14,000) = 16,800$ LBS.

ACTUAL LOAD APPROACHES ALLOWABLE LOAD - OK

FABRIC STRENGTH REQUIREMENTS

OUTER SKIN - $R = ((.6)^2 + (.5)^2)^{1/2} = 6.53$

$S = \phi R = (3.6)(6.53) = 23.5$ LBS./IN.

SAFETY FACTOR = 3

FABRIC STRENGTH = 70.5 LBS./IN.

WEBS - (REFER TO PGS. D-37 → D-39)

STRAIGHT PLY - $S = (3.6)(1.2) = 4.3$

FACTOR OF SAFETY = 3

FABRIC STRENGTH = 13 LBS./IN.

BIAS PLY -

SHEAR FORCE $V(D.L.) = \frac{(.23)(117)}{2} = 13.5$ LBS.

$L' = 132 - 15 = 117$

$V(L.L.) = \frac{(1200)(108.3)}{117} = 1110.8$ LBS.

$L'' = 117 - 8.7 = 108.3$

TOTAL SHEAR FORCE = 1124.3 LBS

PER WEB = 70.3 LBS.

$S = 70.3 \text{ LBS} / (5.2)(1.414) = 9.56$

SAFETY FACTOR = 3

FABRIC STRENGTH = 28.7 LBS./IN.

APPENDIX FDEFLECTION OF AIR-INFLATED RAMP

A critical factor in evaluating the feasibility of an air-inflated ramp is the amount of deflection which might be incurred. Unlike a conventional structure where member stresses are typically the controlling design factor, the normally more flexible air-inflated structure may have perfectly acceptable stress levels and yet deflect to an intolerable degree. In many instances this feature may be used to advantage, allowing the design to flex under high loads (i.e., "give with the punches") and then spring back to its normal shape. Although no critical deflection values have been established for the bow ramp, it is obvious that a great amount of deflection while a heavy vehicle is embarking would not be desirable.

Several efforts have been made to analytically predict the deflection of air-inflated, dual-wall type structures. References 5 thru 10 and 20 all propose analytical means, varying from rather straightforward, linear, small deflection analysis to very complicated, multi-term expressions. The work done by NASA (reference 5, 6, 7, and 8) is mathematically extensive, but has apparently only been used with small (18" x 18" x 1 1/8"), flat plate samples of air mat. It is exceedingly difficult to apply to the subject design. The analysis by Webb (reference 20) is more applicable, but questionable when it attempts to optimize the beam stiffness. Probably the most useful is the work done by Dr. Bulson and Tutt in England (reference 2 and 3); however, it leans upon experimental measurements to establish stiffness

coefficients. As will be discussed, even further difficulty arises due to the composite nature of the feasibility configuration. Deflection of a simple beam structure is typically broken down into two basic mechanisms: that due to bending (i.e., elongation and compression of the upper and lower fibers) and that due to shear (i.e., a vertical shift between adjacent sections). In most long rigid beams, the bending deflection is so predominate that the shear effect may reasonably be ignored.*

This is not necessarily the case with an air-inflated beam. In fact, both the NASA studies on the air mat construction and the English reports on the unreinforced, parallel web, dual-wall bridge indicate that shear distortion is the major factor. As will be shown, shear stiffness is a function of pressure, but typically NASA reports 82-97% of the air mat deflection is due to shear while the bridge studies indicate up to 97% is calculated as shear.**

Beam bending moment, assuming the upper and lower surfaces remain in tension, is resisted by normal stresses in the surface membranes. Transverse (vertical) shear is resisted by the inflation pressure and any shear capacity of the webs and side closures. This is thus somewhat analogous to sandwich plate theory.

* For a simple rectangular beam with load at mid-point:

$$\frac{\Delta_s}{\Delta_b} = \frac{5}{6} \frac{E}{E_s} \left(\frac{d}{L} \right)^2 \quad \text{where}$$

E = modulus of elasticity

E_s = shear modulus

d = depth of beam

L = length of beam

ref.: Laurson and Cox

"Mechanics of Materials"

**In actual testing, the calculated shear values exceeded total measured deflection at low pressure.

The capacity of the ramp or beam to carry load in bending may be analyzed by simple beam theory. As the webs typically have the high strength warp running vertically between the skins (direction of maximum load), the high elongation fill is lengthwise. Conversely, the low stretch warp runs lengthwise on the skin (maximum load direction in that member). Thus the webs may be conservatively assumed to have a negligible contribution as they have a high elasticity in the bending direction. (Frequently, this may not be the case in special constructions. In such cases the section may be treated as a composite beam with the webs having a different modulus than the skins.) The effective moment of inertia is then expressed by:

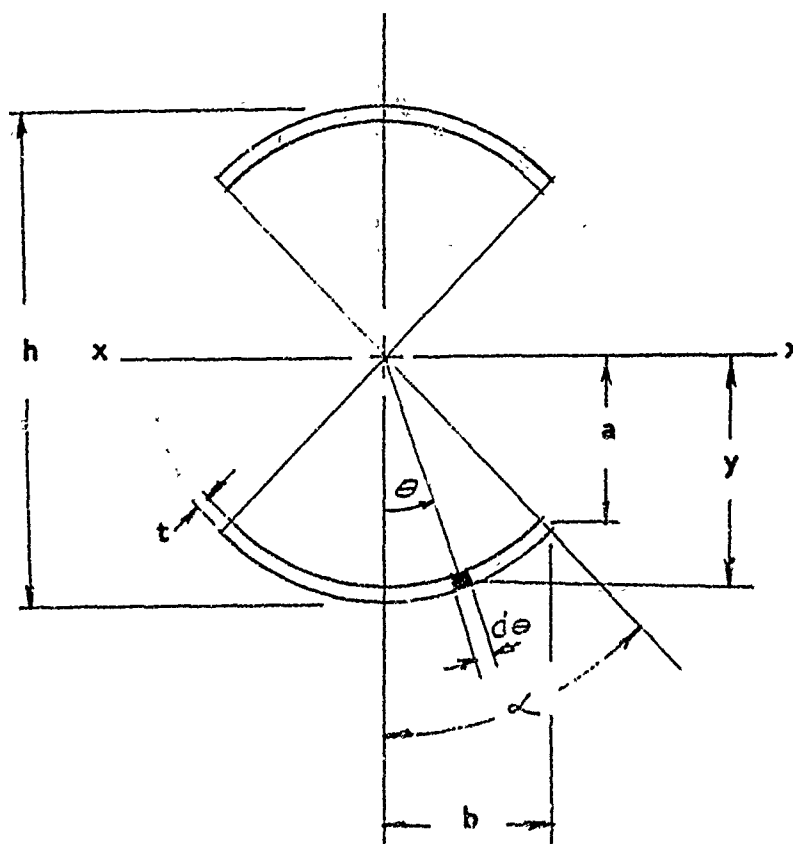


FIG. F1

$$I_{xx} = \int y^2 da$$

$$y = r \cos \theta$$

$$dA = tr d\theta$$

$$I_{xx} = 4 \int_0^{\alpha} r^2 \cos^2 \theta tr d\theta$$

$$= 4r^3 t \int_0^{\alpha} \cos^2 \theta d\theta$$

$$= 4r^3 t \left[\frac{1}{2} \theta + \frac{1}{4} \sin 2\theta \right]_0^{\alpha}$$

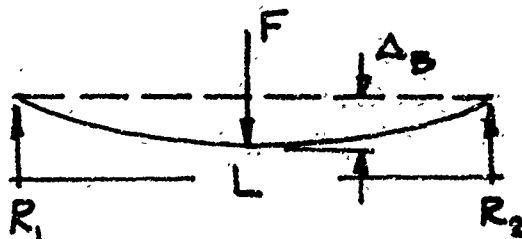
$$= 4r^3 t \left[\frac{1}{2} \alpha + \frac{1}{4} \sin 2\alpha \right]$$

$$= r^3 t [2\alpha + \sin 2\alpha]$$

or

$$I_{xx} = \frac{h^3}{8} t [\sin 2\alpha + 2\alpha]$$

with a simple supported beam, load at center,



@ F

$$\Delta_B = \frac{FL^3}{48 EI}$$

where Δ_B = bending deflection

or alternately

$$\text{Bending stiffness} = S_B = \frac{\text{LOAD}}{\text{DEFL.}}$$

$$S_B = \frac{F}{\Delta_B} = \frac{F(48EI)}{FL^3}$$

$$= \frac{48EI}{L^3}$$

Note that this assumes equal material for upper and lower surfaces.

The basic equation, which is not derived here, also is for small deflections where $\Theta = \tan \Theta = \sin \Theta$

It is interesting to observe that, theoretically, bending stiffness is not a function of inflation pressure. (However, the pressure must be sufficient to prevent compressive wrinkling and maintain a linear modulus of elasticity.)

The capacity of the air-inflated beam to resist shear may be simply* analyzed. Looking at a free body or small portion of the beam:

*Several references develop the same equation by more rigorous means.

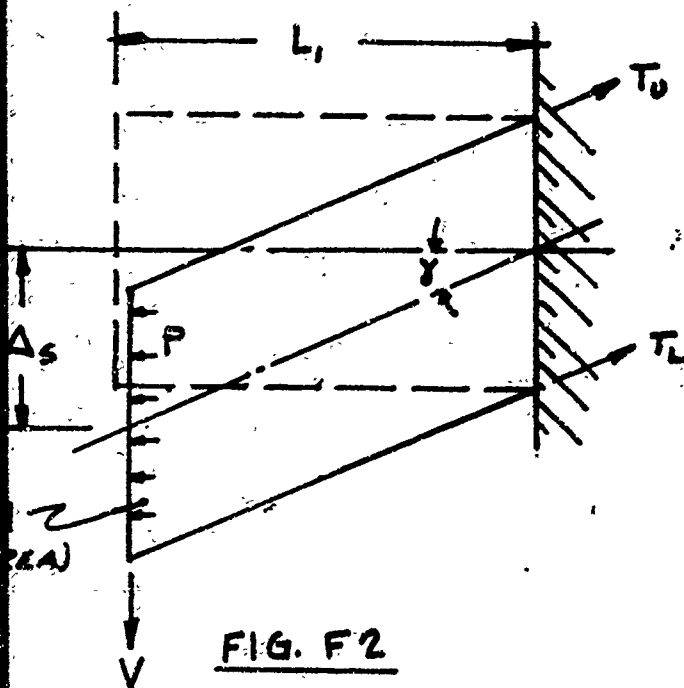


FIG. F2

Δ_s = shear deflection

where P = internal pressure

V = shear force

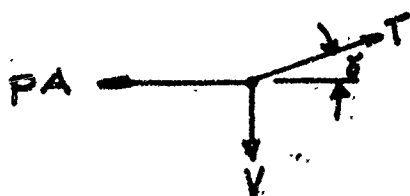
A = cross section area

T = sum of upper + lower skin tensions

L_1 = distance from load to point of reaction.

assuming the webs carry no load lengthwise*

Force balance:



$$\tan \gamma = \frac{V}{pA}$$

$$V = pA \tan \gamma$$

for small angles, $\gamma \approx \tan \gamma \approx \sin \gamma$

$$V \approx pA \gamma$$

or

$$\gamma = \frac{V}{pA}$$

*a reasonable assumption in this case as the webs normally are not attached to the skin at ends.

Deflection

$$\tan \gamma = \frac{\Delta_s}{L_1} \quad \text{or} \quad \sin \gamma = \frac{\Delta_s}{L_1}$$

$$\Delta_s = L_1 \tan \gamma$$

$$\therefore \Delta_s = L_1 \gamma \quad \text{for small angles}$$

$$\Delta_s = \frac{L_1 V}{pA}$$

or deflection per unit length

$$\frac{\Delta_s}{L_1} = \frac{V}{pA}$$

$$\text{incidentally } \frac{\Delta_s}{L_1} = \gamma$$

where γ is the common term for angular shear
deflection for small angles

The shear stiffness is $S = \frac{\text{LOAD}}{\text{DEFL.}}$

$$S = \frac{V}{\Delta_s}$$

$$= \frac{V}{L_1 V / pA}$$

$$S = \frac{pA}{L_1}$$

again, for a unit length, the stiffness is:

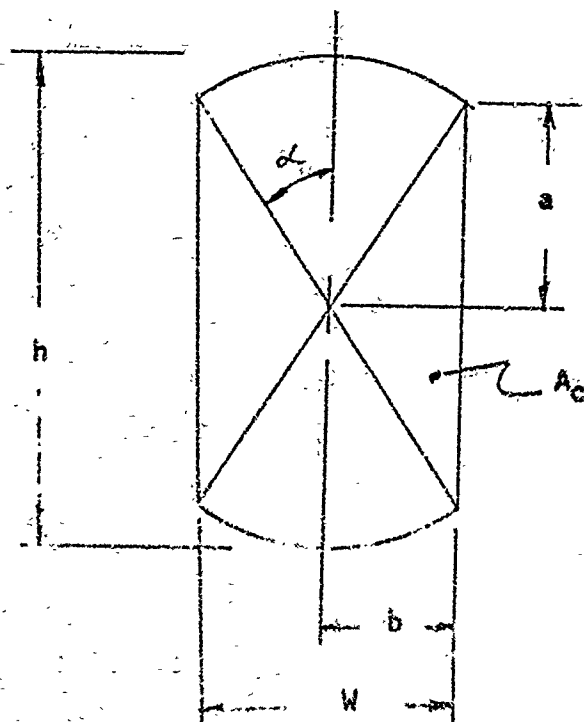
$$S_s = \frac{S}{L_1}$$

$$= \frac{pA}{L_1}$$

$$S_s = pA$$

Thus shear stiffness is a direct function of pressure. It is this deflection mode then that result in the beam becoming stiffer with increasing pressure (an intuitive observation which is easily verified experimentally).

As this value may be of frequent use, it may be further developed for a dual-wall cross section. The area for one cell is:



$$A_1 = \pi r^2 \left(\frac{\alpha}{2\pi} \right)$$

$$\alpha = \frac{2\pi}{r} \text{ radians}$$

$$A_2 = \frac{1}{2} ab$$

$$A_c = 4 \left(\frac{\pi r^2 \alpha}{2} + \frac{ab}{2} \right) = 2 \left(\pi r^2 \alpha + ab \right)$$

$$\alpha = \sin^{-1} \frac{b}{r}$$

$$r = \sqrt{a^2 + b^2}$$

FIG. F3

$$a = r \cos \alpha$$

$$A_c = 2 (r^2 \alpha + b (r \cos \alpha))$$

$$= 2 r (r \alpha + b \cos \alpha)$$

or

$$A_c = h \left(\frac{h}{2} \alpha + \frac{W}{2} \cos \alpha \right)$$

$$= \frac{h}{2} (h \alpha + W \cos \alpha)$$

Substituting in $S = PA$

For one cell

$$S_c = p \frac{h}{2} (h \alpha + W \cos \alpha)$$

$$\frac{W}{h} = \frac{b}{r} = \sin \alpha$$

$$S_c = \frac{ph^2}{2} (\alpha + \sin \alpha \cos \alpha)$$

where S_c = shear stiffness per unit length per cell

It is significant to note that the contribution to shear stiffness by the web members has been ignored in this analysis and in most reported studies. Tutt and Perkins in Ref. 3 analyze stresses in the web diaphragm, but do not enter the effect into theoretical deflection calculation. The web effect is naturally included when they made experimental measurements of shear resistance. Likewise, Birdair has experimentally observed significant differences in deflection with relatively small changes in web construction. The problem presently is not only to develop a reasonable mathematical model of the detail construction, but also to establish suitable property values (modulus of elasticity, rigidity, etc.) for the non-isotropic fabrics. As a result, in actual practice it is common to take a very pessimistic, conservative approach and use the shear stiffness as a function of pressure (which is only true for the most basic designs) and then experimentally measure true values.

Webb, in Ref. 20, develops an optimum relationship of web/cell geometry for maximum stiffness, for minimum weight, based upon the pressure shear stiffness. Unfortunately, there are several questionable means used (principally in arriving at non-dimensional parameters) in reaching the optimum geometry. Consequently, the web layout, shown in Configuration 10, does not agree with Webb's optimum arrangement, but instead has webs at a considerably closer spacing. This should result in a stiffer beam, but at a possible sacrifice in weight.

It may be apparent that Eirdair is not fully convinced of the practical usefulness of the theoretical derivations. In this regard it may be of interest to look at some comparative results with two experimental beams or panels. A typical beam is shown in Fig. F4. Each beam was 9' x 3' x 6" thick with seven cells. The beams were identical except #1 had a straight single ply flange at the web/skin joint, and #2 had a bias single ply flange at this joint. The results of testing of these panels as simple beam members with various loads at the mid-point are shown in Figures F5 and F6. Assuming the total deflection is that due to bending and shear:

$$\Delta_T = \Delta_B + \Delta_S$$

where Δ_T = total deflection

Δ_B = deflection due to bending

Δ_S = deflection due to shear

F = load

p = pressure

Based upon the previously developed equations:

$$\Delta_B = f(F, L^3, E, I)$$

$$\Delta_S = f(F, 1/p, L, A)$$

For a given beam, L, E, I, A are constant.

Therefore, at a given F, but varying p:

$$\Delta_B = \text{constant}$$

$$\Delta_S \text{ varies as } 1/p$$

Thus, if we plot deflection as a function of $1/p$ for various loads, as in Figures F6 and F11, it should be possible to extrapolate the test to obtain a deflection at $1/p = 0$. Unfortunately, the experimental points do not lend themselves to a very reliable extrapolation; however, as shown in the upper corner, it is possible to estimate a most probable point where the loads cross the vertical Y axis. Somewhat questionably for both panels, this forces us to ignore the results at 5 psi (as these would indicate an upward deflection). Figures F7 and F12 are detail plots of deflection vs. loads at the various pressure and deflection due to bending, using the stiffness rate derived from the previous figures.

Using these results and using the relationship $\Delta_s = \Delta_T - \Delta_B$ it is possible to arrive at a value for Δ_s at various loads and pressures. This is plotted for 20 lbs. and 40 lbs. in Figures F8 and F13. The value of F/Δ_s for various pressures may then be plotted as in Figures F9 and F14 to give a line representing shear stiffness as a function of pressure. The previously derived bending stiffness is also shown on these figures. The results indicate a stiffness/pressure relationship much higher than the equation $\frac{pA}{L}$. Even more surprising, the bending stiffness of both panels is apparently the same $(80 \frac{\text{lb.}}{\text{in.}})$.

The stiffness/pressure ratio is different; at 6 psi panel 1 has a rate of 105 lb./in. while panel 2 has a rate of 135 lb./in. This is quite contradictory to what the simple theory would say. We might then question the correctness of the theoretical pressure or shear stiffness.

From the previous equation, $\Delta_s = \frac{LV}{pA}$, it is possible to calculate deflection.

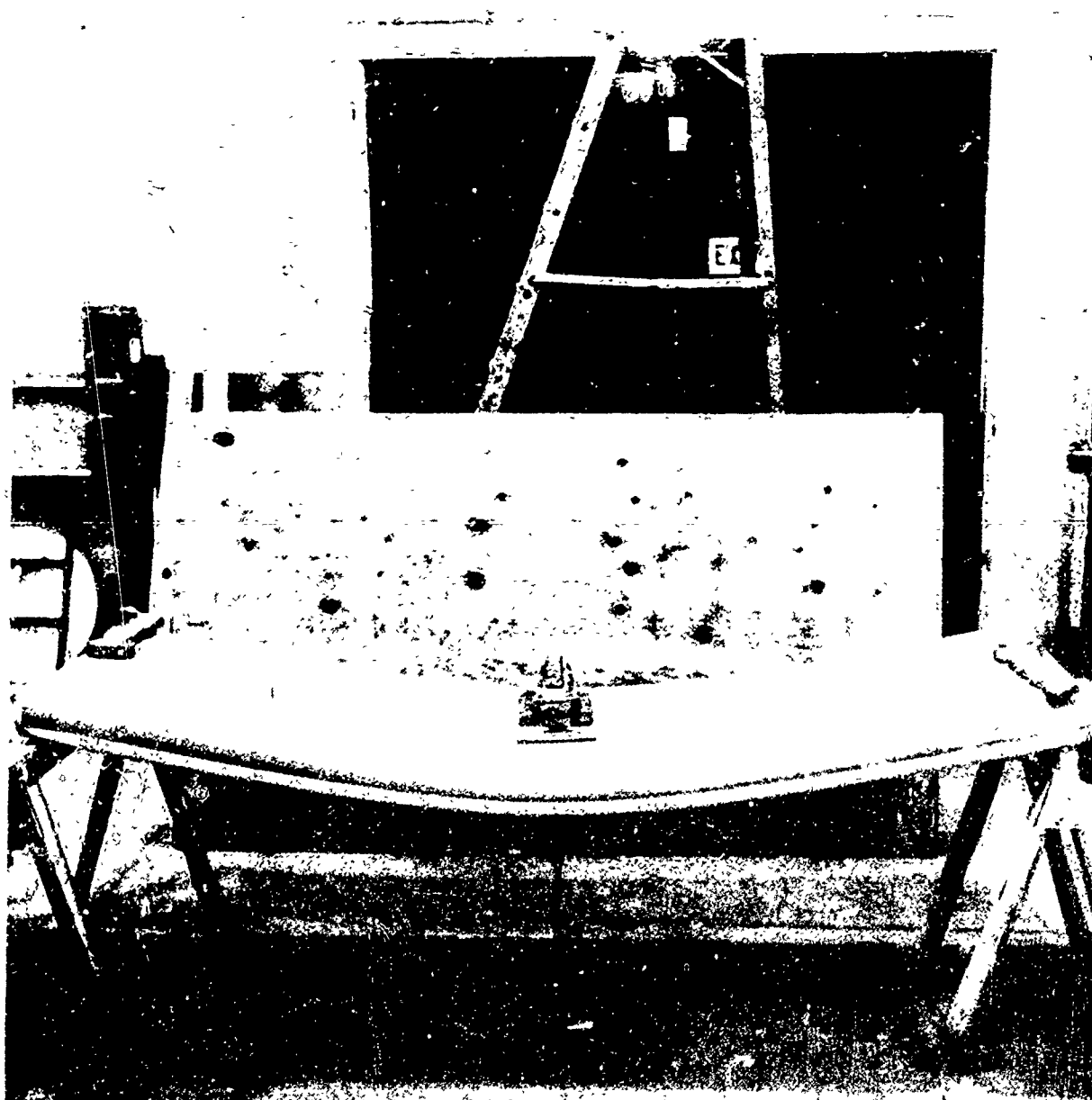


Fig. F.

Concentrated load test of straight cellular shell



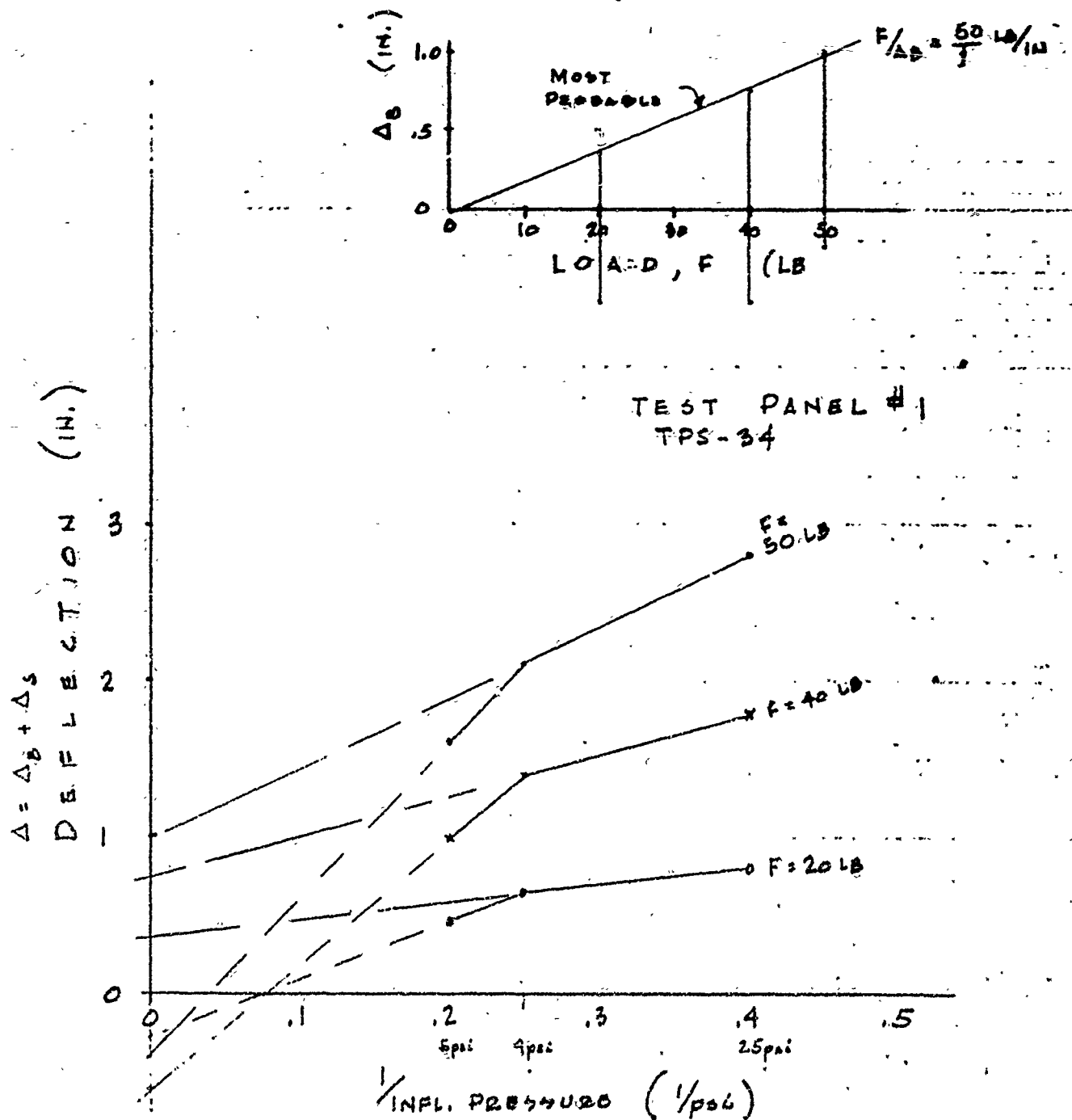


FIG. # F6

F16

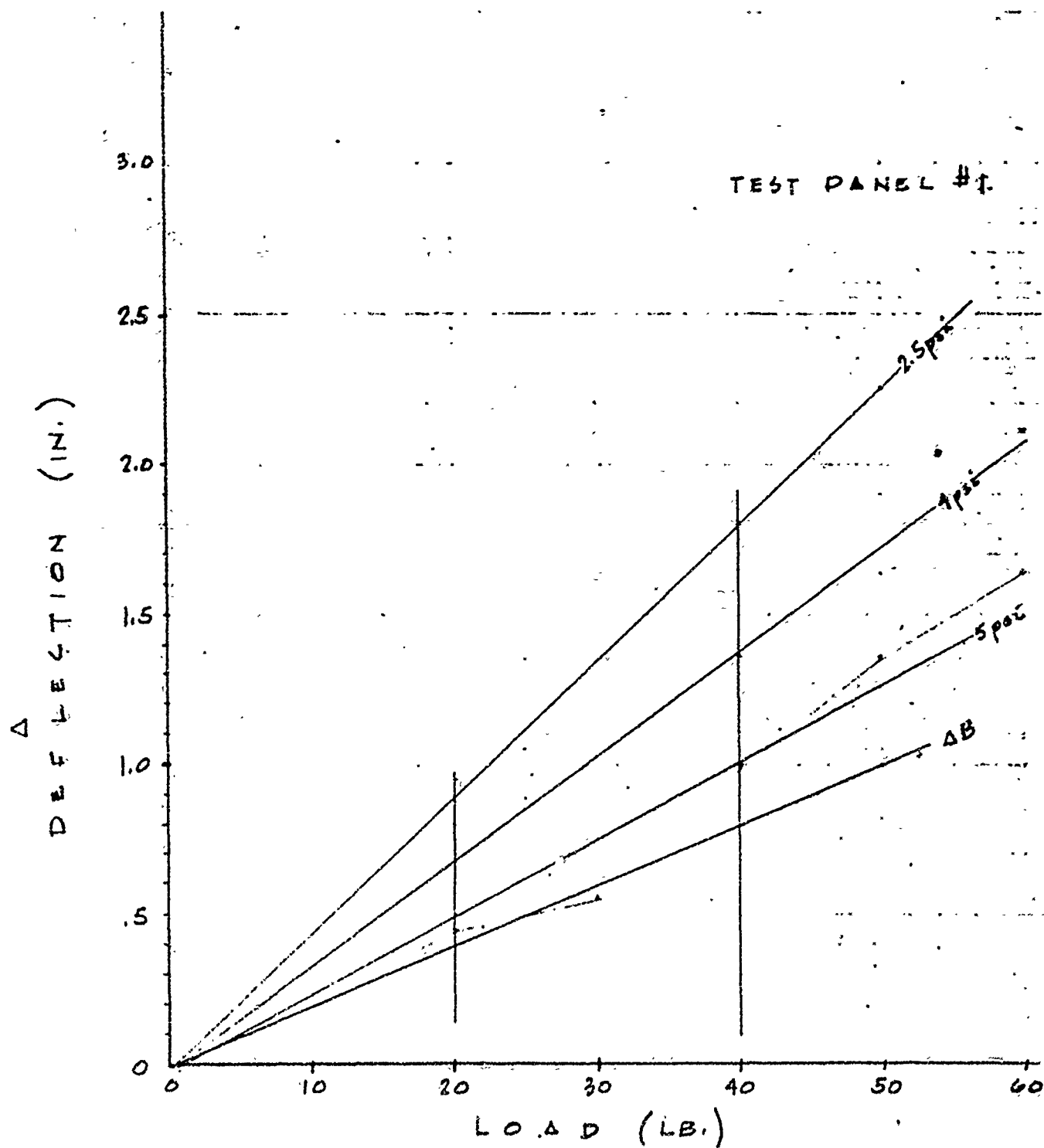
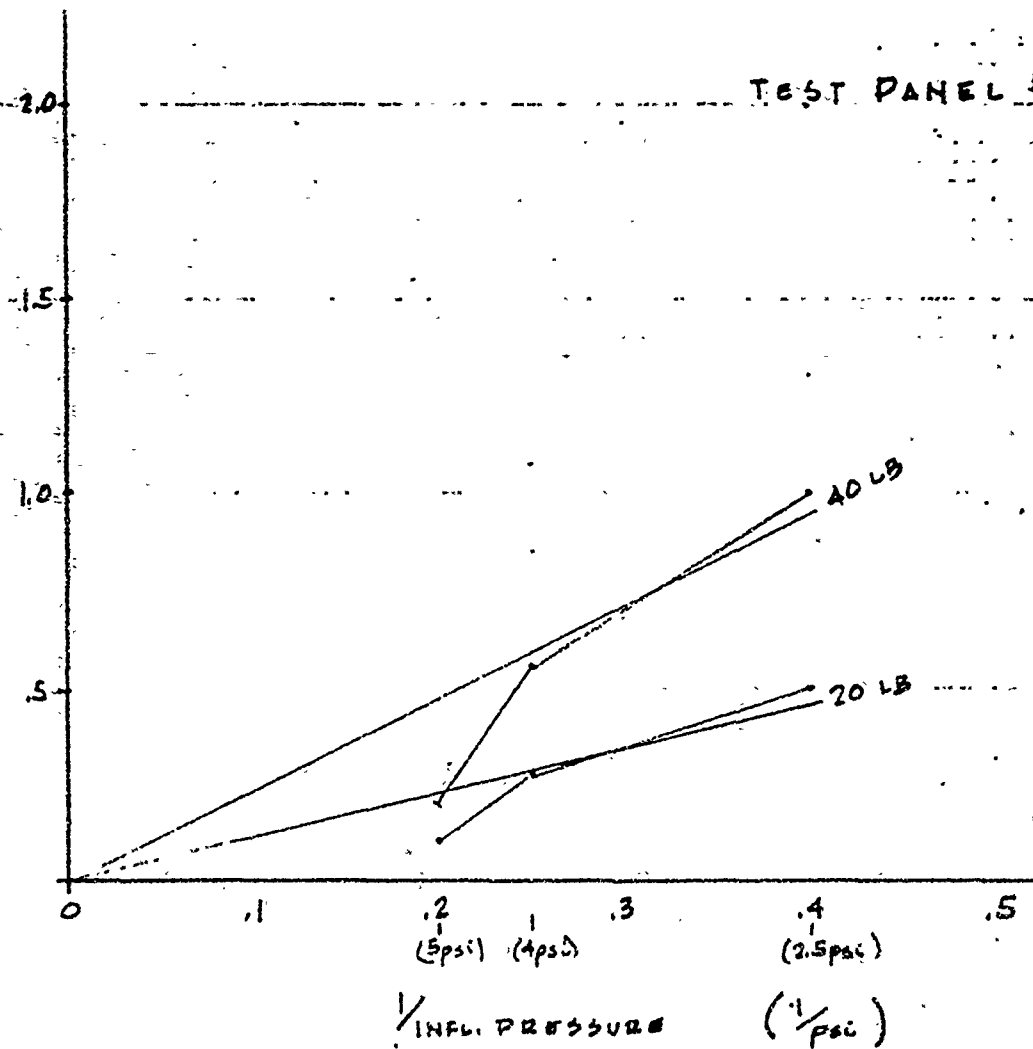


FIG # F7

3/15/73
(2)

AS = Δs

SHEAR DEFLECTION, Δs (IN)



P	F	Δs	F/Δs (lb/in)
2.5	20	.5	40
2.5	40	.95	42.1
4.0	20	.28	71.4
4.0	40	.59	67.8

Fig. # F8

3/15/73
(9)

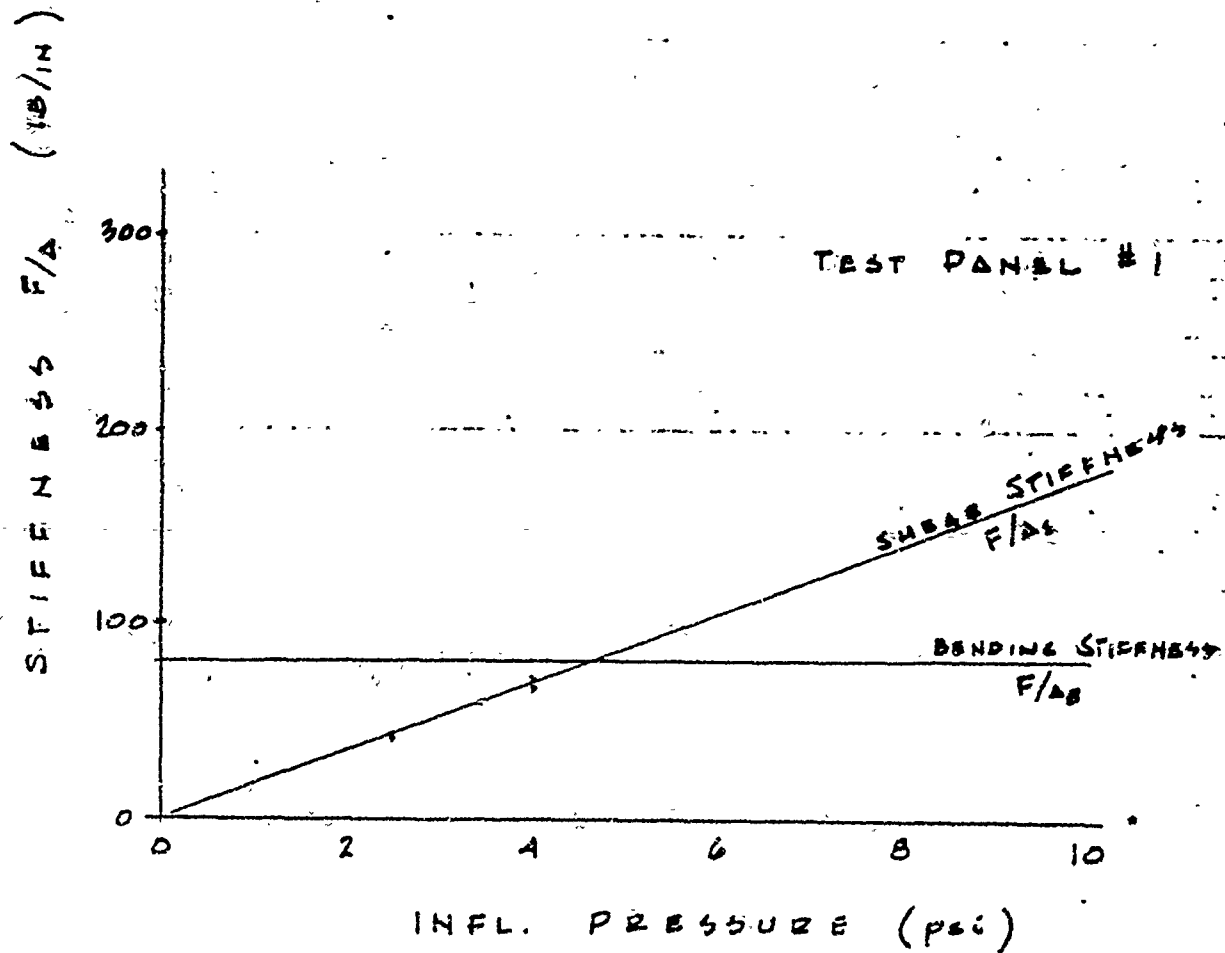


Fig # F9

3/10/73
(4)

110 125 10

TEST CASE #2
7/30/57
BIRD AIR STRUCTURES, INC.



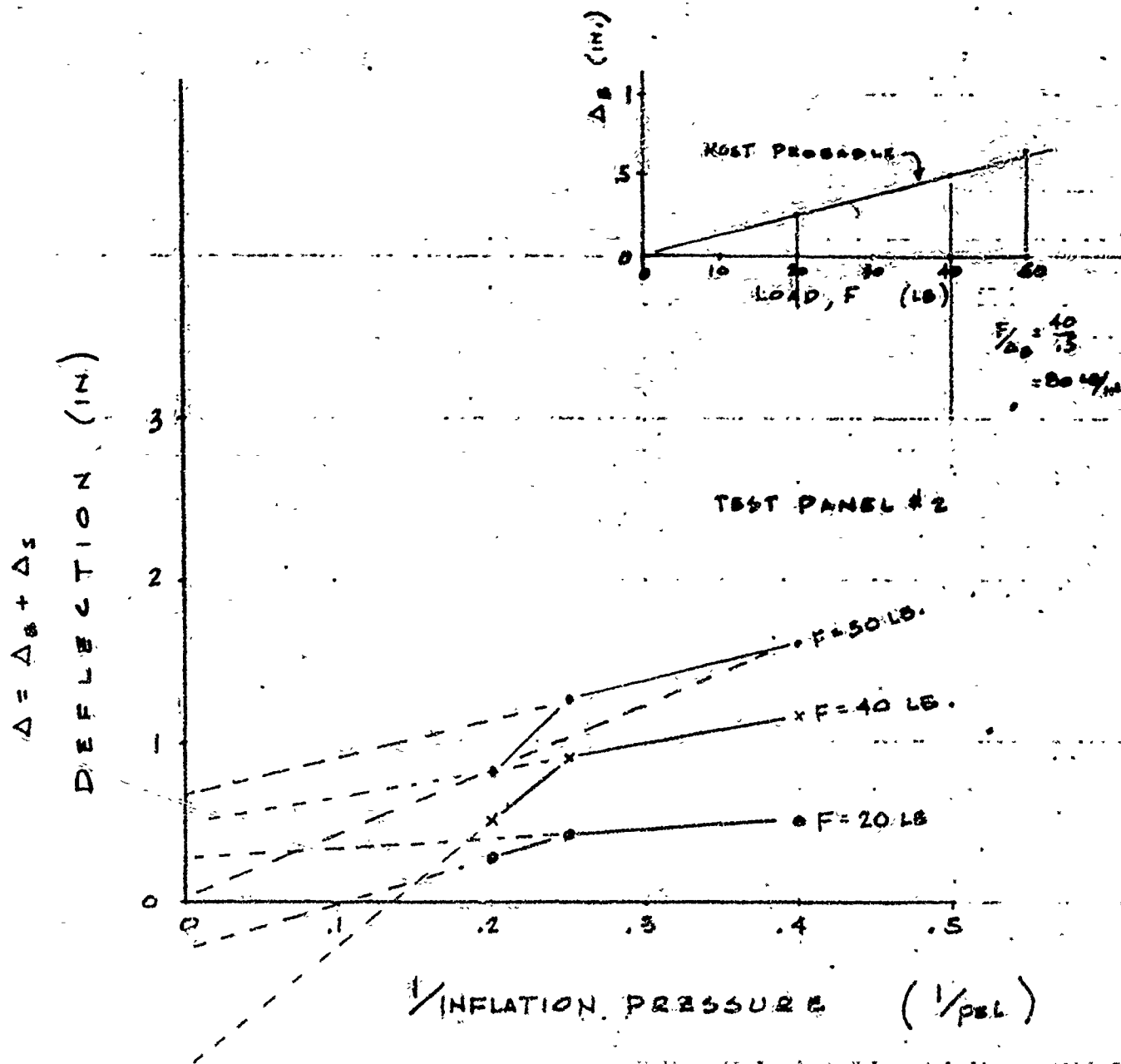


FIG. # F11

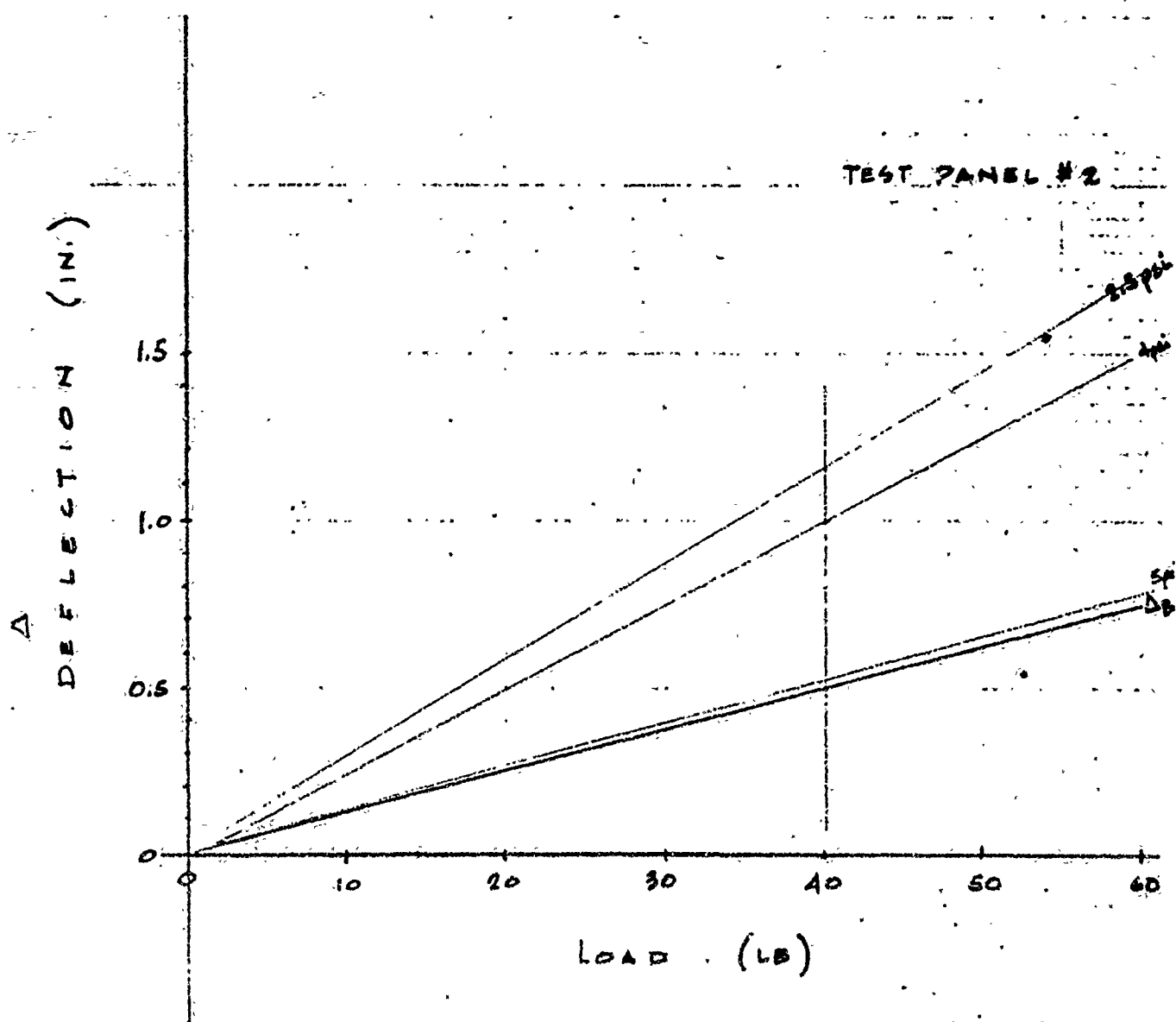
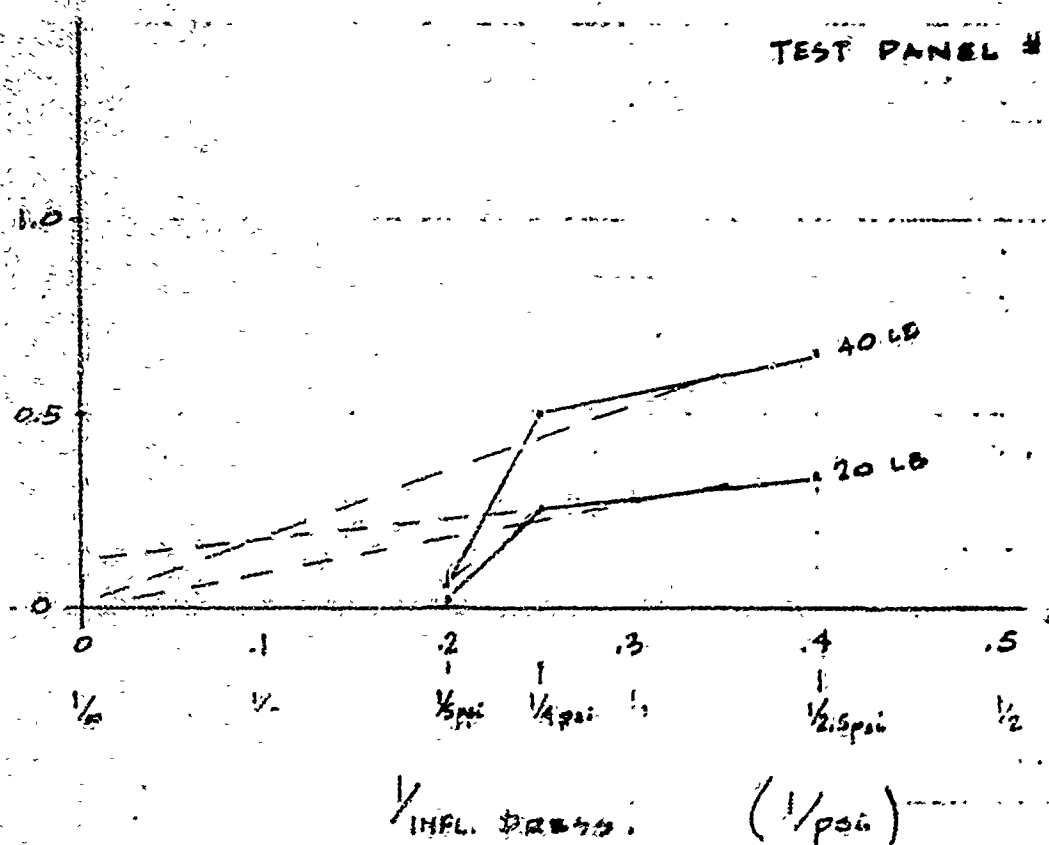


FIG # F12

SHEAR DEFLECTION, Δ_s (IN.)

TEST PANEL #2



p	F (LB)	Δ_s (in.)	F/Δ_s (LB/in.)
2.5	20	.33	61
2.5	40	.65	61.5
4.0	20	.25	80
4.0	40	.50	80
10	20	.09	225
4	25	.12	91

F1 60. F13

3/12/73
(3)

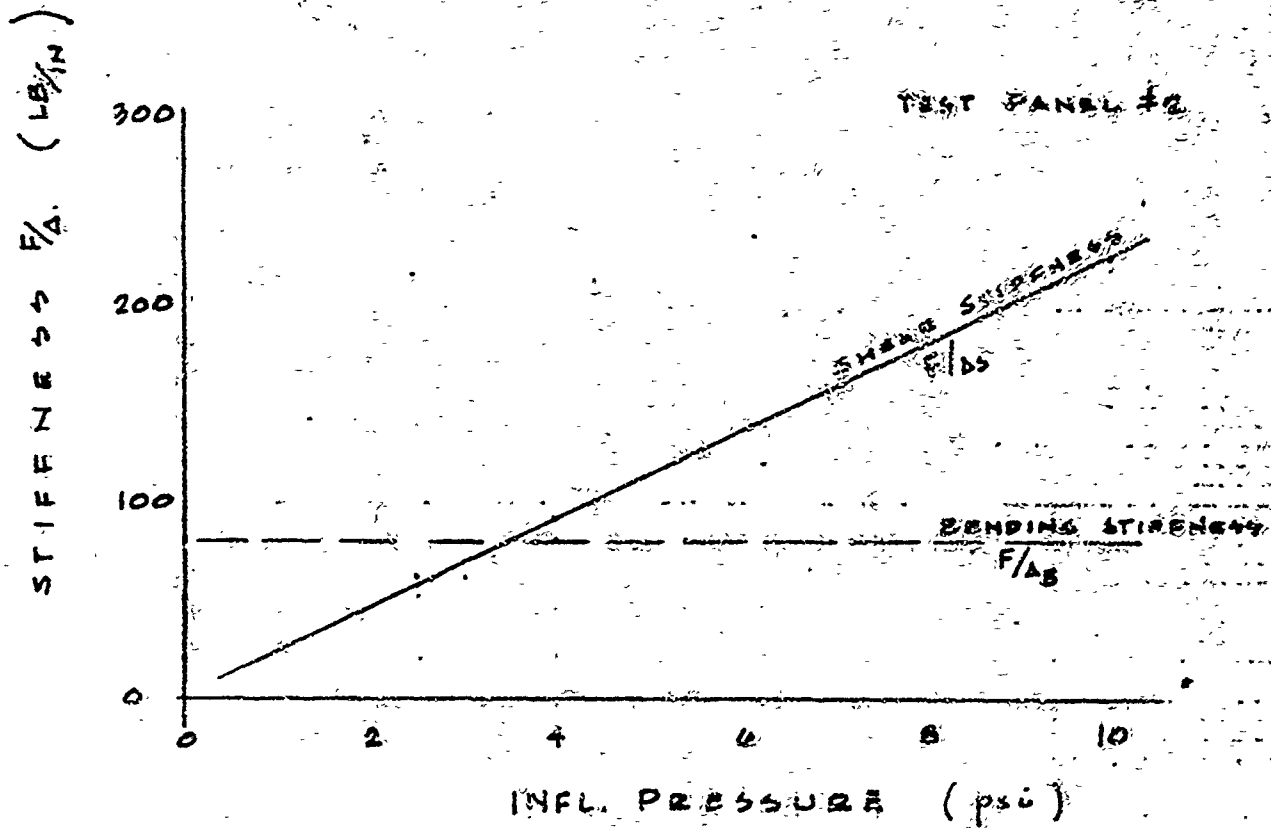


FIG. # F14

This has been done in the computer run (Fig. F15) and plotted in Figures F16 and F17 over the original measurements. In comparison, the results seem to give only a general indication of trends.

Even without further analysis, it is apparent that the actual details of the dual-wall beam construction can have extremely significant effect. It might be hypothesized that in a small beam the shear effect of the webs is extremely significant; likewise, the use of a bias web construction (or 2 ply biased) may yield unusually high stiffness. At this point it may be of interest to comment on the actual application of these test panels. The construction used in Panel #2 was utilized in the design of the TPS 34 dual-wall radome series, which has seen very satisfactory service in the Marine Corps and RAF since 1958.

However, the construction is somewhat expensive, requiring very high quality workmanship; it was subsequently abandoned in favor of a simpler design less subject to errors in workmanship.

Further calculations of deflections are included in the detailed analysis for the specific configurations. Of special note are the calculations for configurations 2 and 10, and the experimental model. Likewise, the Pulson and Tutt reports give actual values for the English bridge experiments.

PUTERSEARCH

01/18/ '73 14:34

!LOGIN: 1507BRD,C.

ID= D

!BASIC

>10 FOR P=0 TO 80 STEP 20

>20 D=((P/2)*54)/(2.5*216)

>30 PRINT P,D

>40 NEXT P

>50 PRINT

>60 FOR P1=0 TO 140 STEP 20

>70 D1=((P1/2)*54)/(4*216)

>80 PRINT P1,D1

>90 NEXT P1

>100 PRINT

>110 FOR P2=0 TO 180 STEP 20

>120 D2=((P2/2)*54)/(5*216)

>130 PRINT P2,D2

>140 NEXT P2

>150 END

>RUN

14:37 01/18

P	D
0	0
20	1
40	2
60	3
80	4

} $p = 2.5$

P1	D1
0	0
20	.625000
40	1.25000
60	1.87500
80	2.50000
100	3.12500
120	3.75000
140	4.37500

} $p = 4.0$

P2	D2
0	0
20	.500000
40	1
60	1.50000
80	2
100	2.50000
120	3
140	3.50000
160	4
180	4.50000

} $p = 5.0$

150 HALT

>SYS

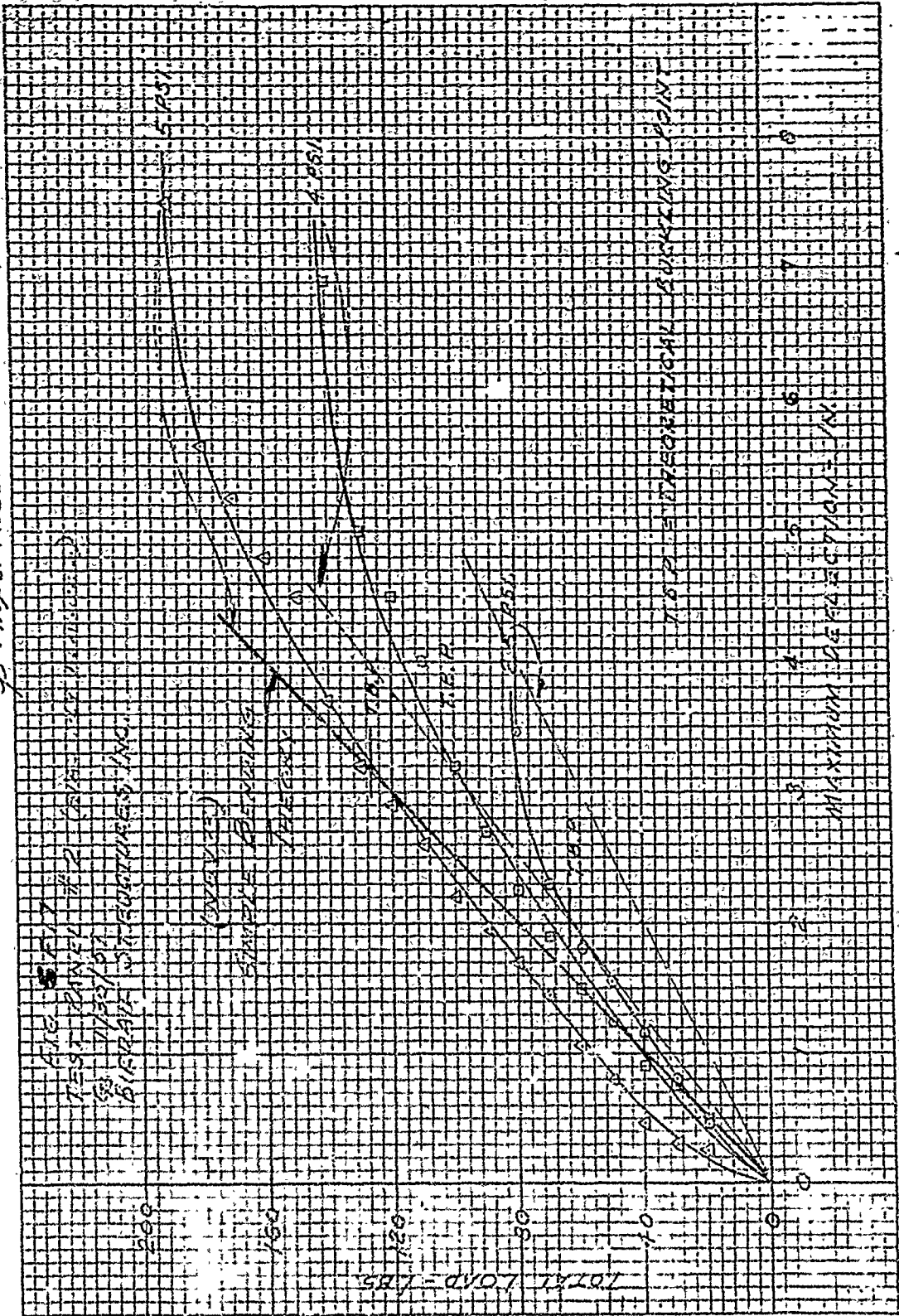
!BYE

01/18/ '73 14:38

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CCU 0.011

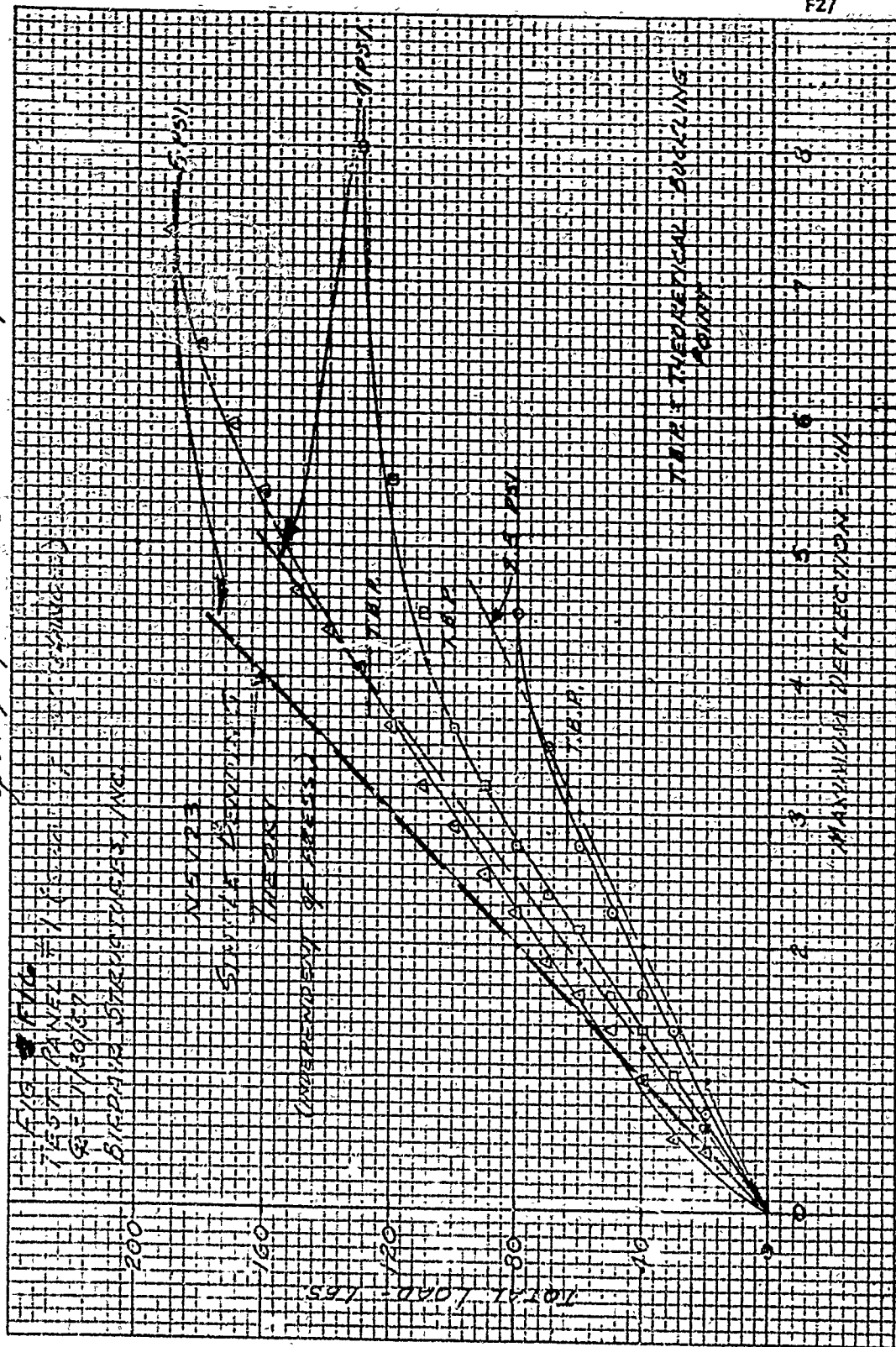
$P = \text{point load}$
 $L = \text{distance from supt.}$
 $\delta = \frac{(1/2)(L)^2}{pA}$
 $p = \text{infl. press.}$



$$S = \frac{(P/2)(L)}{PA}$$

$$L = \text{DISTANCE FROM SUPT.}$$

$$P = \text{INFLATION PRESS.}$$



APPENDIX-G

PRESSURIZATION

CALCULATIONS

Time required for inflation.

V. of cell 17,954 ¹³

Pressure required 3.6 psig.

In increments of 10% of the inflation pressure

$$P_c = (3.6)(.1)$$

$$= .36 \text{ psig} \quad \leftarrow$$

$$[P_g = P - P_c]$$

$$= 3.6 - .36$$

$$= 3.24 \text{ psig} \quad \leftarrow$$

$$[P_a = \text{Press. Atmosp.} + P_g]$$

$$= 14.7 + 3.24$$

$$= 17.94 \text{ psi} \quad \leftarrow$$

$$\left[\rho = 1.325 \frac{P_a}{T} \right]$$

$$= \frac{(1.325)(17.94)(2.036)}{(460 + 68)}$$

$$= 0.0769 \text{ #/ft}^3 \quad \leftarrow$$

NOTE: NOMENCLATURES ON G-5

$$\begin{aligned}
 [Q &= 5.976 K D_o^2 \sqrt{\frac{h}{\rho}}] \\
 &= (5.976)(16)(4.625)^2 \sqrt{\frac{(3.60 - .36)}{(.0769)(.03613)}} \\
 &= 2619 \text{ cfm} \quad \leftarrow
 \end{aligned}$$

$$[W = \frac{P_a V}{R T}]$$

$$W = \frac{(17.94)(144)(17954)}{(53.3)(460 + 68)}$$

$$= 1648 \text{ lbs.} \quad \leftarrow$$

$$[W_d = W_2 - W_1]$$

$$W_d = 1681 - 1648$$

$$= 33 \text{ lbs.} \quad \leftarrow$$

$$[V = \frac{W_d}{\rho}]$$

$$= 33 / .0769$$

$$= 429 \text{ cf}$$

$$[Q_a = \frac{Q_1 + Q_2}{2}]$$

$$= \frac{2793 + 2619}{2}$$

$$= 2706 \text{ CFM.} \quad \leftarrow$$

$$[T = \frac{V}{Q_a}]$$

$$= \frac{429}{2706}$$

$$= .158, .2 \text{ min.} \quad \leftarrow$$

The total time of inflation is
the sum of T = 9.20 minutes

TABLE I

P_c #/in ²	P_g #/in ²	P_m #/in ²	P #/in ²	Q in ³ /min	W	W_d	V	Q_c	T
0	3.6	13.3	.075	2793	1681	-	17934	2793	6.4
.36	3.24	17.94	.0769	2619	1648	33	429	206	5.2
.72	2.88	11.58	.0789	2437	1615	33	419	2529	4.2
1.08	2.52	17.22	.0800	2256	1581	34	422	2348	3.2
1.44	2.16	16.88	.0825	2064	1550	31	376	2160	2.2
1.80	1.80	16.50	.0843	1864	1525	35	415	1964	1.2
2.16	1.44	16.14	.0862	1669	1482	33	383	1756	1.2
2.52	1.08	15.76	.0880	1413	1450	32	364	1531	1.2
2.88	.72	15.42	.0899	1142	1415	35	390	277	1.3
2.94	.36	15.06	.0917	799	1383	32	349	970	1.4
3.6	0	14.7	.0935	250	1350	33	353	524	1.7
									9.20

Best Available Copy

P_c = Inflation pressure of the cell psig

P_g = Pressure differential across the orifice psig

P_a = Pressure in the cell--absolute psi

ρ = Density of air at the cell pressure lbs./cu. ft.

Q = Flow rate of inflation air into the cell cfm

Δ = as above

W_d = Incremental increase in weight in lbs.

V = Volume of the air weighing W_d pounds

Q_a = Average flow rate over the pressure increment cfm

T = Time required to complete the pressure increment in minutes

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